



**Calhoun: The NPS Institutional Archive**  
**DSpace Repository**

---

Theses and Dissertations

1. Thesis and Dissertation Collection, all items

---

1974-12

# Improvement of AN/TPQ-27 filter and control techniques.

Lentz, Robert Eugene

Monterey, California. Naval Postgraduate School

---

<http://hdl.handle.net/10945/17068>

---

This publication is a work of the U.S. Government as defined in Title 17, United States Code, Section 101. Copyright protection is not available for this work in the United States.

*Downloaded from NPS Archive: Calhoun*



Calhoun is the Naval Postgraduate School's public access digital repository for research materials and institutional publications created by the NPS community. Calhoun is named for Professor of Mathematics Guy K. Calhoun, NPS's first appointed -- and published -- scholarly author.

**Dudley Knox Library / Naval Postgraduate School**  
**411 Dyer Road / 1 University Circle**  
**Monterey, California USA 93943**

<http://www.nps.edu/library>

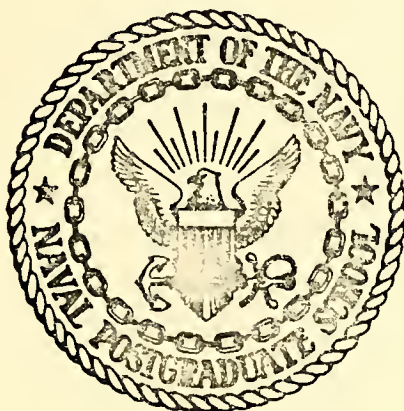
IMPROVEMENT OF AN/TPQ-27 FILTER  
AND CONTROL TECHNIQUES

Robert Eugene Lentz

Library  
Naval Postgraduate School  
Monterey, California 93940

# NAVAL POSTGRADUATE SCHOOL

## Monterey, California



# THESIS

IMPROVEMENT OF AN/TPQ-27 FILTER  
AND CONTROL TECHNIQUES

by

Robert Eugene Lentz

December 1974

Thesis Advisor:

H. A. Titus

Approved for public release; distribution unlimited.

T164073





| REPORT DOCUMENTATION PAGE  |                       | READ INSTRUCTIONS<br>BEFORE COMPLETING FORM                                |
|--|-----------------------|--|
| 1. REPORT NUMBER   | 2. GOVT ACCESSION NO. | 3. RECIPIENT'S CATALOG NUMBER  |
| 4. TITLE (and Subtitle)<br>Improvement of AN/TPQ-27 Filter and Control Techniques  |                       | 5. TYPE OF REPORT & PERIOD COVERED<br>Electrical Engineer<br>December 1974 |
| 7. AUTHOR(s)<br>Robert Eugene Lentz  |                       | 6. PERFORMING ORG. REPORT NUMBER   |
| 9. PERFORMING ORGANIZATION NAME AND ADDRESS<br>Naval Postgraduate School<br>Monterey, California 93940   |                       | 8. CONTRACT OR GRANT NUMBER(s)   |
| 11. CONTROLLING OFFICE NAME AND ADDRESS<br>Naval Postgraduate School<br>Monterey, California 93940   |                       | 10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS                |
| 14. MONITORING AGENCY NAME & ADDRESS (If different from Controlling Office)<br>Naval Postgraduate School<br>Monterey, California 93940   |                       | 12. REPORT DATE<br>December 1974   |
|  |                       | 13. NUMBER OF PAGES<br>201   |
|  |                       | 15. SECURITY CLASS. (of this report)<br>Unclassified                       |
|  |                       | 15a. DECLASSIFICATION/DOWNGRADING SCHEDULE                                 |
| 16. DISTRIBUTION STATEMENT (of this Report)<br><br>Approved for public release; distribution unlimited.  |                       |  |
| 17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)   |                       |  |
| 18. SUPPLEMENTARY NOTES  |                       |  |
| 19. KEY WORDS (Continue on reverse side if necessary and identify by block number)<br>Kalman Filter Application<br>AN/TPQ-27<br>Remote Guidance and Control<br>Radar Tracking  |                       |  |
| 20. ABSTRACT (Continue on reverse side if necessary and identify by block number)<br><br>A modified linear Kalman filter with deterministic forcing is used to improve the tracking capabilities of the Marine Corps AN/TPQ-27 remote tactical aircraft guidance system. Both sixth and ninth order filters are developed and used with the Precision and Coarse Guidance simulation programs. A technique for overcoming the effects of auto-pilot bias is presented and tested through simulation. |                       |  |



## Block #20 Continued

Precision Guidance control is modified to utilize angle error and angle error rate to generate corrective commands. Significant improvement in aircraft state estimation, bombing accuracy, and overall system response is shown. The Coarse Guidance algorithms and simulation program are nearly completely new and perform aircraft guidance to the bombing run with more than adequate precision under simulated conditions. The new version of the program is significantly less complex than the previous version and incorporates features which more realistically reflect actual conditions under which the system would be used.



Improvement of AN/TPQ-27  
Filter and Control Techniques

by

Robert Eugene Lentz  
Lieutenant, United States Navy  
B.S.E.E., University of Maryland, 1968

Submitted in partial fulfillment of the  
requirements for the degree of

ELECTRICAL ENGINEER

from the  
NAVAL POSTGRADUATE SCHOOL  
December 1974

Thesis  
L 526  
c. 1

## ABSTRACT

A modified linear Kalman filter with deterministic forcing is used to improve the tracking capabilities of the Marine Corps AN/TPQ-27 remote tactical aircraft guidance system. Both sixth and ninth order filters are developed and used with the Precision and Coarse Guidance simulation programs. A technique for overcoming the effects of autopilot bias is presented and tested through simulation. Precision Guidance control is modified to utilize angle error and angle error rate to generate corrective commands. Significant improvement in aircraft state estimation, bombing accuracy, and overall system response is shown. The Coarse Guidance algorithms and simulation program are nearly completely new and perform aircraft guidance to the bombing run with more than adequate precision under simulated conditions. The new version of the program is significantly less complex than the previous version and incorporates features which more realistically reflect actual conditions under which the system would be used.





## TABLE OF CONTENTS

|      |  |    |
|------|--|----|
| I.   | INTRODUCTION-----  | 8  |
| A.   | AN/TPQ-27 INTRODUCTION-----  | 8  |
| B.   | AN/TPQ-27 PROBLEM AREA DEFINITION-----   | 9  |
|      | 1. Problem Areas in Coarse Guidance-----   | 9  |
|      | 2. Problem Areas in Precision Guidance-----                                      | 9  |
| II.  | AIRCRAFT POSITION AND VELOCITY ESTIMATION-----                                   | 11 |
| A.   | BACKGROUND AND INTRODUCTION TO THE KALMAN<br>FILTER-----                         | 11 |
| B.   | KALMAN FILTER ASSUMPTIONS AND GENERAL<br>RECURSION EQUATIONS-----                | 12 |
| C.   | SELECTION OF REQUIRED SYSTEM MODEL ORDER-----                                    | 13 |
| D.   | DERIVATION OF THE COVARIANCE OF MEASUREMENT<br>NOISE MATRIX, $R(k)$ -----        | 15 |
| E.   | STATE PREDICTION EQUATIONS-----  | 20 |
|      | 1. State Prediction in the Linear Case-----                                      | 21 |
|      | 2. Aircraft Response to Bank Angle Commands-                                     | 22 |
|      | 3. State Prediction in the Nonlinear Case---                                     | 24 |
| F.   | KALMAN FILTER IMPLEMENTATION-----  | 27 |
|      | 1. Differences in RADAR6 and RADAR9-----   | 27 |
|      | 2. Initialization and Constant Array<br>Calculations-----                        | 29 |
| G.   | PREDICTION ERROR, THE GAIN SCHEDULE, AND<br>COVARIANCE OF AIRCRAFT MANEUVER----- | 31 |
| H.   | REDUCTION OF COMPUTATIONAL TIME-----   | 35 |
| III. | PRECISION GUIDANCE SIMULATION-----   | 37 |
| A.   | INTRODUCTION-----  | 37 |
| B.   | INITIALIZATION AND FILTER SETTling TIME-----                                     | 39 |



|     |   |    |
|-----|---|----|
| C.  | PRECISION GUIDANCE COORDINATE CONVENTIONS<br>AND TRANSFORMATIONS----- | 40 |
| D.  | LOOP GEOMETRY AND ERROR CALCULATIONS-----                             | 43 |
| E.  | AIRCRAFT CONTROLLER DESIGN-----                                       | 46 |
| F.  | PRECISION GUIDANCE PROGRAM IMPLEMENTATION----                         | 50 |
|     | 1. Main Program and Subroutines-----                                  | 50 |
|     | 2. Program Input and Output-----                                      | 50 |
| IV. | COARSE GUIDANCE SIMULATION-----                                       | 53 |
| A.  | INTRODUCTION-----   | 53 |
| B.  | PRE-MISSION DATA TABLE COMPUTATIONS AND<br>INITIAL CONDITIONS-----    | 54 |
|     | 1. True and Estimated Wind Components-----                            | 56 |
|     | 2. Mission Data Table Calculations-----                               | 58 |
|     | 3. Initial Position and Velocity of the<br>Aircraft-----              | 60 |
| C.  | AIRCRAFT POSITION, VELOCITY, AND ERROR<br>ESTIMATION-----             | 61 |
| D.  | COMMAND TURN CALCULATIONS-----  | 64 |
|     | 1. Time Remaining on Present Leg-----                                 | 65 |
|     | 2. Time Required to Complete the Turn-----                            | 67 |
|     | 3. Command Turn Timing Logic-----                                     | 71 |
| E.  | AIRCRAFT CONTROLLER DESIGN-----                                       | 72 |
| F.  | COARSE GUIDANCE PROGRAM IMPLEMENTATION-----                           | 75 |
|     | 1. Main Program and Subroutines-----                                  | 75 |
|     | 2. Program Input and Output-----                                      | 76 |
| V.  | PRESENTATION OF RESULTS-----  | 77 |
| A.  | PRECISION GUIDANCE PERFORMANCE COMPARISON----                         | 77 |
|     | 1. Filter Performance Comparison-----                                 | 79 |
|     | 2. Bombing Accuracy and Time Response<br>Comparison-----              | 81 |



|                                     |     |
|-------------------------------------|-----|
| B. COARSE GUIDANCE PERFORMANCE----- | 90  |
| APPENDIX A-----                     | 99  |
| APPENDIX B-----                     | 107 |
| APPENDIX C-----                     | 109 |
| COMPUTER OUTPUT-----                | 110 |
| LIST OF REFERENCES-----             | 200 |
| INITIAL DISTRIBUTION LIST-----      | 201 |



## I. INTRODUCTION

### A. AN/TPQ-27 INTRODUCTION

The AN/TPQ-27 system is a tactical aircraft guidance and control system used by the Marine Corps to guide strike force aircraft along a preplanned route, and then down a final leg for the purpose of performing precision bombing.

The mission control and guidance is divided into two modes. The first mode, called Coarse Guidance, takes the aircraft from a TACAN entry point through a series of straight paths and command turns. These "legs" of the Coarse Guidance run are defined by the leg end points. The actual route to be followed is determined by tactical considerations. The last leg is also the bombing leg. After proper entrance onto the final approach to the bombing leg, the second mode of the mission guidance control takes command; this is called Precision Guidance. During the Precision Guidance mode, very accurate aircraft position estimates are developed to enable bomb placement calculations which will be accurate to errors on the order of feet at the final impact point. The primary difference between these two modes, other than purpose, is the radar precision used to make the measurement of aircraft position. The resultant precision is also a function of the data rates of the respective radars, which differ significantly in this case.

The initial efforts on this system have suffered from some problems which are also apparent from observation of the





results of software simulations of actual missions. The purpose of this study was to look into various techniques currently employed in the simulation programs, and attempt to improve the response and overall accuracy of the system through the use of different and/or improved algorithms.

## B. AN/TPQ-27 PROBLEM AREA DEFINITION

The specific problem areas which were investigated were defined primarily through contact with personnel closely associated with the system's performance. Other areas were noted as in need of improvement during the familiarization and simulation trial phases of study.

### 1. Problem Areas in Coarse Guidance

Coarse guidance has suffered from many separate but related problems. Pilots have complained that the controls sent to the aircraft in the final moments before turning to a new leg have been violent. In addition, there have been complaints of not knowing where the aircraft was at any time other than having just exited from a "command turn," i.e., a turn from one leg onto a new leg, vice a course correction. The simulation program was found to be suffering from unnecessary complexity in some areas, and was apparently in need of refined estimation and control procedures.

### 2. Problem Areas in Precision Guidance

The single most prevalent complaint with the Precision Guidance program was the length of time required for the estimates to stabilize in order that an accurate determination on exactly when the bomb should be dropped could be made.



Again, this and other related problems with Precision Guidance seemed due to inadequate aircraft estimation algorithms, and a control scheme which was too simplistic in design.



## II. AIRCRAFT POSITION AND VELOCITY ESTIMATION

### A. BACKGROUND AND INTRODUCTION TO THE KALMAN FILTER

The technique previously used to provide noise filtering on aircraft position and velocity was a standard alpha-beta filter with parameters chosen to yield the "optimal" tracking capability in accordance with the theory developed in [1]. However, this reference also states that in the case when adaptive tracking is required, the  $\alpha$  parameter should be permitted to vary with observed high frequency power fluctuations in the error signal

$$e = x_n - x_{pn} \quad (1)$$

where  $x_n$  is the state estimation, and  $x_{pn}$  is the state prediction prior to measurement. Provisions for this variation were not included in the tracking algorithm which was implemented. In addition, the alpha-beta filter which was implemented was not an unbiased estimator of the aircraft state vector. This is due to the fact that as controls were used to cause changes in the free inertial model of the motion assumed by the alpha-beta filter, no corresponding changes were added to the filter states to account for this deterministically added control. This accounts for the exceptionally large and prolonged transient errors which resulted from large control bank commands.

The Kalman filter yields a minimum variance estimate of the state vector when the statistics of the noise are as



described below. This filter includes the effects of deterministic control commands to the aircraft to yield an estimator which is very nearly unbiased. The greatest improvement in estimation is yielded during the initial filter transient behavior. This is particularly critical in this application, in order to overcome the long filter settling period required by the alpha-beta filter.

#### B. KALMAN FILTER ASSUMPTIONS AND GENERAL RECURSION EQUATIONS

Application of the Kalman filter assumes that the discrete system under consideration satisfies

$$X(k+1) = \phi(k)X(k) + W(k) \quad (2)$$

$$Z(k) = H(k)X(k) + V(k) \quad (3)$$

where  $X$  is an  $n \times 1$  state vector,  $Z$  is an  $m \times 1$  output vector,  $W$  is a zero-mean  $n \times 1$  vector of state excitation white noise, uncorrelated with the zero-mean additive white noise vector  $V$ ,  $\phi$  is the state transition matrix ( $n \times n$ ), and  $H$  is the  $m \times n$  observation or measurement matrix. The assumed noise statistics are

$$E[V(k) V(j)^T] = R(k) \delta(k, j) \quad (4)$$

$$E\{\Gamma[W(k) W(j)^T]\Gamma^T\} = Q(k) \delta(k, j) \quad (5)$$

$$E[V(k) W(j)^T] = 0 \text{ for all } k, j \quad (6)$$

where

$$\delta(k, j) = \begin{cases} 0 & k \neq j \\ 1 & k = j. \end{cases} \quad (7)$$

The actual Kalman filter recursion equations are summarized





below, where  $\hat{X}(k/j)$  denotes the estimate of the state  $X(k)$  based upon the  $j$  measurement observations  $Z(1), Z(2), \dots, Z(j)$ .

$$P(k/k-1) = \phi(k, k-1)P(k-1/k-1)\phi(k, k-1)^T + Q(k) \quad (8)$$

$$G(k) = P(k/k-1)H(k)[H(k)P(k/k-1)H(k)^T + R(k)]^{-1} \quad (9)$$

$$P(k/k) = P(k/k-1) - G(k)H(k)P(k/k-1) \quad (10)$$

$$\hat{X}(k/k) = \hat{X}(k/k-1) + G(k)[Z(k) - H(k)\hat{X}(k/k-1)] \quad (11)$$

$$\hat{X}(k/k-1) = \phi(k, k-1)\hat{X}(k-1/k-1) + \Gamma(k)U(k-1) \quad (12)$$

where  $P(k/k-1)$  is the covariance of error for the state prediction vector  $\hat{X}(k/k-1)$ ,  $P(k/k)$  is the covariance of error matrix for the state estimation vector  $\hat{X}(k/k)$ , and  $G(k)$  is the gain matrix to be applied at the time of the  $k^{\text{th}}$  measurement. Further detail on the summary and development of the Kalman filter equations is available in [2], [3], and [4].

### C. SELECTION OF REQUIRED SYSTEM MODEL ORDER

The order of the filter refers to its capability to track a target exhibiting a particular type of motion without error, in a noiseless environment. For a single dimensional problem, a first order filter would estimate position only. Second order filters are capable of tracking a constant velocity target and estimating both position and velocity. Similarly, third order filters are capable of tracking a target exhibiting a constant acceleration profile, estimating position, velocity and acceleration in the process.

Documentation provided on the original AN/TPQ-27 programs indicated that the aircraft would be flying a constant airspeed



profile. This then indicates that the aircraft model might be appropriately chosen to be a free inertial ( $1/s^2$ ) plant. Command orders to the aircraft in the form of bank angles serve to change the aircraft's heading in a totally deterministic manner, provided the true transfer function of the aircraft is known with respect to roll response. In view of the above, it was originally thought that it would be sufficient to implement second order Kalman filters to estimate position and velocity in each of the three coordinates, yielding a sixth order filter.

It was later discovered that a problem known as autopilot bank angles bias exists with sufficient frequency and resultant imprecision that the order of the original feedback loop was increased to compensate for the error through the use of a discrete integrator [5]. Concepts such as integrators and digitally implemented lead-lag networks were to be avoided in the improved version of the simulation routines due to the resultant phase lags which they introduce. This is not to say that the steady-state response is in error, but simply that the time to reach that state is unsatisfactorily long. When simulations were run with non-zero autopilot bias bank angles in conjunction with second order Kalman filters, significant errors resulted.

A bias angle causes the aircraft to turn in a given direction at a constant heading rate. It was postulated that it might be possible to estimate the bias angle, and induce an anti-bias in the estimator, but the noise on the bias estimate proved to be excessive.



Third order filters will estimate a constant acceleration. The second attempt to overcome the bias problem was to postulate that the acceleration in the horizontal components would not change significantly over the relatively short periods of flight time in question. (Of course, if a bias existed and the aircraft was flown for a long enough time, the path flown would appear as a circle, and the third order filters could not possibly be satisfactory for that situation.) Thus, development of two separate filtering schemes was pursued. A sixth order (second order for each of three dimensions of motion) and a ninth order (third order for each of the three dimensions) filter were developed and tested. Use of the programs is very similar for each of the filters and is described below.

#### D. DERIVATION OF THE COVARIANCE OF MEASUREMENT NOISE MATRIX, $R(k)$

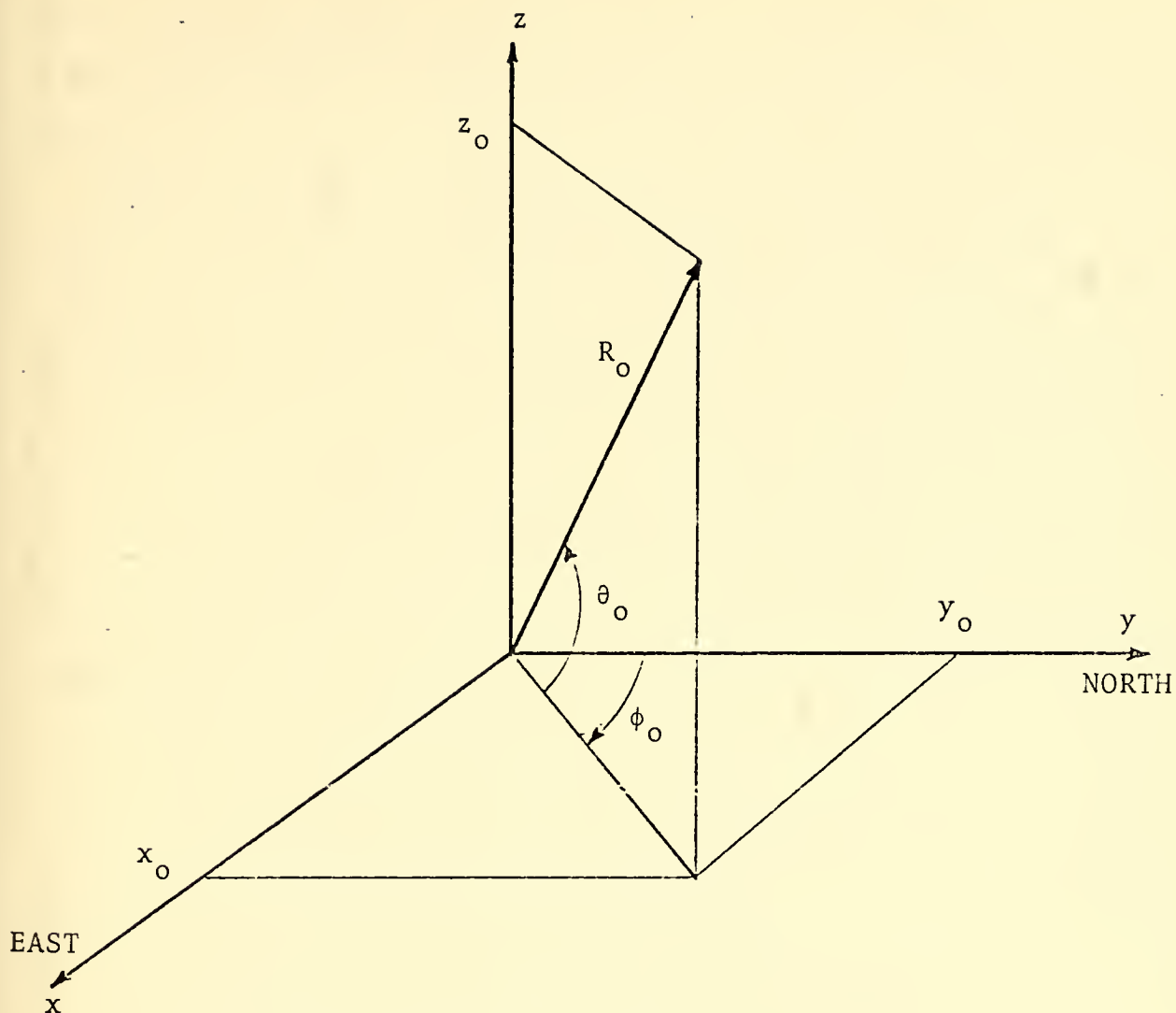
The Kalman Filter assumptions include linear relationships among measurements and states, as well as linear state transition dynamics. The first of these is of concern at this point. The states of concern in measurement have been selected as Cartesian coordinates  $(x,y,z)$ . However, the radar measures range, azimuth, and elevation. The assumed relationship between the states and the measured values are as shown in Fig. 1 and given by the equations below.

$$x = R \cos\theta \sin\phi \quad (13)$$

$$y = R \cos\theta \cos\phi \quad (14)$$

$$z = R \sin\theta \quad (15)$$





$$x_0 = R_0 \cos \theta_0 \sin \phi_0$$

$$y_0 = R_0 \cos \theta_0 \cos \phi_0$$

$$z_0 = R_0 \sin \theta_0$$

Figure 1. Illustration of assumed coordinate system used in the radar filters.





where  $R$  is the range to the aircraft,  $\theta$  is the elevation angle, and  $\phi$  is the azimuth angle of the aircraft from North.

Note that this form departs from that as given in (3) since the relationship between the measured variables and the states is a nonlinear one. If the states were directly observable, then (3) would appear as

$$\begin{bmatrix} z1(k) \\ z2(k) \\ z3(k) \end{bmatrix} = H(k) X(k) + \begin{bmatrix} v1(k) \\ v2(k) \\ v3(k) \end{bmatrix} \quad (16)$$

where for a sixth order system

$$H(k) = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix} \quad (17)$$

and

$$X(k) = [x(k) \dot{x}(k) y(k) \dot{y}(k) z(k) \dot{z}(k)]^T. \quad (18)$$

Similarly, for a ninth order system

$$X(k) = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \end{bmatrix} \quad (19)$$

and

$$X(k) = [x(k) \dot{x}(k) \ddot{x}(k) y(k) \dot{y}(k) \ddot{y}(k) z(k) \dot{z}(k) \ddot{z}(k)]^T. \quad (20)$$

Thus, in both cases the equations reduce to

$$\begin{bmatrix} z1(k) \\ z2(k) \\ z3(k) \end{bmatrix} = \begin{bmatrix} x(k) \\ y(k) \\ z(k) \end{bmatrix} + \begin{bmatrix} v1(k) \\ v2(k) \\ v3(k) \end{bmatrix} \quad (21)$$



where  $v1(k)$  is the  $k^{th}$  component of noise added to the x coordinate,  $v2(k)$  is the  $k^{th}$  component of noise added to the y coordinate, and  $v3(k)$  is the  $k^{th}$  component of noise added to the z coordinate. Due to the linearity of this problem, the three coordinate components might be considered as being statistically independent, in which case the  $R(k)$  matrix would probably be a diagonal array consisting of the individual coordinate measurement variances which would be constant for all  $k$ . For the nonlinear radar problem, the relationships for each  $k$  are

$$z1 = (R + n_r) \cos(\theta + n_\theta) \sin(\phi + n_\phi) \quad (22)$$

$$= x + v1$$

$$z2 = (R + n_r) \cos(\theta + n_\theta) \cos(\phi + n_\phi) \quad (23)$$

$$= y + v2$$

$$z3 = (R + n_r) \sin(\theta + n_\theta) \quad (24)$$

$$= z + v3$$

where  $n_r$ ,  $n_\theta$ , and  $n_\phi$  are incremental noise disturbances to the true range, elevation and azimuth, respectively. Expanding (22) yields

$$z1 = (R + n_r) [\cos\theta \cos n_\theta - \sin\theta \sin n_\theta] \cdot \quad (25)$$

$$[\sin\phi \cos n_\phi + \cos\phi \sin n_\phi].$$

It is assumed that  $n_\theta$  and  $n_\phi$  are small angle perturbations, and therefore that

$$\cos n_\theta \doteq \cos n_\phi \doteq 1 \quad (26)$$

$$\sin n_\theta \doteq n_\theta \quad (27a)$$



$$\sin n_\phi \doteq n_\phi \quad (27b)$$

(25) can then be written as

$$z1 \doteq (R + n_r)[\cos\theta \sin\phi - n_\theta \sin\theta \sin\phi \quad (28)$$

$$+ n_\phi \cos\theta \cos\phi - n_\theta n_\phi \sin\theta \cos\phi] \\ \doteq R \cos\theta \sin\phi + v1 \quad (29)$$

where

$$v1 \doteq -Rn_\theta \sin\theta \sin\phi + Rn_\phi \cos\theta \cos\phi - Rn_\theta n_\phi \sin\theta \cos\phi \\ + n_r \cos\theta \sin\phi - n_r n_\theta \sin\theta \sin\phi + n_r n_\phi \cos\theta \cos\phi \\ - n_r n_\theta n_\phi \sin\theta \cos\phi. \quad (30)$$

Similar developments for the z1 and z2 measurements yields

$$v2 \doteq -Rn_\theta \sin\theta \cos\phi - Rn_\phi \cos\theta \sin\phi + Rn_\theta n_\phi \sin\theta \sin\phi \\ + n_r \cos\theta \cos\phi - n_r n_\theta \sin\theta \cos\phi - n_r n_\phi \cos\theta \sin\phi \\ + n_r n_\theta n_\phi \sin\theta \sin\phi \quad (31)$$

and

$$v3 \doteq Rn_\theta \cos\theta + n_r \sin\theta + n_r n_\theta \sin\theta. \quad (32)$$

Repeating (4), the equation for the covariance of measurement error matrix is

$$R(k) = E \left\{ \begin{bmatrix} v1(k) \\ v2(k) \\ v3(k) \end{bmatrix} [v1(k) \ v2(k) \ v3(k)] \right\}. \quad (33)$$

It is assumed that  $n_r$  is much smaller than  $R$ . Evaluating the diagonal terms of  $R(k)$  yields

$$R(1,1) \doteq R^2 \sigma_\theta^2 \sin^2\theta \sin^2\phi + R^2 \sigma_\phi^2 \cos^2\theta \cos^2\phi \\ + R^2 \sigma_\theta^2 \sigma_\phi^2 \sin^2\theta \cos^2\phi + \sigma_r^2 \cos^2\theta \sin^2\phi \quad (34)$$



$$R(2;2) \doteq R^2\sigma_\theta^2 \sin^2\theta \cos^2\phi + R^2\sigma_\phi^2 \cos^2\theta \sin^2\phi \\ + R\sigma_\theta^2\sigma_\phi^2 \sin^2\theta \sin^2\phi + \sigma_r^2 \cos^2\theta \cos^2\phi \quad (35)$$

$$R(3,3) \doteq R^2\sigma_\theta^2 \cos^2\theta + \sigma_r^2 \sin^2\theta. \quad (36)$$

The off-diagonal elements are simply the expected values of the cross product terms, and are computed in the same way yielding

$$R(1,2) \doteq R^2\sigma_\theta^2(1 - \sigma_\theta^2)(\sin^2\theta \sin\phi \cos\phi) \\ + (\sigma_r^2 - R^2\sigma_\phi^2)(\cos^2\theta \sin\phi \cos\phi) \quad (37)$$

$$R(2,3) \doteq (\sigma_r^2 - R^2\sigma_\theta^2)(\sin\theta \cos\theta \cos\phi) \quad (38)$$

$$R(1,3) \doteq (\sigma_r^2 - R^2\sigma_\theta^2)(\sin\theta \cos\theta \sin\phi). \quad (39)$$

Due to the symmetry of the  $R(k)$  array, it is also true that

$$R(2,1) = R(1,2) \quad (40)$$

$$R(3,1) = R(1,3) \text{ and} \quad (41)$$

$$R(3,2) = R(2,3). \quad (42)$$

Note that the  $R(k)$  matrix is in fact not a constant array, but is one which is state dependent, or rather  $R$ ,  $\theta$ , and  $\phi$  dependent.

#### E. STATE PREDICTION EQUATIONS

The state prediction equations are used to predict ahead from the current estimate to some arbitrary future point in time. Normally this time is that of the next measurement, however, this is not always the case. As a relevant example, in Coarse Guidance, it is required to predict ahead several times between radar samples, due to the long sampling interval





of the radar, and the need to precisely determine times to order command turns.

### 1. State Prediction in the Linear Case

The analysis which follows will be addressed primarily to the ninth order case. The state vector is given in (20). The strictly linear prediction equations are given by (12) where

$$\phi(k, k-1) = \begin{bmatrix} 1 & T & \frac{T^2}{2} & | & 0 & 0 & 0 & | & 0 & 0 & 0 \\ 0 & 1 & T & | & 0 & 0 & 0 & | & 0 & 0 & 0 \\ 0 & 0 & 1 & | & 0 & 0 & 0 & | & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & | & 1 & T & \frac{T^2}{2} & | & 0 & 0 & 0 \\ 0 & 0 & 0 & | & 0 & 1 & T & | & 0 & 0 & 0 \\ 0 & 0 & 0 & | & 0 & 0 & 1 & | & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & | & 0 & 0 & 0 & | & 1 & T & \frac{T^2}{2} \\ 0 & 0 & 0 & | & 0 & 0 & 0 & | & 0 & 1 & T \\ 0 & 0 & 0 & | & 0 & 0 & 0 & | & 0 & 0 & 1 \end{bmatrix} \quad (43)$$

$$\Gamma(k) = \begin{bmatrix} T^3/6 & 0 & 0 \\ T^2/2 & 0 & 0 \\ T & 0 & 0 \\ 0 & T^3/6 & 0 \\ 0 & T^2/2 & 0 \\ 0 & T & 0 \\ 0 & 0 & T^3/6 \\ 0 & 0 & T^2/2 \\ 0 & 0 & T \end{bmatrix} \quad (44)$$



and

$$U(k) = [\dot{a}_x(k) \quad \dot{a}_y(k) \quad \dot{a}_z(k)]^T. \quad (45)$$

Note that although in general the  $\phi$  and  $\Gamma$  matrices are functions of  $k$ , in this case they are not. This is an arbitrary choice. Normally,  $T$  represents the interval between sampling points and is a constant. If one wished to predict ahead by  $2T$ , he could either perform the prediction operation twice in succession, or simply compute a new  $\phi$  and  $\Gamma$  matrix using  $2T$  in place of  $T$ . The former technique is used in this study.

The  $U(k)$  array represents the deterministic forcing for each of the three dimensions; the units are distance per  $\text{sec}^3$  since the forcing is an acceleration rate. (For the sixth order filter  $U(k)$  is an acceleration (distance/ $\text{sec}^2$ ).) This must be a function of  $k$  since at each time point the control to the aircraft may be different, and in general will be different.

The above linear prediction equations of motion are those which would normally be used in a Kalman Filter. However, it was found that these equations did not yield results of sufficient accuracy. A nonlinear technique was required to obtain precise results. This is derived below, along with the equations for aircraft response to a bank angle command.

## 2. Aircraft Response to Bank Commands

The aircraft is sent bank angle commands in order to cause heading changes. The flight profile is assumed to be a coordinated turn, in which there is no motion in the vertical plane, and the heading rate change is proportional to the



bank angle, as described in [6]. The relationship is

$$\dot{\psi} = (g/V) \phi_a \quad (46)$$

where  $\dot{\psi}$  is the heading rate in degrees/sec,  $g$  is the earth's gravitational constant (32.2 ft/sec<sup>2</sup>),  $V$  is the airspeed in ft/sec, and  $\phi_a$  is the actual angle of bank.

The roll transfer function of the aircraft can be approximated by

$$\frac{\phi(s)}{\phi_c(s)} = 1/(s\tau_b + 1) \quad (47)$$

as given in [6], where  $\tau_b$  is the response time constant.  $\tau_b$  is a function of the particular aircraft in use. The discretized version of the solution to the differential equation resulting from (47) is

$$\phi(k) = \phi_c(k-1)(1 - e^{-T/\tau_b}) + \phi(k-1)e^{-T/\tau_b} \quad (48)$$

where  $T$  is the interval between predictions,  $\phi_c$  is the commanded bank angle, and  $\phi(k)$  is the actual bank angle at time  $T(k)$ . Then the turning rate is

$$\dot{\psi}(k) = (g/V) \phi(k). \quad (49)$$

To get the incremental heading angle change over the time  $T$ , integrate (49).

$$\begin{aligned} \Delta\psi(k) &= \int_0^T \dot{\psi} \, dt = (g/V) \int_0^T \phi(k) \, dt \\ &= (g/V) \left[ \phi_c(k)t + (\phi(k-1) - \phi_c(k)) \frac{e^{-\frac{t}{\tau_b}} - 1}{-\frac{1}{\tau_b}} \right] \bigg|_0^T \end{aligned} \quad (50)$$



$$= (g/V) [\phi_c(k)T + (\phi(k-1) - \phi_c(k))(\tau_b)(1 - e^{-T/\tau_b})]. \quad (50)$$

Then

$$\psi(k) = \psi(k-1) + \Delta\psi(k). \quad (51)$$

### 3. State Prediction in the Nonlinear Case

A ninth order filter is assumed for this analysis.

The analysis includes effects of wind motion in x and y, and assumes knowledge of the wind components. Since the filter assumes a constant acceleration track, the acceleration prediction equations are

$$\ddot{x}(k/k-1) = \ddot{x}(k-1/k-1) \quad (52a)$$

$$\ddot{y}(k/k-1) = \ddot{y}(k-1/k-1) \quad (52b)$$

$$\ddot{z}(k/k-1) = \ddot{z}(k-1/k-1). \quad (52c)$$

Since the new heading is known in terms of the command bank angle, the predicted velocities are

$$\hat{\dot{x}}(k/k-1) = \hat{V}(k-1)\sin[\psi(k)] + W_x + \hat{\dot{x}}(k-1/k-1)T \quad (53a)$$

$$\hat{\dot{y}}(k/k-1) = \hat{V}(k-1)\cos[\psi(k)] + W_y + \hat{\dot{y}}(k-1/k-1)T \quad (53b)$$

$$\hat{\dot{z}}(k/k-1) = \hat{\dot{z}}(k-1/k-1)T \quad (53c)$$

where  $\hat{V}(k-1)$  is the estimated air speed at time  $T(k-1)$ , and  $W_x$  and  $W_y$  are the estimated wind components. The predicted position is approximated through the use of numerical integration using the Euler-Maclaurin summation formula, retaining only the first correction term. In general, this formula is given by [7] as

$$\int_{t_0}^{t_n} f(t)dt \approx T \sum_{i=0}^n f_i - \frac{T^2}{2} (f_0 + f_n) - \frac{T^2}{12} (f'_n - f'_0) + \dots \text{h.o.t.} \quad (54)$$





The equations involving the integrals are

$$\hat{x}(k/k-1) = \hat{x}(k-1/k-1) + \int_{T(k-1)}^{T(k)} \dot{x}(t) dt \quad (55a)$$

$$\hat{y}(k/k-1) = \hat{y}(k-1/k-1) + \int_{T(k-1)}^{T(k)} \dot{y}(t) dt \quad (55b)$$

$$\hat{z}(k/k-1) = \hat{z}(k-1/k-1) + \int_{T(k-1)}^{T(k)} \dot{z}(t) dt \quad (55c)$$

Applying (54) yields

$$\begin{aligned} \hat{x}(k/k-1) &= \hat{x}(k-1/k-1) + \frac{T}{2} [\hat{\dot{x}}(k-1/k-1) + \hat{\dot{x}}(k/k-1)] \\ &\quad - \frac{T^2}{12} [\hat{\ddot{x}}_t(k/k-1) - \hat{\ddot{x}}_t(k-1/k-1)] \end{aligned} \quad (56a)$$

$$\begin{aligned} \hat{y}(k/k-1) &= \hat{y}(k-1/k-1) + \frac{T}{2} [\hat{\dot{y}}(k-1/k-1) + \hat{\dot{y}}(k/k-1)] \\ &\quad - \frac{T^2}{12} [\hat{\ddot{y}}_t(k/k-1) - \hat{\ddot{y}}_t(k-1/k-1)] \end{aligned} \quad (56b)$$

$$\hat{z}(k/k-1) = T \hat{\dot{z}}(k/k-1) \quad (56c)$$

where  $\ddot{x}_t$  and  $\ddot{y}_t$  represent total accelerations in x and y. The simplification of the equation used to predict altitude is a result of the fact that there is no deterministic forcing in that direction.

A discussion of the relationship between the acceleration estimate  $\hat{\ddot{x}}(k/k-1)$  and the total accelerations shown in (56a) and (56b) is required at this point. The purpose of estimating an acceleration is due to the fact that bias bank angles exist which tend to cause a continuous turning motion,



and thus additional and unknown accelerations in the x and y directions. The prediction method as described above will place the aircraft at exactly the correct point with the correct velocity if there is no bias. In this case, the estimator will estimate that zero additional acceleration is present. In the case in which an unknown bias bank angle is present, the prediction equations will not be moving the aircraft heading angle the correct number of degrees/sec and thus lag will develop in the filter. This lag will cause a non-zero acceleration to be estimated, and this value will subsequently be added appropriately to the respective velocity components in order to compensate for the insufficient motion.

In summary, the acceleration estimate is not an estimate of the total acceleration, but is only an estimate of that acceleration which is unknown, due possibly to a variety of causes, but due primarily to an unknown bias angle in the autopilot roll reference. Thus the derivatives with respect to time of the velocity components in (56a) and (56b) do not equate to the acceleration estimates. Rather, they may be computed by differentiating equations (53) with respect to time and assuming that  $\hat{\ddot{X}}(k-1/k-1)$  is approximately constant. This yields

$$\hat{\ddot{x}}_t(k/k-1) = \hat{V}(k-1) \cos[\psi(k)] \dot{\psi}(k) \quad (57a)$$

$$\hat{\ddot{y}}_t(k/k-1) = -\hat{V}(k-1) \sin[\psi(k)] \dot{\psi}(k) \quad (57b)$$

and



$$\hat{\ddot{x}}_t(k-1/k-1) = \hat{V}(k-1) \cos[\psi(k-1)] \dot{\psi}(k-1) \quad (58a)$$

$$\hat{\ddot{y}}_t(k-1/k-1) = -\hat{V}(k-1) \sin[\psi(k-1)] \dot{\psi}(k-1). \quad (58b)$$

## F. KALMAN FILTER IMPLEMENTATION

Two separate Kalman filter subroutines were developed to simulate the operation and filtering of the radar processor. RADAR6 is the sixth order filter and RADAR9 is the ninth order filter. Their implementation in software is very similar; the differences are described below along with specific characteristics of the Kalman filter which apply to both versions. A general flow diagram for the filter is presented as Fig. 2.

### 1. Differences in RADAR6 and RADAR9

The obvious difference between the two filters is that one is capable of tracking a maneuvering aircraft with nonzero autopilot bank angle bias, and the other is not. This is due to the fact that the sixth order filter does not include the acceleration states in x, y, and z. The price paid for this additional estimation capability is an increase in computation time and program size. As implemented, the ninth order filter requires about 32 percent more storage allocation in memory than does RADAR6; RADAR6 requires about 76 K bytes of storage on an IBM 360-67. The increased computational time is difficult to judge since all timing data refers to the running of the overall program. The estimate for increased run time for the ninth order filter is on the order of 20 to 50 percent, depending on overall program run time.

The increased run time and storage requirements result from the requirement that the ninth order filter must have



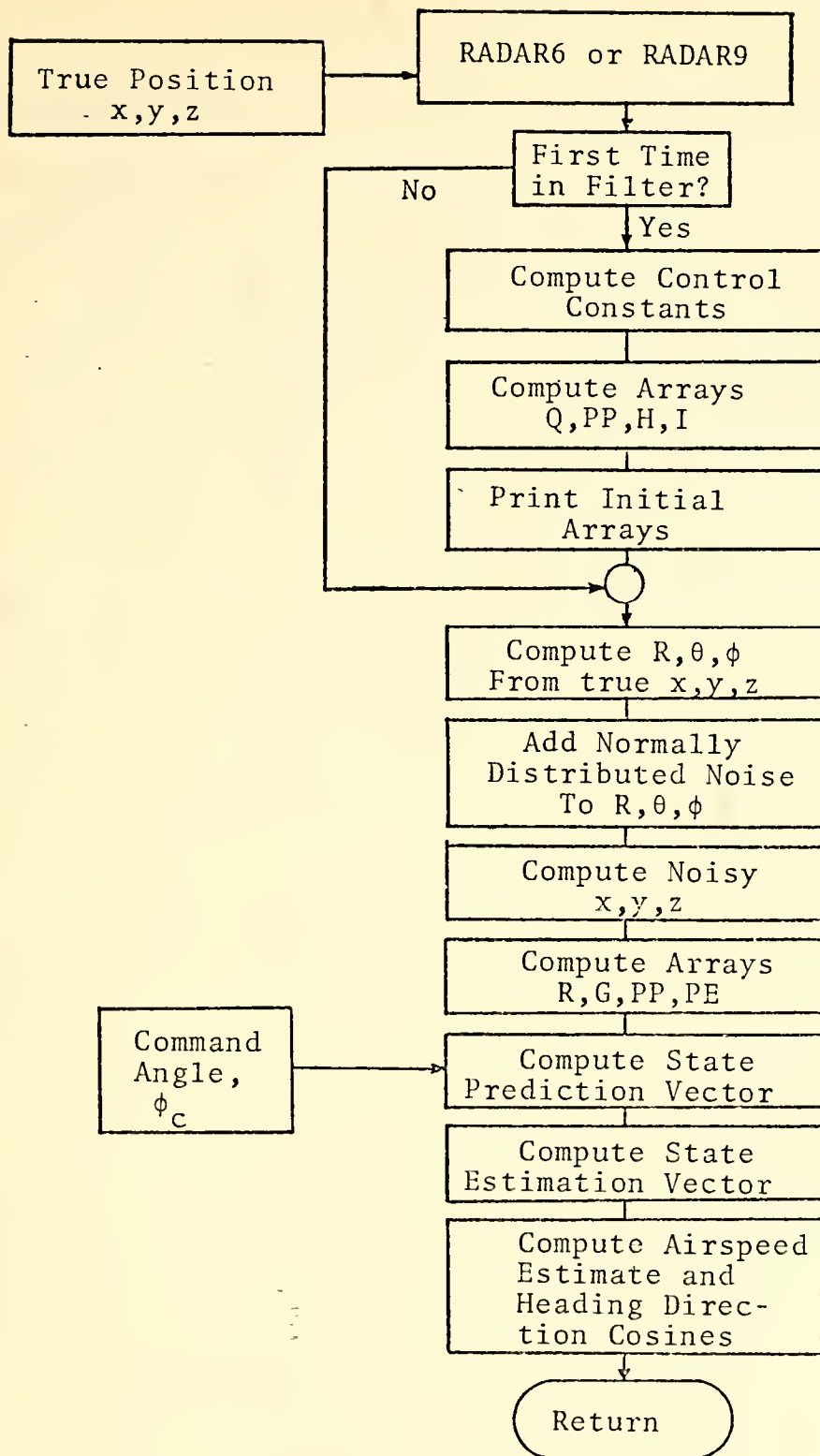


Figure 2. General block diagram of Radar Subroutines.





arrays which are  $9 \times 9$ , while the sixth order filter requires only arrays which are  $6 \times 6$ ; 18 of these arrays are involved resulting in a factor of 2.25 increase in array storage alone.

The prediction calculations for the sixth order filter differ from the ninth order filter only in the fact that the acceleration terms are missing in augmenting the predicted velocity components.

RADAR6 was used to develop the Coarse Guidance program since no mention of autopilot bias problems was found in the available documentation on that original system, [8] and [9]. RADAR9 was developed directly in response to the bias problem and was therefore used exclusively in the improvement of the Precision Guidance simulation program. The two subroutines could be interchanged to work with the other simulation mode's program in a matter of minutes, should this be desired.

## 2. Initialization and Constant Array Calculations

Upon entering either RADAR subroutine for the first time, logic passes control through a section of constant array calculation and definition of program constants. The constants specified at this point are primarily those which are used in bank and turn angle equations. These are a function of the aircraft type and update intervals and remain constant throughout a given simulation run.

A total of five arrays are defined at the program start and remain constant. An Identity array of order equal to the filter order is set up. The Measurement matrix, (H),



as given in either (17) or (19), depending on filter order is then defined. The state transition array,  $\phi$ , is considered constant for this application and is defined in accordance with the filter order. The Q matrix, which is a measure of the expected unknown random forcing to be applied to the system is computed using the  $\Gamma$  array as given in (44) (for the ninth order filter) in conjunction with the expected value of the random forcing array, W. For this study, W has been set to 0. The use and effects of non-zero values in this array are discussed below.

The covariance of the initial state prediction vector is set to  $10^6$ , a somewhat arbitrarily large number. The effect of choosing such a large variance on the states is to cause the filter to set the initial state estimation vector equal to the observation. In other words, the filter essentially ignores the *a priori* information set in as initial conditions. This is a very typical method of initializing a linear Kalman filter, when little confidence is placed on any initial estimate of the states. The original simulation programs followed this practice (of zero initialization) and it was continued in the improved version. However, considerable improvement in initial filter settling for the Kalman filters implemented could be achieved through the use of good initial conditions. The improved version of Coarse Guidance yields good estimates of the aircraft position, and in a "pass-off" to the Precision Guidance mode in a "live run" the states active in Coarse Guidance at the time would make



valid initial conditions for the Precision Guidance radar filter.

#### G. PREDICTION ERROR, THE GAIN SCHEDULE, AND COVARIANCE OF AIRCRAFT MANEUVER

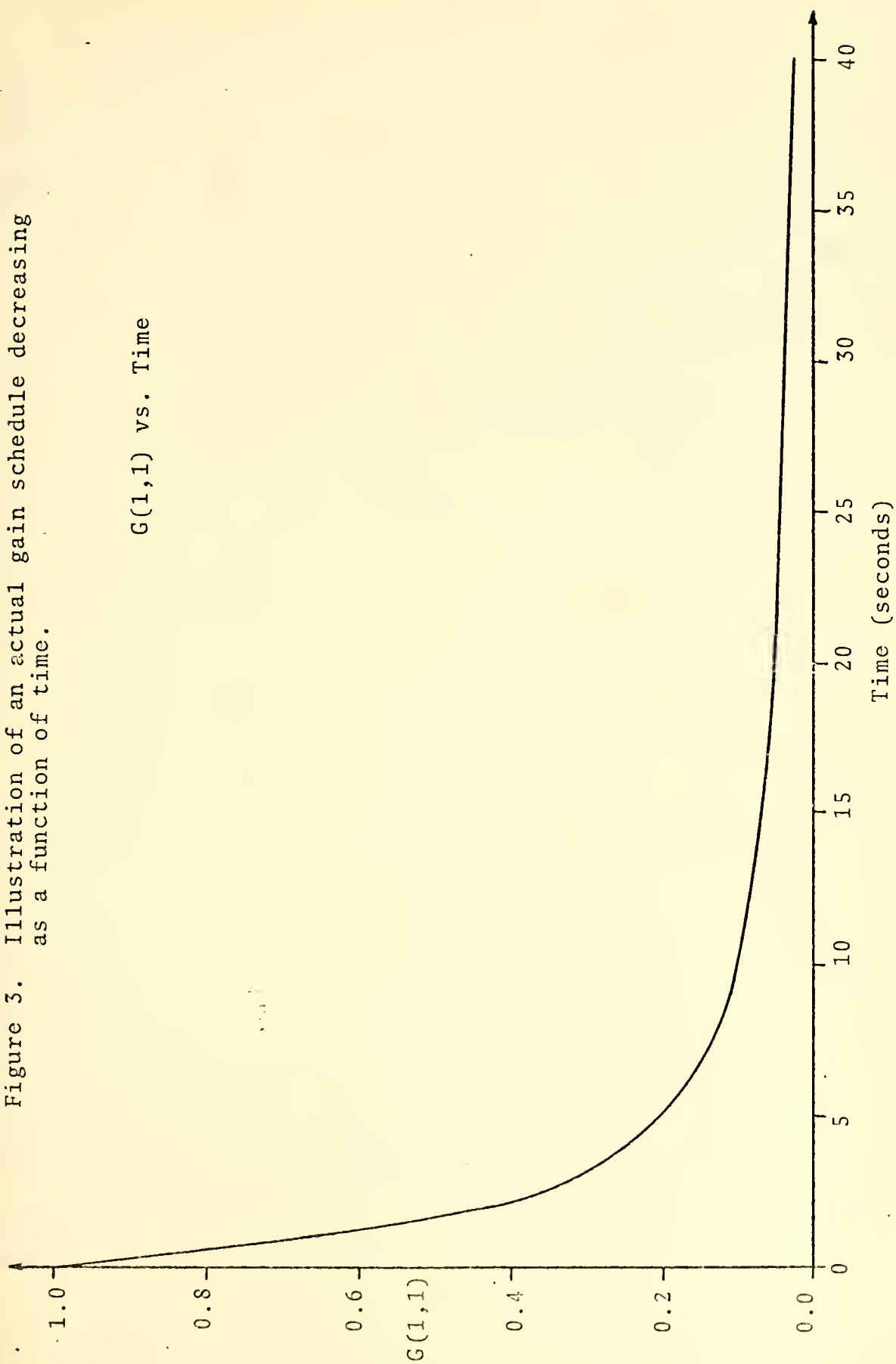
The gain matrix,  $G(k)$ , determines to what extent the data will be permitted to affect the state estimation. During the initial few estimations, the data usually always plays a large role in determining states, due to the large uncertainties in the actual states specified by the large covariances of prediction and estimation. As more data is taken, the covariances fall, and there is less requirement to accept noisy data into the filter to update the state estimate. Figure 3 shows a plot of the typical gain schedule for the x coordinate,  $G(1,1)$  term as a function of time. Values for the primary gain terms in y and z are similar. The curve is approximately exponential in shape, starts essentially at 1.0 at time zero, and decreases monotonically. As can be seen from (9), the exact values in the gain matrix depend on a multitude of variables, including the states themselves in the form of the R matrix.

Absolute compliance with the Kalman filter assumptions results in a gain schedule which is optimal in the sense that the state estimates will be of minimum variance. The use of changing gains with time is implicit. Note that in the original simulation programs, only constant gain filters were used, or in a few instances, filters which started at one constant gain value and then switched to one different set of gains.



Figure 3. Illustration of an actual gain schedule decreasing as a function of time.

$G(1,1)$  vs. Time







The gains are related to the filter bandwidth. High gains correspond to wide bandwidth since they "let in" nearly all of the measured data, including the noise on the data. Lower gains correspond to narrow band filters since very little data gets into the state estimation calculations. Use of low gains also resembles a narrow band low pass filter in the phase lag which results in the state estimation vector due to an abrupt change in the actual states. When this results, large differences begin to develop in the prediction residual of the estimation equation (11):

$$E(k) = Z(k) - H(k)\hat{X}(k/k-1). \quad (59)$$

In this case, (59) simplifies to

$$E_x = x_{data} - \hat{x}(k/k-1) \quad (60a)$$

$$E_y = y_{data} - \hat{y}(k/k-1) \quad (60b)$$

$$E_z = z_{data} - \hat{z}(k/k-1). \quad (60c)$$

As the differences in equations (60) begin to be biased either positively or negatively over a period of time, the filter will begin to integrate to a new trajectory in state space to compensate for the fact. The lower the gains, the longer this process will take.

If no random excitation noise, or no unknown forces or uncertainties are present in the system whose states are to be estimated, then the proper setting for  $W$ , the covariance of random state excitation, is  $\underline{0}$ . Since the  $Q$  array in (9) is

$$Q(k) = \Gamma E[W W^T] \Gamma^T, \quad (61)$$



if  $W$  is  $\underline{0}$ , then  $Q$  will also be  $\underline{0}$ . Examination of (9) in this case will reveal that as  $t \rightarrow \infty$  the gain schedule will go to zero, and as a result data will have little effect on the state estimation process after a relatively short period of time after initialization. This is fine if all factors are known.

In real systems, all factors affecting the states are rarely known. Uncertainties in AN/TPQ-27 might include wind velocity, exact aircraft roll response, biases in measurement equipment, and time variations of all of these.

The goal in establishing improved simulation programs was to devise techniques which would perform the required estimation and tracking assuming the above uncertainties did not exist to a significant extent. This attitude seemed to follow that used in the generation of the original program. It was recognized that use of a gain schedule which goes to zero is not a likely useable solution to the problem; however, it did seem reasonable to try to generate a solution which worked with zero  $Q$  when the uncertainties did not exist. With this accomplished, actual utilization of the algorithms against real data will determine the extent to which the bandwidth must be opened to achieve the best results.

Selection of  $Q$  is a problem which perpetually plagues users of the Kalman filter. Any given data set will have a given  $Q$  which will yield best results in terms of a specified performance criteria, normally tracking precision. The  $Q$  cannot be selected with the benefit of hindsight, and must be chosen to yield the optimum performance over the ensemble of state trajectories of interest. The normal method for finding



this value would be to take as many raw data tracks as possible, and try to determine the  $Q$  using statistical methods.

An alternate technique to generate  $Q$  on-line through the use of prediction error is described in [10]. In this paper, Aldrick and Krabill propose the calculation of  $Q$  by the following method:

$$Q(k) = a[Del(k) \ Del(k)^T] + b[Del(k-1) \ Del(k-1)^T] \quad (62)$$

where  $a$  and  $b$  are constants to be determined by analysis of actual data, and

$$Del(k) = \hat{X}(k/k) - \hat{X}(k/k-1) . \quad (63)$$

This method was investigated to a limited extent, and showed some promise if refined. Simple use of (62) seems to open the bandwidth wider than is desired. It has the advantage over the use of some constant  $Q$  for all runs that, in theory, if no uncertainties exist, the  $Del(k)$  arrays will be zero and thus  $Q$  will be  $\underline{0}$ . Thus, wide bandwidth is achieved only when required, as determined by prediction success. In practice however, it was found that this method caused the gains to oscillate, and created excessive error.

#### H. REDUCTION OF COMPUTATIONAL TIME

The most obvious disadvantage of using the Kalman filter compared with the constant gain alpha-beta filter is the increase in complexity and computation time required to compute this optimal gain schedule. There are several techniques which can be employed to reduce this burden, all of which result in further loss of optimality, but to limited extents.



In general, the R matrix is a function of the states or position of the aircraft. If the rough start and end points for the tracks to be followed are known in advance of the mission, it is possible to compute the average R,  $\theta$ , and  $\phi$  and thus an average R matrix. Unless R,  $\theta$ , and  $\phi$  vary over wide ranges, the loss in optimality by this approximation should be small. Since the gain schedule is state dependent only to the extent that R is state dependent, the gain schedule can now be computed and stored in a mission data table, and thus need not be computed on-line. Since 18 different gains are required by RADAR6 and 27 by RADAR9 for each sampling time, this becomes a rather large problem if auxiliary storage is not available.

An alternative to storing the gain schedule is to fit each of the gain schedules to either an exponential curve or to a function of the type

$$f(x) = a + b x^{-1} + c x^{-2} + d x^{-3} + \dots \quad (64)$$

Then only 18 (or 27) computations would be required at each sampling time.

Whatever technique is chosen to approximate the true gain schedule, it will not be nearly as sub-optimal as a constant gain over all time, or two constants which are switched in and out.





### III. PRECISION GUIDANCE SIMULATION

#### A. INTRODUCTION

A limited amount of Precision Guidance simulation program documentation was provided with the original version of the program. This greatly facilitated understanding of the original version of the program, and also subsequent modification for improvement. Many of the original concepts used were not changed. Input and output formats were revised for ease of use and to provide a greater indication of program performance. Since large portions of the original program's logic and coding have been retained, these may be mentioned and summarized lightly for continuity. The derivations and justification of assumptions in these areas will not be addressed, as they are considered to be adequately documented in the existing system documentation.

A block diagram of the simulation program control loop is presented in Fig. 4. In a few words, the program starts with the aircraft at some designated position and velocity with respect to a target which is to be bombed. After a 6 sec filter settling period, control logic determines the lateral error which will be incurred if the present flight profile is continued until time to release the bomb. Functions of the lateral error become the controlling mechanism to generate command bank angles which cause the aircraft to change course. It is emphasized that all control commands



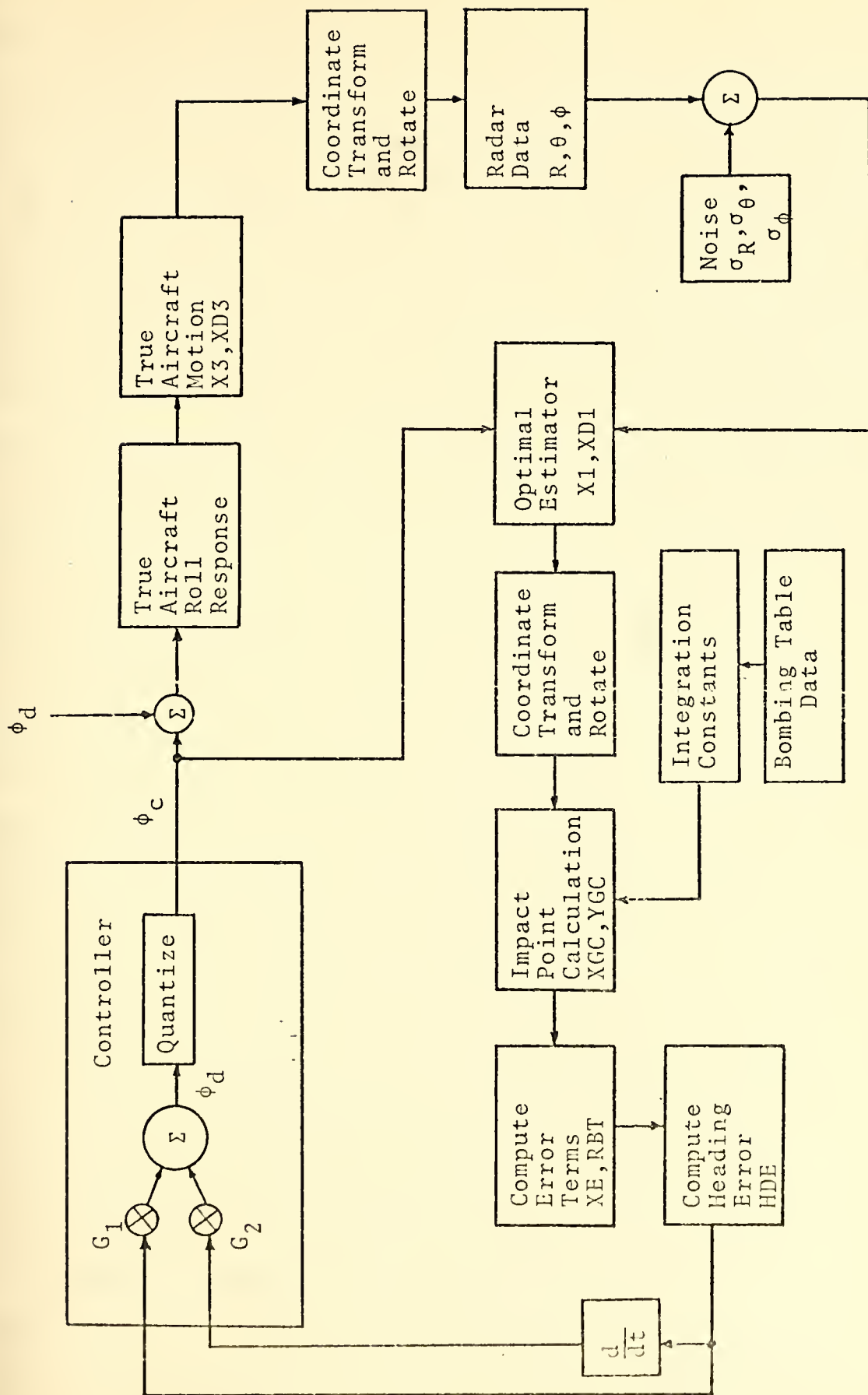


Figure 4. Simulation Program block diagram.



are based on estimated positions and velocities. Thus it may be possible to drive the estimated lateral error to zero, and still miss the target considerably, if the state estimation vector is in error. One further comment is that the problem is not totally one of estimation and control. The aircraft has a bank angle limitation imposed of  $\pm 30$  degrees. This limits the turning rate such that, depending on the initial position and velocity with respect to the target, the aircraft may not be physically able to come about to the correct heading in the time required. Examples of this situation are provided.

#### B. INITIALIZATION AND FILTER SETTling TIME

The new simulation program is functionally similar to the original version in initialization. The same variables are used wherever meaningful. The coordinate transformation vectors and matrices defined during initialization are retained, as are all equations for operating in the dive bombing mode. (The original program provided logic for executing a diving mode, but use of this mode has not been investigated in this study.)

The precision radar sampling rate is 8 Hz. No action except state estimation is taken during the first 2 sec of the simulation run. At the 2 sec point, logic is executed to enable prediction of the lateral error at 6 seconds into the run. The 4 second lag is assumed to be due to an attempt to simulate the fact that the actual computer used is computer-time limited, thus constraining the integration logic to



execution at no more than 0.25 Hz. At  $t = 6$  seconds, the lateral error is first estimated, and the first non-zero command to the aircraft can be transmitted.

### C. PRECISION GUIDANCE COORDINATE CONVENTIONS AND TRANSFORMATIONS

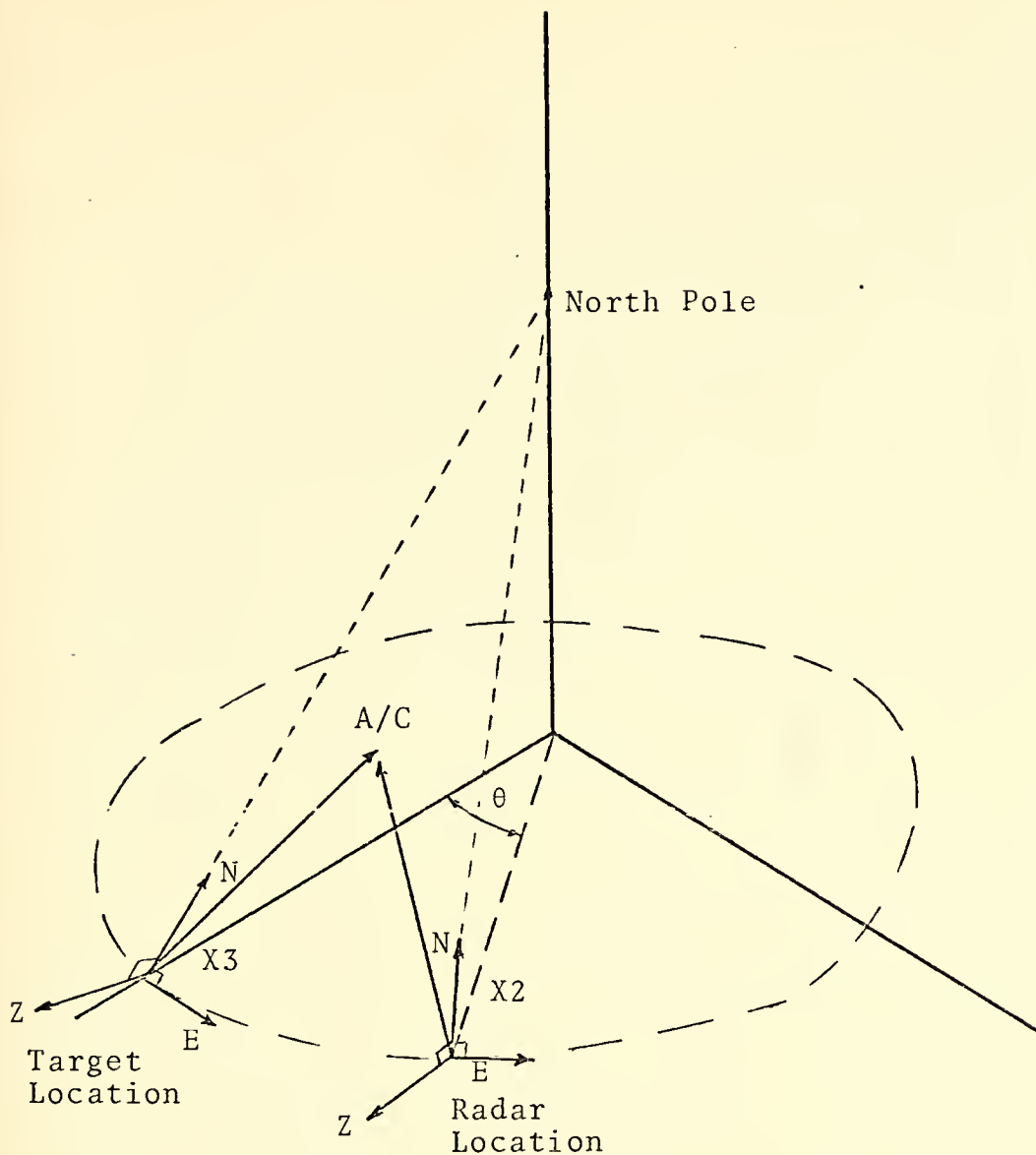
Three primary coordinate systems are used in Precision Guidance calculations. These systems have their origins at the target, the radar, and the aircraft. A convention in notation is used throughout the program to denote vectors in the various coordinate systems.  $X1$  represents a position vector,  $XD1$  represents a velocity vector, and  $XDD1$  represents an acceleration vector. (The only time acceleration vectors appear are in RADAR9.) The number "1" in the notation simply refers to a specific coordinate system.

$X1$  represents the state estimate of the aircraft in the radar reference frame;  $X2$  represents the true state vector of the aircraft in the radar frame.  $X3$  represents the state vector of the aircraft in the target frame. Conversion from one frame to the other is accomplished through the use of transformation matrices  $EM1$ ,  $EM2$ , and  $EV1$ , and the subroutines  $MATMLT$ , and  $MATMAD$  which perform the matrix multiplication and addition. The relationship between  $X2$  (or  $X1$ ) and  $X3$  is illustrated in Fig. 5.

Aircraft control is derived through the use of the  $X6$  coordinate system, which has its origin at the aircraft and its  $y$  axis oriented along the estimated aircraft ground heading. This transformation is accomplished through the coordinate transformation matrix  $EM3$ . Figure 6 illustrates the







The local vertical is labeled Z. Local North is the y axis, and local East is the x axis in each frame. The dashed line is a great circle through the two points. Point labeled A/C is the aircraft.

Figure 5. Illustration of the relationship between the X3 and the X2 coordinate systems.



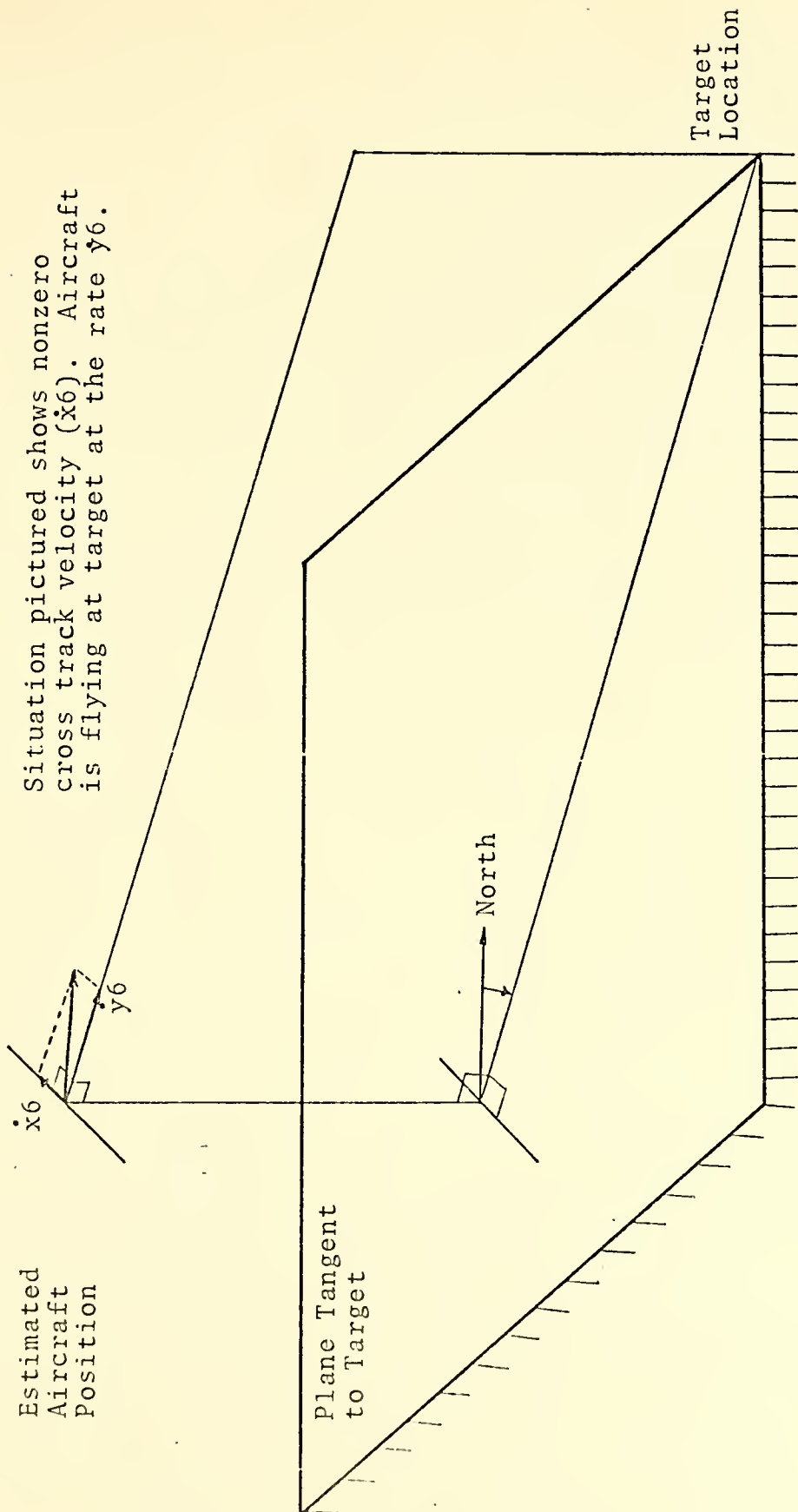


Figure 6. Illustration of relationship between  $X_6$  and the Target.



the relationship between this coordinate system and the target. Note that in the case of perfect estimation and no wind that this y axis orientation would point directly at the target.

Each of the X, XD, and XDD vectors are of dimension 3, one storage allocation for each physical dimension. Thus,

$$X1(1) = x1$$

$$X1(2) = y1$$

$$X1(3) = z1.$$

The coordinate systems and transformation equations are fully specified in [11].

#### D. LOOP GEOMETRY AND ERROR CALCULATIONS

The normal flow of control through the main program loop following the initial 6 second settling period begins with a time update and a movement of the aircraft in accordance with the command bank angle generated at the previous time, all within the original subroutine ARCRFT. The true position is then transformed into the radar frame, noise added, and the new state vector estimated using the RADAR9 subroutine. The estimated state vector is then transformed into the X6,XD6 system, sometimes referred to as the "double primed" reference system in the original program documentation.

As mentioned previously, every 4 seconds the simulation program computes new coefficients which are used to calculate the ballistic range to the target, and bomb time of fall. This involves integration of a system of 16 differential equations using a fourth order Runge-Kutta scheme. The ballistic



range (RA) and time of fall for the bomb (TF) are computed using a first order linearized approximation to the system of equations described above at those times when no integration has been performed. Subroutines STIFF, DER, and OUT are used to perform the required calculations; these are completely specified in [10].

The ballistic range, RA, is the distance the bomb will impact from the present aircraft position. Time of fall, TF, is the time in seconds which will elapse between bomb release and impact. These values and the ballistic wind components in track and cross-track to the aircraft estimated heading determine the impact point for the bomb in X6 reference frame. The equations for this estimated impact point, (XGC,YGC), are as described in [11]. Figure 7 illustrates the geometry of the situation for the windless case. It is assumed that by selecting the bomb release time carefully, a near-zero error in impact on the y6 axis can be achieved. Only by having the aircraft heading precisely correct will the cross track impact error, called lateral error (XE), be zero as well.

At each sampling point, the Time-to-Go-to-Release the bomb, TG, is computed using

$$TG = (y6 - YGC)/\dot{y6} \quad (65)$$

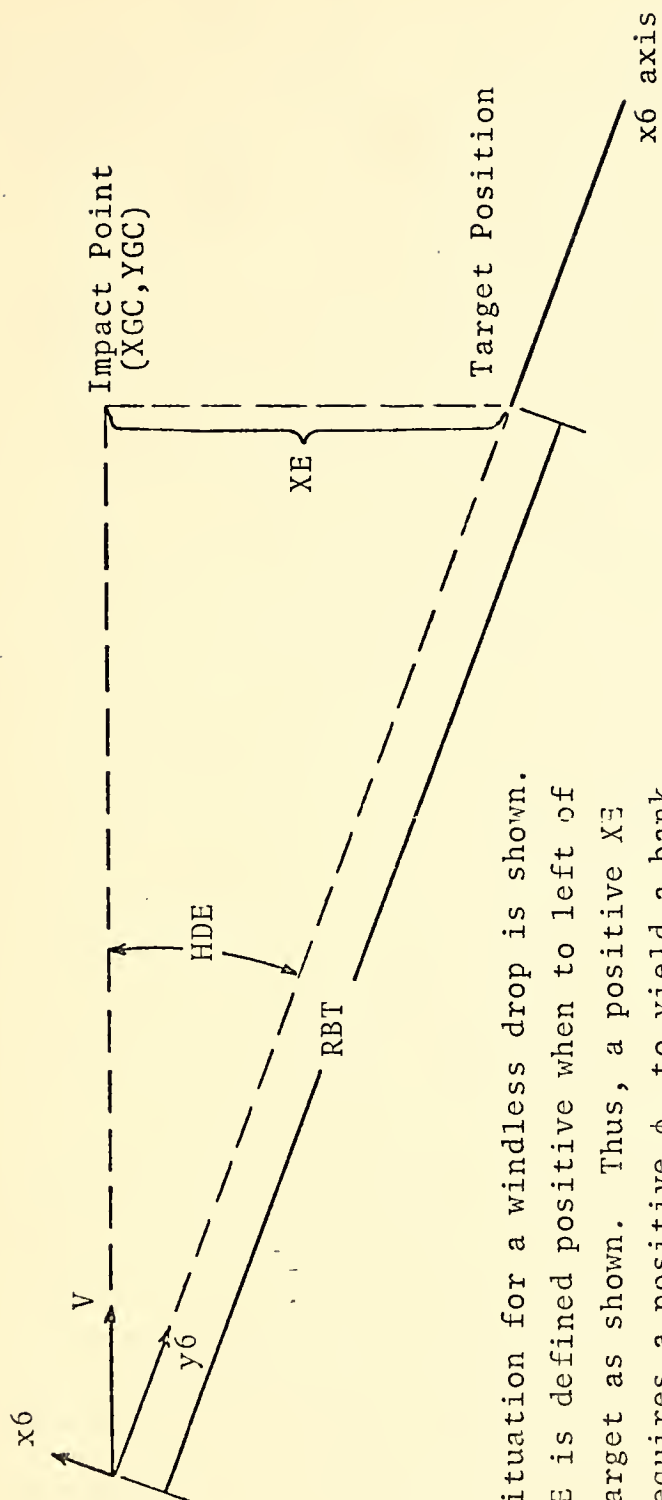
The lateral error is given by

$$XE = x6 - XGC.$$

Other quantities which are used in error calculations are the ballistic range to the target, RBT, and the heading angle error, HDE. These are given by







Situation for a windless drop is shown.  $XE$  is defined positive when to left of target as shown. Thus, a positive  $XE$  requires a positive  $\phi_c$  to yield a bank to the right.

Figure 7. Illustration of error and bombing geometry.



$$RBT = (x5^2 + y5^2)^{\frac{1}{2}} \quad (67)$$

where X5 is the coordinate system X6 prior to being rotated for heading-target alignment, and

$$HDE = \arcsin(XE/RBT). \quad (68)$$

#### E. AIRCRAFT CONTROLLER DESIGN

The new controller for the aircraft is considerably less complex than that originally used. The original version employed lead-lag networks, suitably digitized, with constants which were switched in or out at different stages of the simulation run. The lateral error was driven to zero in the original version of the program, by selection of a gain constant times the lateral error to yield a desired bank angle.

The new controller design attempts to drive both an error and an error rate to zero. The error signals to be driven to zero are the heading angle error, HDE, and the heading angle error rate, HDEDOT, where

$$HDEDOT = \dot{HDE}. \quad (69)$$

The desired control bank angle,  $\phi_d$ , is given by

$$\phi_{d1} = G_1 HDE \quad (70)$$

$$\phi_{d2} = G_2 HDEDOT \quad (71)$$

and 
$$\phi_d = \phi_{d1} + \phi_{d2}. \quad (72)$$

This procedure requires selection of the feedback gain constants  $G_1$  and  $G_2$ . It should be noted at this time that  $G_1$  and  $G_2$  are the only two constants in the simulation program which must be determined "through simulation," i.e., by



trial and error. The original program was filled with numerous "gain constants" which were, or were to have been selected by "simulation." In addition, in the original version, much of the theory was developed through the assumption that the process was approximately a linear one, and development of a linearized model which reflected these linearizations. Such linearization may be somewhat valid in the final stages of a long run where only small commands are being sent, but in the initial phase of heading correction, the commands saturate and the assumption of linearity is invalid. It is in this nonlinear region of operation that commands must be optimized to yield a combination of rapid correction of heading error and minimum overshoot of the correct heading.

Two sets of control gains have been selected for the two prevalent aircraft roll response time constants,  $\tau_b = 2$  and  $\tau_b = 3.3$ . The gain constants are given below.

$$\tau_b = 2 : G_1 = G_2 = 75$$

$$\tau_b = 3.3 : G_1 = G_2 = 150.$$

These parameters were selected through analysis of numerous simulation runs with each  $\tau_b$  and subjectively evaluating the resultant performance. The performance criteria used was to generate initial commands which are of the "bang-bang" type referred to in optimal control theory, causing the bank command to saturate at the autopilot limit of  $\pm 30$  degrees.

This causes the aircraft to begin turning toward the correct heading at the maximum possible rate permitted. The effect



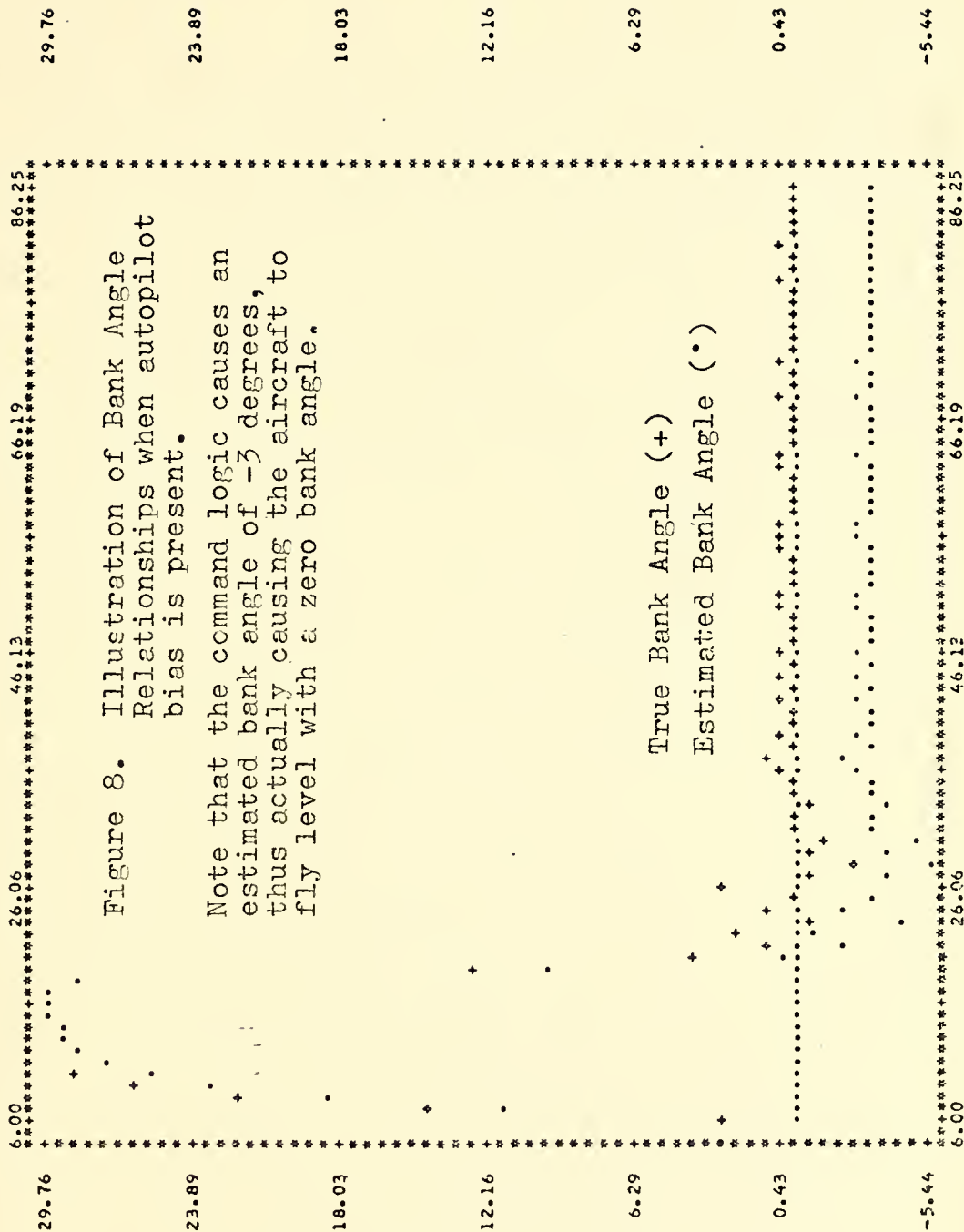
of heading error rate control is to act as a damper in that the faster the heading angle changes, the more the control will begin to decrease. The second part of the performance criteria was to require that when small angle errors are noted, only small commands are generated.

There is a requirement for no bank commands during the final second of flight. This is to ensure that the aircraft does not make a violent maneuver just as the bomb is dropped, causing the bomb to be pitched from the aircraft rather than simply dropped as had been assumed in the bombing calculations.

For a one second period beginning three seconds before bomb release, i.e.,  $TG = 3$  to  $TG = 2$ , the average estimated aircraft bank angle is computed. This average estimated bank angle is then sent as the command during the final two seconds before bomb release. The reason for sending this value vice a command of zero degrees is the possible presence of a bias angle. Figure 8 is a plot of a typical simulation run in which the autopilot has a bias bank angle of 3 degrees. Note that this bias is automatically compensated for by the commands sent. The average command at the end of the run is approximately -3 degrees. This has the effect of rolling the aircraft back to a level flight profile in a steady-state situation, vice a slowly turning profile which would be present if the command was 0 degrees. By averaging the estimated bank angle over the period defined above, and sending this value for the final few seconds, the aircraft continues on an approximately error free path. A zero command









at this time would cause the aircraft to begin a slow turn and greatly increase the lateral error with no opportunity for correction.

Command system requirements require that the command angle be quantized to the nearest  $15/128$  degree. This is accomplished through simple logic as described in [11].

## F. PRECISION GUIDANCE PROGRAM IMPLEMENTATION

### 1. Main Program and Subroutines

The Precision Guidance simulation program consists of a main routine and seven primary subroutines. The program listing is appended at the end of this report. Each of the subroutines is included and in each of the routines the primary variables and purpose of the routine is specified, with the exception of subroutines STIFF, DER, and OUT, which serve only to support the Runge-Kutta integration defined above. The simulation program was written to run on an IBM 360-67 computer system and takes advantage of several of the system software subroutines. The program with linkage and subroutines requires approximately 150 K to execute and will run a typical time of from one to three minutes of CPU time. Compilation requires approximately 50 seconds.

A listing of the variables used in the program along with the variable definitions is provided in Appendix A.

### 2. Program Input and Output

Specific format definitions for program input data are provided in Appendix B. The program output has been



changed significantly from that in the original program version. A sample of one complete simulation run is provided at the end of this report. The initial conditions and constants are output along with short word definitions of their meaning or useage. Each second, a summary of the critical parameters of the program are output in block form; the output key is printed on each page for ready availability to the user. During the final second before bomb release, the critical parameters summary is printed at every sampling point.

On the final time through the main processing loop, all estimates are replaced by their corresponding true values, and the bomb "released." The impact point is computed, and the miss distances in x,y and overall are printed, designated XI, YI, and RI, respectively.

As a measure of filter effectiveness in noise reduction and state prediction in position including deterministic motion, the square of filter residual is summed throughout the run. The RMS values of filter residue are printed following the bomb impact miss distances. Filter residue in this sense is defined as

$$\text{FILRES}_x = x1 - x2 \quad (73a)$$

$$\text{FILRES}_y = y1 - y2 \quad (73b)$$

$$\text{FILRES}_z = z1 - z2. \quad (73c)$$

In addition to the filter residual in each coordinate, a radial residual defined as



$$\text{FILRES}_R = (\text{FILRES}_x^2 + \text{FILRES}_y^2 + \text{FILRES}_z^2)^{\frac{1}{2}} \quad (74)$$

is printed in RMS form, where the average is over the entire simulation run.

Some of the critical parameters are stored in arrays each second throughout the run. These are then line printer plotted at the completion of the run with appropriate labelling.





#### IV. COARSE GUIDANCE SIMULATION

##### A. INTRODUCTION

Two documents, [8] and [9], were provided to describe the techniques and general approach being followed on the original Coarse Guidance simulation program. However, no program documentation such as that provided for Precision Guidance, [11], was available. The program provided seemed inordinately complex in some places and the general approach to the problem did not appear to be a viable one from which to build an improved version.

It was determined that the best approach would be to write a totally new main simulation driving routine, use the already existing aircraft simulation program, ARCRFT, and the already developed Kalman filter radar simulation program RADAR6 to simulate the Coarse Guidance tracking system. RADAR6 was chosen vice RADAR9 simply because neither [8] nor [9] mentioned any difficulty with bank angle biasing. Also, the smaller size and faster running time of RADAR6 made that subroutine a preferred choice. The decision to mate RADAR6 to Coarse Guidance rather than RADAR9 is by no means a final choice. A matter of only a few minutes would be required to modify RADAR9 to be compatible with the Coarse Guidance simulation program. Thus if biasing is a problem in this mode also, RADAR9 could serve as the appropriate unbiased state estimator. The changes in RADAR6 from RADAR9 other than those which relate to acceleration estimation will be discussed



below. A few simplifying changes in the ARCRFT subroutine were also accomplished to reduce core storage requirements and execution time; these will also be described.

Some of the concepts and a few equations from the original documents on Coarse Guidance were used in this study. Since the new simulation program differs significantly from the original version, nearly all equations will be presented and most will be derived.

The basic concept in Coarse Guidance is to get the aircraft from some initial starting point to the final bombing run by flying a predetermined course which is specified by "waypoints" and azimuths of course "legs." A typical simulation setup might appear as illustrated in Fig. 9. The designated legs presumably follow a "safe" path for the strike aircraft. Also, presumably, if the aircraft deviate from the specified path too far, they become in danger. Therefore, it is desirable to provide some control to keep the aircraft as near to the specified path as possible. Of particular importance is to recognize the approach of the beginning of a new leg and begin a "command turn" onto this new leg at such a time that upon completion of the turn, the aircraft will be on the new leg with the same ground heading as the leg's azimuth.

#### B. PRE-MISSION DATA TABLE COMPUTATIONS AND INITIAL CONDITIONS

Once the path to be flown is specified, the individual legs can be characterized by their azimuth with respect to North and their length. The beginning of the mission is



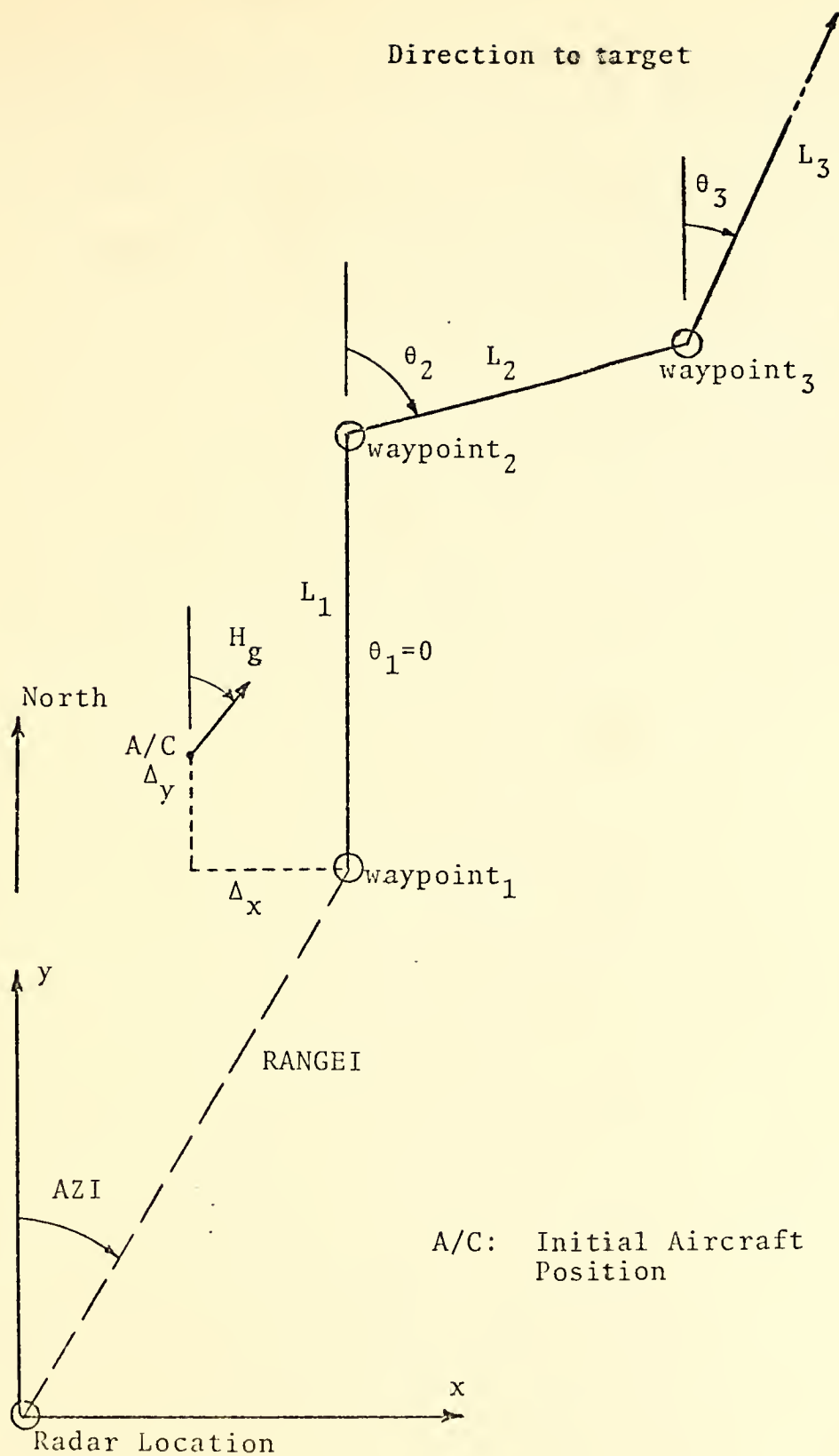


Figure 9. Illustration of a typical 3 leg course.



referred to as a TACAN Entry Point, and is the approximate position of aircraft entry into the problem. Wind causes the ground heading and the air heading to differ. Since most of the aircraft control calculations are made with respect to the air heading, effects of wind must be considered. The initial position of the aircraft is placed at the beginning of the first leg perturbed by some error, and with ground heading of the first leg's azimuth also perturbed by some angle deviation from desired.

### 1. True and Estimated Wind Components

Figure 10 illustrates the relationship assumed for wind in the problem. Provision is made for an error in estimated wind speed and direction. All true aircraft motion is computed using true wind. All estimated aircraft motion and control decisions are made using the estimated wind components. Wind is assumed zero in the vertical direction. If the true (estimated) direction toward which the wind is blowing is  $\theta_w$  ( $\theta_{wh}$ ), and the true (estimated) wind speed is  $V_w$  ( $V_{wh}$ ) then the components of wind are given by

$$w_x = V_w \sin(\theta_w) \quad (75a)$$

$$w_y = V_w \cos(\theta_w) \quad (75b)$$

for the true wind, and

$$w_{xh} = V_{wh} \sin(\theta_{wh}) \quad (76a)$$

$$w_{yh} = V_{wh} \cos(\theta_{wh}) \quad (76b)$$

for the estimated wind.





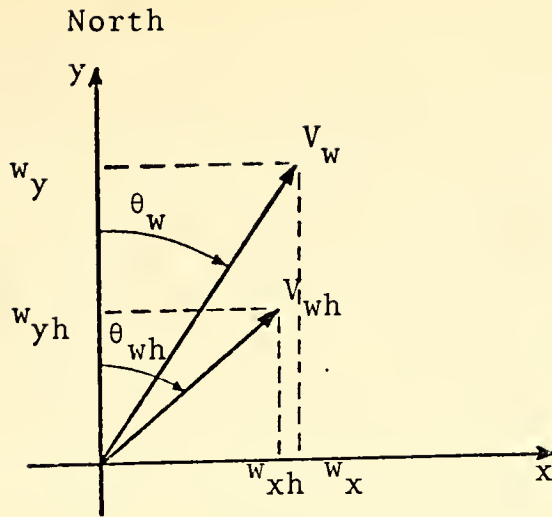


Figure 10. Illustration of Wind Relationships.

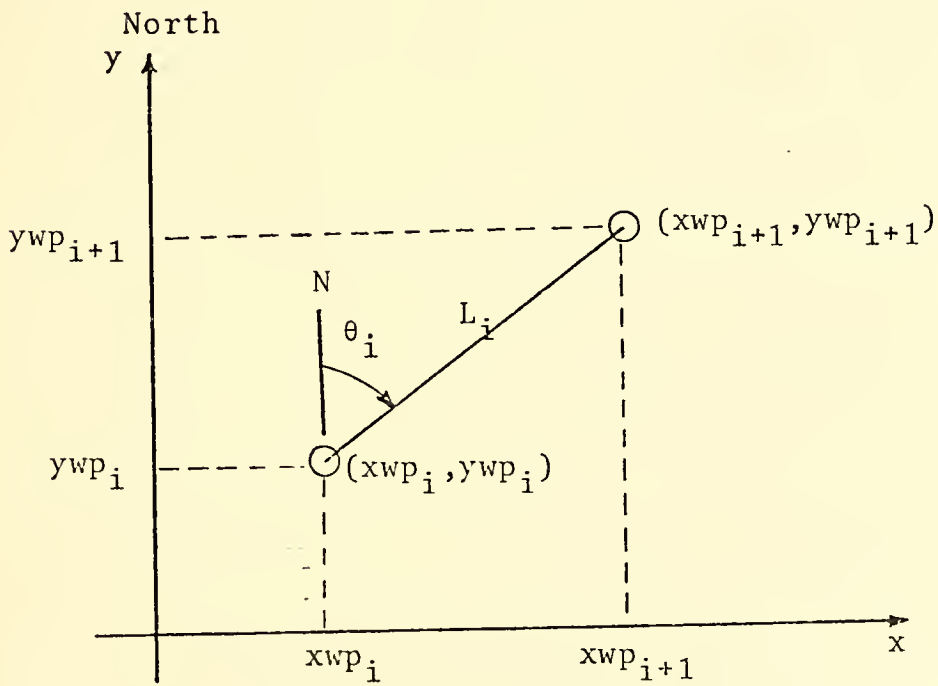


Figure 11. Illustration of Waypoint Coordinate Calculations.



## 2. Mission Data Table Calculations

Included in the mission data table are the waypoint coordinates, average radar range to each leg, average radar azimuth to a given leg, desired air heading while on each leg, desired ground speed while on each leg, approximate time to fly each leg, and the ground velocity components for each leg.

For notational purposes, it is assumed that there are a total of  $n$  legs to be flown; a subscript  $i$  on any parameter indicates that parameter for the  $i^{\text{th}}$  leg. Figure 11 illustrates calculation of the  $i+1$  waypoint coordinates from the previous leg's parameters. If  $(x_{wp_i}, y_{wp_i})$  are the coordinates of the  $i^{\text{th}}$  waypoint, the azimuth of the  $i^{\text{th}}$  leg is  $\theta_i$ , and the length of the  $i^{\text{th}}$  leg is  $L_i$ , then

$$x_{wp_{i+1}} = x_{wp_i} + L_i \sin(\theta_i) \quad (77a)$$

$$y_{wp_{i+1}} = y_{wp_i} + L_i \cos(\theta_i). \quad (77b)$$

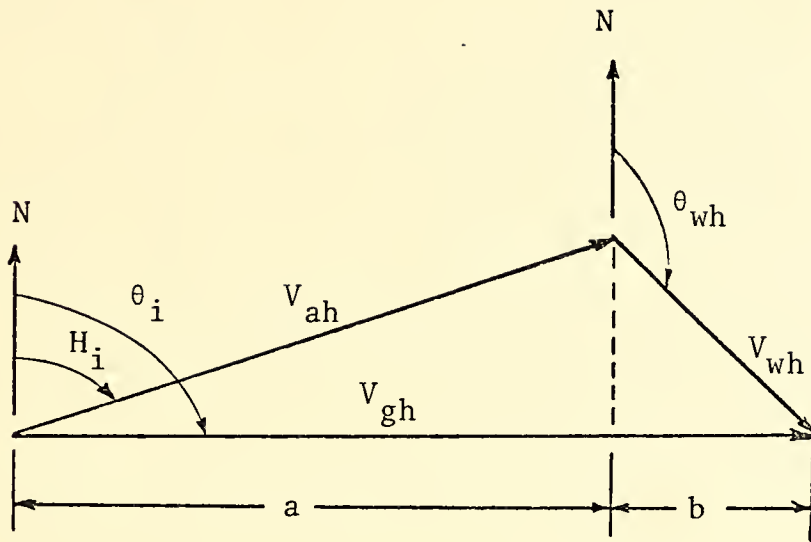
The average range and azimuth to the  $i^{\text{th}}$  leg,  $R_i$  and  $Az_i$  are given by

$$R_i = \frac{1}{2}[(x_{wp_i} + x_{wp_{i+1}})^2 + (y_{wp_i} + y_{wp_{i+1}})^2]^{\frac{1}{2}} \quad (78)$$

$$Az_i = \arctan \left[ \frac{x_{wp_i} + x_{wp_{i+1}}}{y_{wp_i} + y_{wp_{i+1}}} \right]. \quad (79)$$

Figure 12 presents geometry which aids in clarifying calculation of the air heading and ground speed, assuming the air speed is a known constant. (This assumption is maintained through the problem and seems reasonable, since





$$a = V_{ah} \cos(H_i - \theta_i)$$

$$b = V_{wh} \cos(\theta_{wh} - \theta_i)$$

Figure 12. Illustration of Ground Speed and Air Heading Calculation Geometry.



the pilot has a direct readout of his speed with respect to the air.) Since it is desired to fly along the leg, it is correct to sum components perpendicular to the leg and set these to zero. If  $V_{ah}$  is the estimated air speed and  $H_i$  is the air heading then

$$V_{ah} \sin(H_i - \theta_i) + V_{wh} \sin(\theta_{wh} - \theta_i) = 0. \quad (80)$$

Summing components in the direction of the leg yields the desired ground speed

$$V_{gh} = V_{ah} \cos(H_i - \theta_i) + V_{wh} \cos(\theta_{wh} - \theta_i) \quad (81)$$

$V_{gh}$  can be broken into Cartesian components,  $V_{gx}$  and  $V_{gy}$  as follows:

$$V_{gx} = V_{gh} \sin(\theta_i) \quad (82a)$$

$$V_{gy} = V_{gh} \cos(\theta_i). \quad (82b)$$

The air heading required to fly in the direction  $\theta_i$  is found by solving (80) for  $H_i$ .

$$H_i = \theta_i - \arcsin \left[ \frac{V_{wh}}{V_a} \sin(\theta_{wh} - \theta_i) \right]. \quad (83)$$

### 3. Initial Position and Velocity of the Aircraft

The initial true position of the aircraft is that of the first waypoint plus a perturbative error. Since the waypoint is on the ground, the altitude of the aircraft is given by the perturbation in the  $z$  coordinate. The true position of the aircraft is contained in the  $X$  array.

$$x3 = xwp_1 + \Delta_x \quad (84a)$$

$$y3 = ywp_1 + \Delta_y \quad (84b)$$

$$z3 = \Delta_z. \quad (84c)$$





The initial true ground heading,  $H_g$ , is read as data. This in addition to the known airspeed,  $V_a$ , specifies the true ground speed,  $V_g$ , and the true air heading,  $H_a$ , through a set of equations similar to (80), (81), and (83). The results are given by

$$H_a = H_g - \arcsin \left[ \frac{V_w}{V_a} \sin(\theta_w - H_g) \right] \quad (85)$$

and by

$$V_g = V_a \cos(H_a - H_g) + V_w \cos(\theta_w - H_g). \quad (86)$$

The initial true velocity of the aircraft is then broken into Cartesian coordinates and stored in the XD3 array.

$$\dot{x}_3 = V_g \sin(H_g) \quad (87a)$$

$$\dot{y}_3 = V_g \cos(H_g) \quad (87b)$$

$$\dot{z}_3 = 0. \quad (87c)$$

Note that it is through specification of  $H_g$  different from  $\theta_1$ , and  $\Delta_x$  and  $\Delta_y$  different from 0 that nonzero perturbations in velocity and position from the desired values are entered. Figure 9 also shows the geometry which might exist in the case of nonzero displacement and velocity from the desired track.

### C. AIRCRAFT POSITION, VELOCITY, AND ERROR ESTIMATION

As previously stated, aircraft motion is simulated by the use of a slightly modified version of subroutine ARCRFT associated with Precision Guidance. Position and velocity estimation is accomplished using RADAR6. At the beginning of



the main processing loop, true aircraft position is updated followed immediately by a prediction update on estimated aircraft position. A new estimation update is performed only if the total radar sampling interval DTRAD has elapsed. (It is assumed that prediction updates occur at a higher rate than radar sampling.) The most current aircraft position and velocity estimates are contained in the X1 and XD1 arrays. From this and the estimated wind components, the estimated air and ground headings, and estimated ground speed are computed;  $H_{ah}$ ,  $H_{gh}$ , and  $V_{gh}$ , respectively.

$$H_{gh} = \arctan \left[ \frac{\dot{x}_1}{\dot{y}_1} \right] \quad (88)$$

$$H_{ah} = \arctan \left[ \frac{\dot{x}_1 - w_{xh}}{\dot{y}_1 - w_{yh}} \right] \quad (89)$$

$$V_{gh} = (\dot{x}_1^2 + \dot{y}_1^2)^{\frac{1}{2}}. \quad (90)$$

These parameters can be monitored to determine the degree of error in heading and speed from the desired values. An additional and important parameter to be monitored is the extent to which the aircraft has deviated from the desired course,  $E_{est}$ . Figure 13 illustrates the geometry used in this calculation. The error is given by

$$E_{est} = (x_1 - x_{wp_i}) \cos(\theta_i) - (y_1 - y_{wp_i}) \sin(\theta_i). \quad (91)$$

Note that (91) computes the distance from the present position estimate to the leg  $i$ . In a command turn, the aircraft should not be on either leg, but will be somewhere between



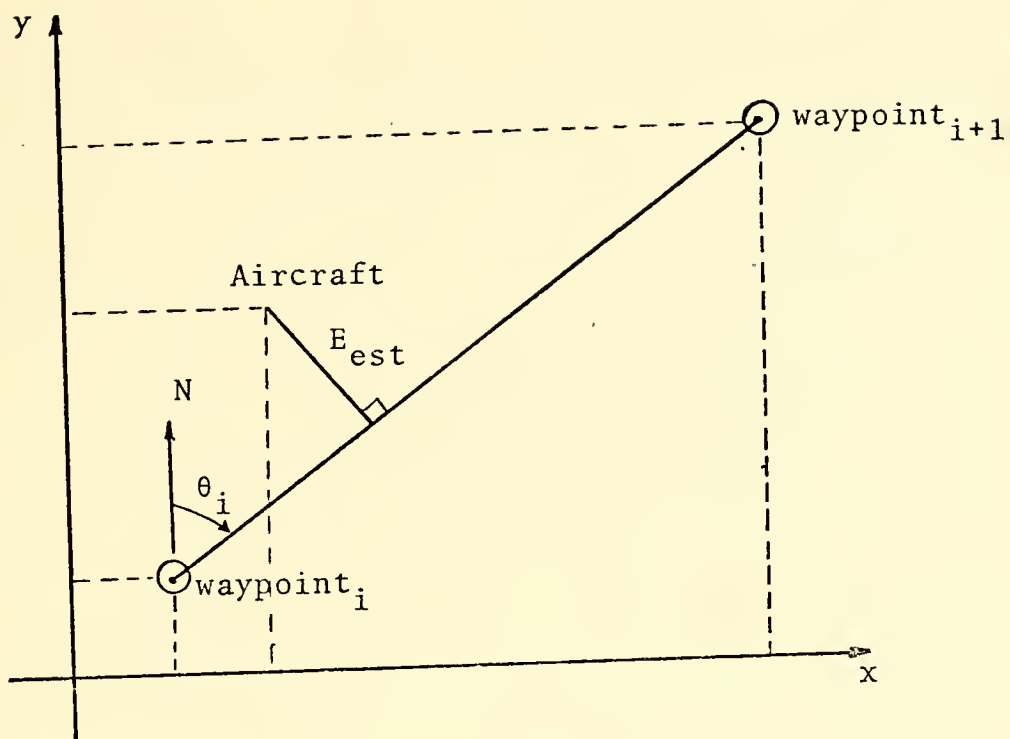


Figure 13. Illustration of Geometry for Calculating Deviation from the Desired Leg Path.



the legs. For this reason, distance from both the  $i^{\text{th}}$  and  $i+1$  leg is computed, and the smaller of the two values chosen.

True headings, speeds, and distances corresponding to those given above are also computed using the same equations with  $X3$  substituted for  $X1$ , and  $W$  substituted for  $W_h$ .

#### D. COMMAND TURN CALCULATIONS

The command turn is that which is computed to cause a smooth transition of the aircraft from the present leg to the next leg with a minimum overshoot or undershoot of the desired path. The aircraft autopilot is constrained to a maximum bank angle,  $\phi_m$ , typically equal to 30 degrees. Since the heading angle rate is proportional to the bank angle in a coordinated turn, the time to complete the turn using the maximum possible bank must be precalculated so that the turn can be started prior to reaching the new leg. This process is complicated by three factors. The first is that the time to the next leg is variable with the current position and velocity. Thus the time to begin the turn as well as the amount of heading change required is a function of the state estimate. The second factor is that the equation to be solving for the amount of time required for the turn is a transcendental equation and must be solved through iteration. The third factor is that this equation becomes unduly complex if the turn is not started from a zero bank angle. This requires that the aircraft begin the turn in level flight.





### 1. Time Remaining on Present Leg

The time remaining on the present leg before intersecting with either the next leg or its extension is computed by finding the intersection of the two paths, calculating the distance to be traversed, and then dividing by the estimated ground speed. The geometry is illustrated in Fig. 14.

The coordinates of intersection of the present path, based on the present velocity estimate and the next leg are designated  $(x_{int}, y_{int})$ . Let  $m_i$  and  $m_{i+1}$  represent the slopes of the present aircraft heading and the next leg, respectively.

Then

$$m_i = \dot{y}_1 / \dot{x}_1 \quad (92)$$

$$m_{i+1} = (y_{wp_{i+1}} - y_{wp_i}) / (x_{wp_{i+1}} - x_{wp_i}). \quad (93)$$

The equations of the two lines whose intersection is to be found are

$$y = m_{i+1} x - (m_{i+1} x_{wp_{i+1}} - y_{wp_{i+1}}) \quad (94)$$

$$y = m_i x - (m_i x_1 - y_1). \quad (95)$$

These equations are solved simultaneously to give the point of intersection.

$$x_{int} = \frac{(y_1 - y_{wp_{i+1}}) + (m_{i+1} x_{wp_{i+1}} - m_i x_1)}{(m_{i+1} - m_i)} \quad (96)$$

$$y_{int} = m_i x_{int} - m_i x_1 + y_1. \quad (97)$$

The distance between  $x_1$  and the point of intersection is then

$$D_{tg} = [(x_{int} - x_1)^2 + (y_{int} - y_1)^2]^{1/2} \quad (98)$$



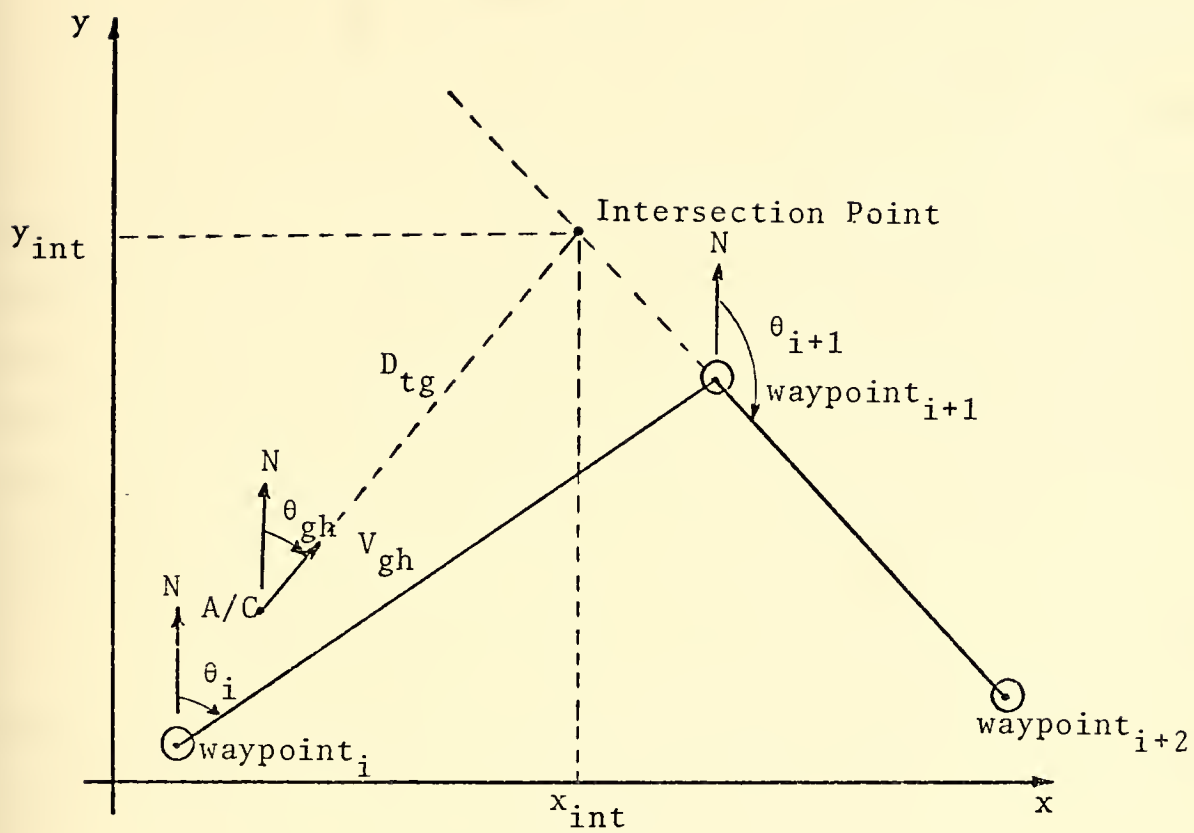


Figure 14. Illustration of Path-Leg Intersection Geometry.



and the time to reach this point is given by

$$TLEG1 = D_{tg}/V_{gh}. \quad (99)$$

## 2. Time Required to Complete the Turn

The amount of turn required,  $\Delta H$ , is simply

$$\Delta H = |H_{i+1} - H_{ah}|. \quad (100)$$

Air headings are used in the calculations since all aircraft motion and turn equations must account for the possible presence of wind. Equation (50) gives the relationship between the change in heading angle, time in the turn, and the roll response of the aircraft. Setting  $\Delta\psi$  equal to  $\Delta H$  and  $\phi_c$  equal to  $\phi_m$  gives

$$\Delta H = (g/V_{ah}) \left[ \phi_m T + (\phi(k-1) - \phi_m)(\tau_b)(1 - e^{-T/\tau_b}) \right]. \quad (101)$$

If it is assumed that  $\phi(k-1)$  is zero (starting with level flight), then the equation can be rewritten as

$$K = U - (1 - e^{-U}) \quad (102)$$

where

$$U = T/\tau_b \quad (103)$$

and

$$K = \frac{\Delta H V_{ah}}{g \tau_b \phi_m}. \quad (104)$$

For the purpose of finding the turn time required, assume that the turn can be divided into three parts as illustrated in Fig. 15. The first part is the transient period during which the aircraft is coming to the maximum (or minimum) bank angle, going to that limit exponentially with time constant



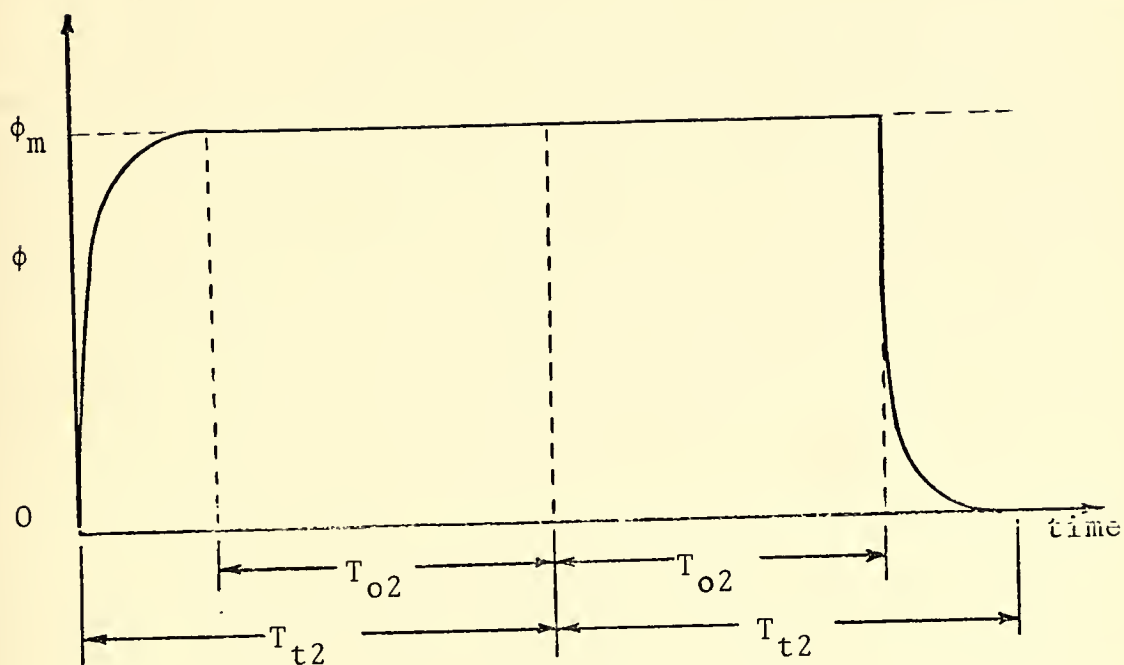


Figure 15. Illustration of Relationships Between Times and Bank Angles in a Command Turn.





$\tau_b$ . The second part of the turn is that segment when the aircraft is holding at the bank limit and changing direction with an approximately constant heading rate. The third and final part of the turn is a transient segment during which the aircraft returns to a zero bank angle, also exponentially.

Figure 15 shows that the turn can be divided into two approximately equal parts, during which the aircraft executes approximately half of the turn,  $\Delta H/2$ . Let the time required to complete half of the turn be  $T_{t2}$ , and the time to complete half of the constant bank segment of the turn be  $T_{02}$ . If  $K$ , above, is replaced by  $K/2$ , then the solution to (102) yields

$$U = T_{t2}/\tau_b. \quad (105)$$

The equation is solved using the Newton-Raphson iterative technique. The initial approximation to  $T_{t2}$  is taken from [9]. Iteration continues until the change in  $T_{t2}$  is less than 0.01.

Motion of the aircraft through the turn is approximated in nearly the same manner as described in [9]. Briefly, it is assumed that the aircraft continues on an approximately a straight path for a period  $T_{t2} - T_{02}$  seconds after the command turn is ordered, followed by the command turn as described above, followed by another period of approximately straight flight along the new leg during the final seconds of the turn. A diagram of the geometry of the turn is presented in Fig. 16. Since the turn has been computed with respect to the motion of the air mass, movement of the air mass during the turn is



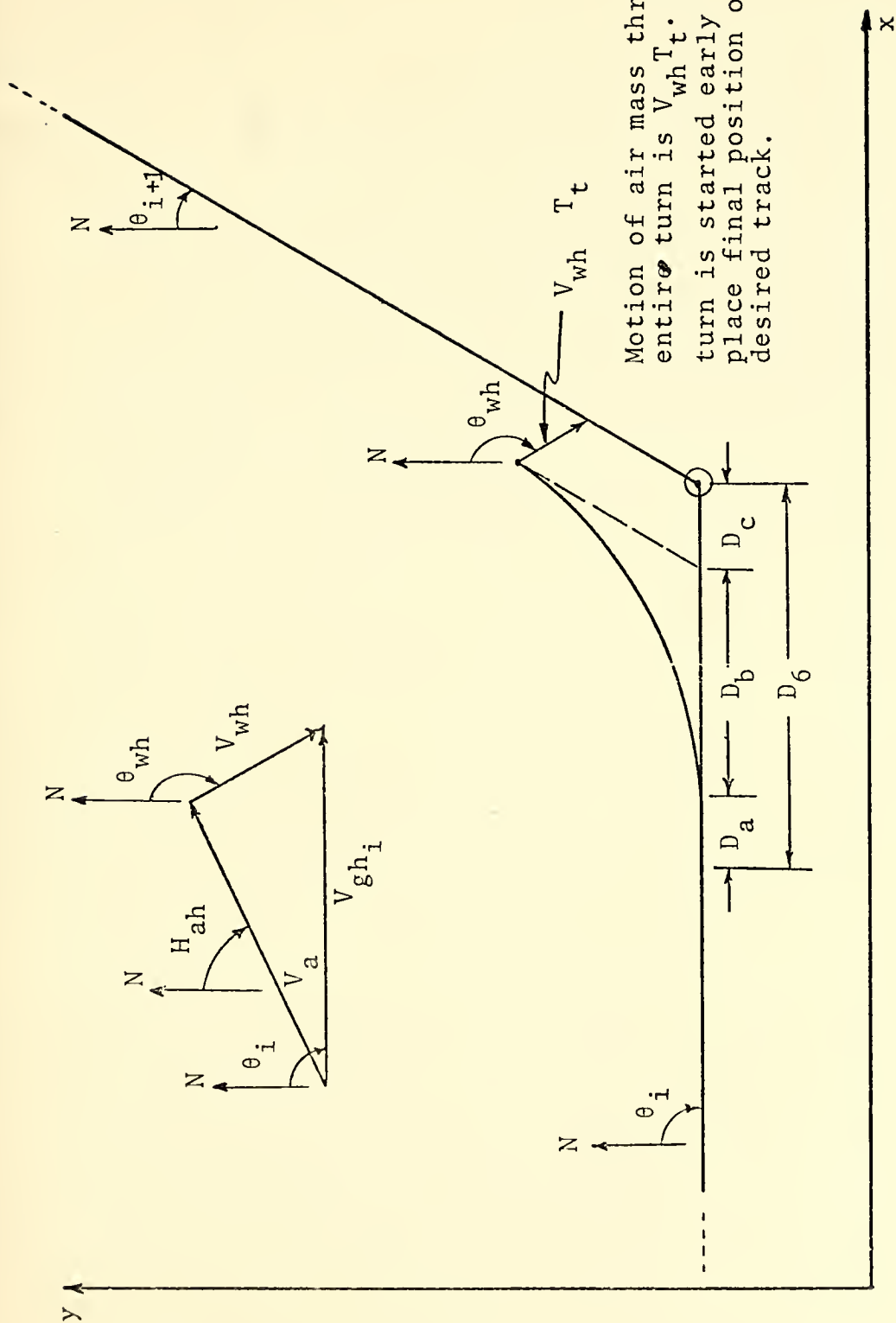


Figure 16. Illustration of Turn Geometry, Including Effects of Wind Shifting the Final Aircraft Position.



compensated for. The only modified equation used to calculate the distance prior to leg intersection from which the turn must start is that which relates to air mass motion. The new equation for computation of the parameter  $D_c$  is given correctly by

$$D_c = T_{o2} V_{wh} \sin(\theta_{i+1} - \theta_{wh}) \sin(\theta_{i+1} - \theta_i). \quad (106)$$

The turn must be started a distance  $D_6$  before the intersection with the next leg, where  $D_6$  is shown on the illustration and mathematically defined adequately in [9].

### 3. Command Turn Timing Logic

The time-to-go before beginning a command turn is given by

$$TG = T_{LEG1} - D_6/V_{gl1}. \quad (107)$$

When TG is less than or equal to zero, the aircraft is commanded to go to the maximum bank angle, with the sign of the bank chosen appropriately. The time to command the bank angle back to zero is  $T_{stoptn}$  and is given by

$$T_{stoptn} = T_t - 2\tau_b. \quad (108)$$

Initially it might appear that  $3\tau_b$  should be subtracted from the total turn time, since that would be closer to the amount of time required to decrease the full bank angle when the change is occurring exponentially. However, this value was arrived at through simulation trials, and is probably best due to the compounded approximations made in the overall turn solution. The time at which the turn is complete is defined as  $T_t$ ; no actions depend on this time.



Figure 17 is a logic flow chart of the start/stop turning process. Briefly, a counter in the form of the variable TINTRN is incremented each time through the loop as the turn progresses. The variable ITURN is used as a flag to pass logical control to the correct coding. When no turn is in execution, ITURN = -1, and the only turning which is performed is that to correct the course deviations. No control banking for the above purpose is permitted within the  $3\tau_b$  seconds prior to executing a command turn. This is to ensure that the bank angle of the aircraft is zero when beginning the command turn, an assumption which was used in the derivation of the command turn equations. During the command turn, ITURN = 0, and all control logic is bypassed. Immediately upon executing the logic which indicates the turn is ending, ITURN = 1, and calculations to check for the next turn time begin. If required, a new command turn can be executed immediately, before the aircraft has come down from its bank from the previous turn. This feature was added to ensure that if a short leg or a very acute turn was encountered, the best possible flight trajectory would be flown. Examples of the requirement for this feature and its performance are included.

#### E. AIRCRAFT CONTROLLER DESIGN

The controller, used to guide the aircraft to a desired velocity and keep it there until a command turn, is of the same type used in Precision Guidance. In this case, the controller attempts to keep the estimated ground heading,  $H_{gh}$ ,





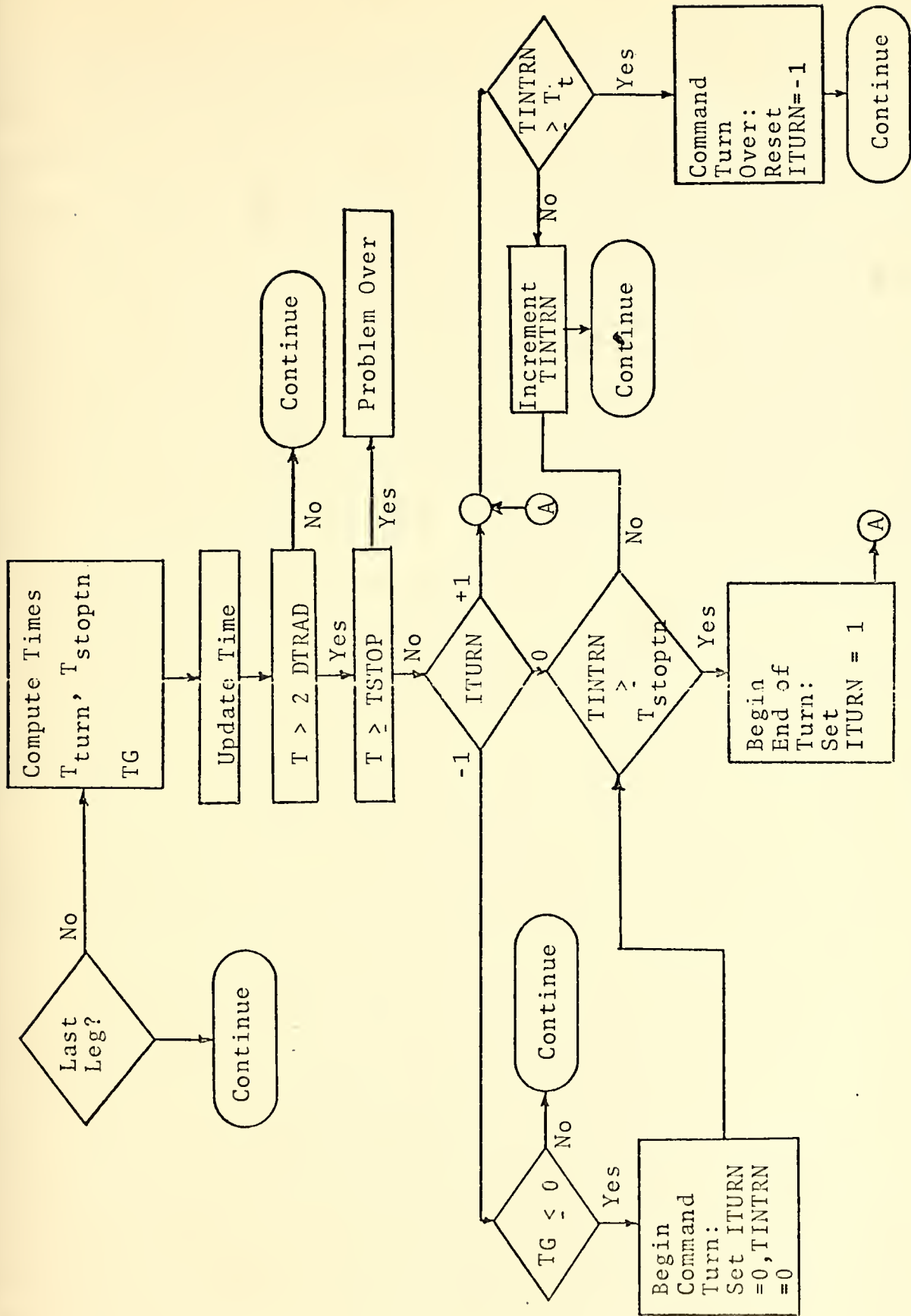


Figure 17. Command Turn Start and Stop Logic.



at that heading from the current estimated position which will fly the aircraft directly at the next waypoint. This scheme was selected for two primary reasons. The first is that it requires minimal control to get the heading correct and thus requires considerably less updating than the technique used in the original simulation program. The second reason is that this technique tends to avoid the problem of oscillation which plagued the original scheme. The controller features a technique which will block any command updates to the aircraft unless the heading error exceeds some minimum error angle,  $H_{ermin}$ .

The estimated heading to the next waypoint is

$$H_{hgwpt} = \arctan \left[ \frac{x_{wp_{i+1}} - x_1}{y_{wp_{i+1}} - y_1} \right] . \quad (109)$$

The heading error is then

$$HDE = H_{hgwpt} - H_{hg} \quad (110)$$

and the heading error rate,  $HDEDOT$  is the discrete derivative of (110). These are combined as given in (70), (71), and (72) to give the desired control angle. The gains  $G_1$  and  $G_2$  were selected equal, as before, with the value 4. Different feedback gains were used in a number of simulation runs, and the results indicated that the system was somewhat insensitive to the values chosen. The gains yielded desired commands of about 20 degrees during normal course corrections, and with the  $H_{ermin}$  feature seemed to avoid the undesired oscillation for the most part.



The commands are quantized before being sent, as in Precision Guidance.

## F. COARSE GUIDANCE PROGRAM IMPLEMENTATION

### 1. Main Program and Subroutines

The Coarse Guidance simulation program consists of a main routine and two primary subroutines. The subroutine ARCRFT used to simulate true aircraft motion, was simplified from that version used in Precision Guidance in that all dive bombing equations were removed. The RADAR6 subroutine differs from RADAR9 by the obvious fact that it does not estimate acceleration due to bank angle bias, as well as in two other ways. The first is that RADAR6 is designed to operate at a sampling interval greater than the control interval. This requires that the subroutine be called, standard prediction equations executed, and then estimation only if the sampling interval has elapsed. The second difference is in the use of NWLD. NWLD indicates that "wild points" are in effect, and are ignored by the radar filter. This amounts to simple prediction without the benefit of radar sampled data.

The Coarse Guidance radar receives little if any return from the aircraft during command turns. In an effort to simulate this effect, NWLD is set to a negative value during turns, thus requiring prediction of position and velocity based only on past data and commands.

Coarse Guidance requires a little less than 100 K of core for linkage and execution. Compilation of the program



and subroutines requires about 25 seconds, and execution requires between 5 and 25 seconds, depending on the number of legs and the leg lengths.

A listing of the variables used in the program along with the variable definitions is provided at the end of Appendix A.

## 2. Program Input and Output

Specific format definitions for program input data are provided in Appendix C.

The program output consists of three primary parts. The first part is a listing of all input data and simulation run parameters. The second part is a summary of critical parameters printed once per second, and the third part is a summary of the deviation error from the desired path, along with a plot showing the desired, true and estimated paths.

At the beginning of each new leg, a summary of data table information is provided about that leg which can then be compared to what actually occurs. As the run progresses, a notification of the three stages of command turning is presented interspersed with the critical parameter summary.

The only performance criteria selected is the root mean square aircraft deviation from the desired path. The plot of the paths shows the deviations very well. The plot scaling is accomplished to maintain the same scale on both axes for a truer visual indication of relative error. All output values are in nautical miles and feet per second, for position and velocity, respectively.





## V. PRESENTATION OF RESULTS

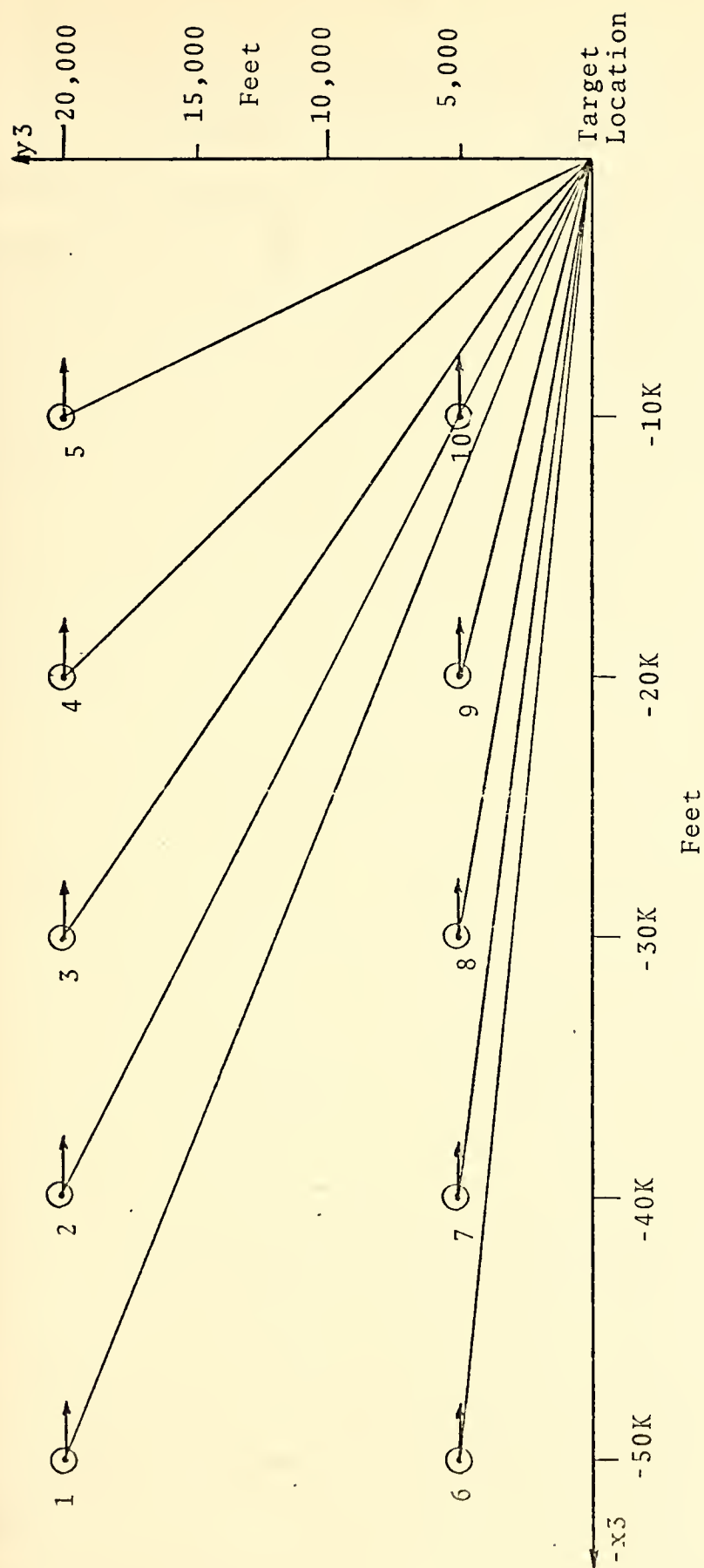
### A. PRECISION GUIDANCE PERFORMANCE COMPARISON

In the process of improving, changing, and verifying performance of the new version of the Precision Guidance simulation program, a very large number of runs were accomplished. A proper comparison between the two program versions requires side-by-side contrast of appropriate performance parameters, each derived from the same set of initial conditions.

In establishing specific run parameters for the initial conditions, three parameter sets were varied: initial aircraft position,  $X_3$ , autopilot bias angle,  $\phi_b$ , and aircraft roll response time constant,  $\tau_b$ . All other variables in the programs were held constant and equal in the two program versions. Variation of the above parameters seemed to yield conditions which would ably show those areas where performance was improved, and at the same time permit runs with initial conditions varying from nearly perfect to considerably in error from the optimal initial bombing path.

Ten different aircraft initial positions were chosen and assigned a "run number." The initial velocity on each of these was identical. The resultant geometry created is shown in Fig. 18. Note that runs 1 through 5 present a considerably more difficult mission than runs 6 through 10. "Difficulty" can be roughly equated to the angle through which the aircraft must change its velocity in order to fly toward the target, located at the origin of the  $X_3$  coordinate system.





Initial velocities in each case were the same at 500 ft/sec in the x direction. Note that runs 1 through 5 represent rather extreme initial conditions, and that runs 6 through 10 are more realistic.

Figure 18. Illustration of Initial Position and Velocity Relationships for Runs Included as Results.



## 1. Filter Performance Comparison

The filters were tested within the framework of the Precision Guidance program. The most important performance parameter to monitor for this problem is the difference between the estimated position of the aircraft and the true position of the aircraft, already defined as the "residual" in II and III. Table I presents a comparison between the Kalman filter and the alpha-beta filter's radial residual, i.e., total estimation error in position, and Fig. 19 presents these results graphically. The numbers shown are average radial residuals, averaged over the runs accomplished for each version.

| <u>AVERAGE RADIAL RESIDUAL (ft)</u> |                       |                         |                         |
|-------------------------------------|-----------------------|-------------------------|-------------------------|
| <u>Run No.</u>                      | <u>Initial<br/>x3</u> | <u>Original Version</u> | <u>Improved Version</u> |
| 1.                                  | -50,000               | 79                      | 15                      |
| 2.                                  | -40,000               | 107                     | 17                      |
| 3.                                  | -30,000               | 154                     | 20                      |
| 4.                                  | -20,000               | 216                     | 21                      |
| 5.                                  | -10,000               | 128                     | 27                      |

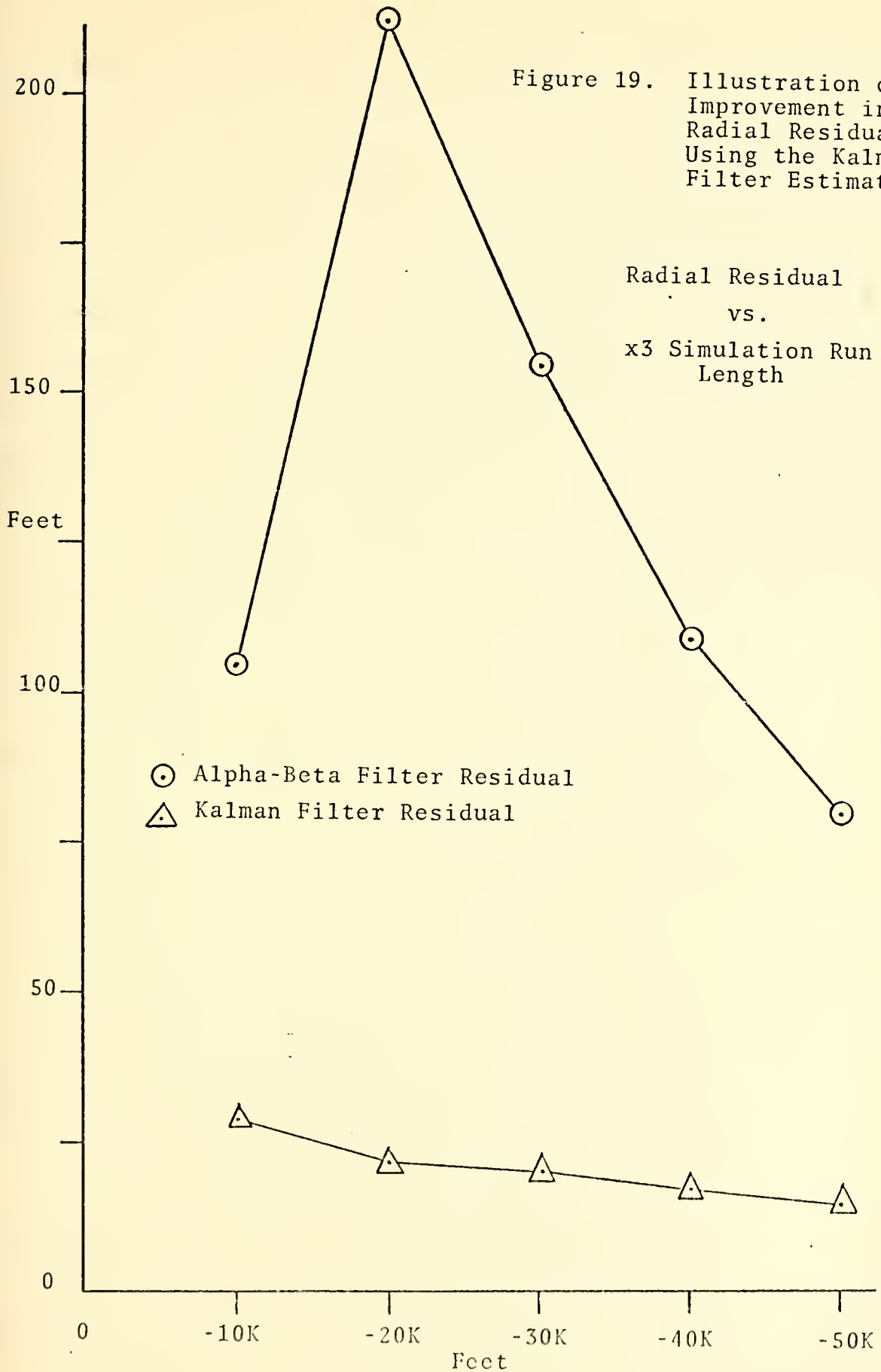
Table I. Comparison of Average Radial Residuals for the Alpha-Beta and Kalman Filters.

---

The figures show an average percent improvement for the new program version of 680 percent, with a maximum improvement of over 1000 percent. It should be noted at this point that these numbers do not represent the results of a



Figure 19. Illustration of Improvement in Radial Residual Using the Kalman Filter Estimator.







true Monte Carlo simulation. To achieve Monte Carlo precision would have required an inordinate amount of computer time to prove or illustrate a point. The differences in accuracy presented in Table I are not simply a result of stochastic luck on obtaining a "good" set of random numbers. The differences in the two versions represents a biasing in the original filter due to the lack of deterministic forcing. This point is brought out even more forcibly in the comparison of Figs. 20 and 21, and Figs. 22 and 23. These plots show that the errors in estimation for the Kalman filter on a typical run are roughly unbiased; however, the biasing on the estimation in both x and y coordinates from the alpha-beta filter is very obvious. Note that, as explained in II, the alpha-beta filter eventually "catches up" to the correct position. This occurs only after the initial period of banking at the limit is complete, and explains the peak in residual error which can be noted on the runs beginning at -20 K ft.

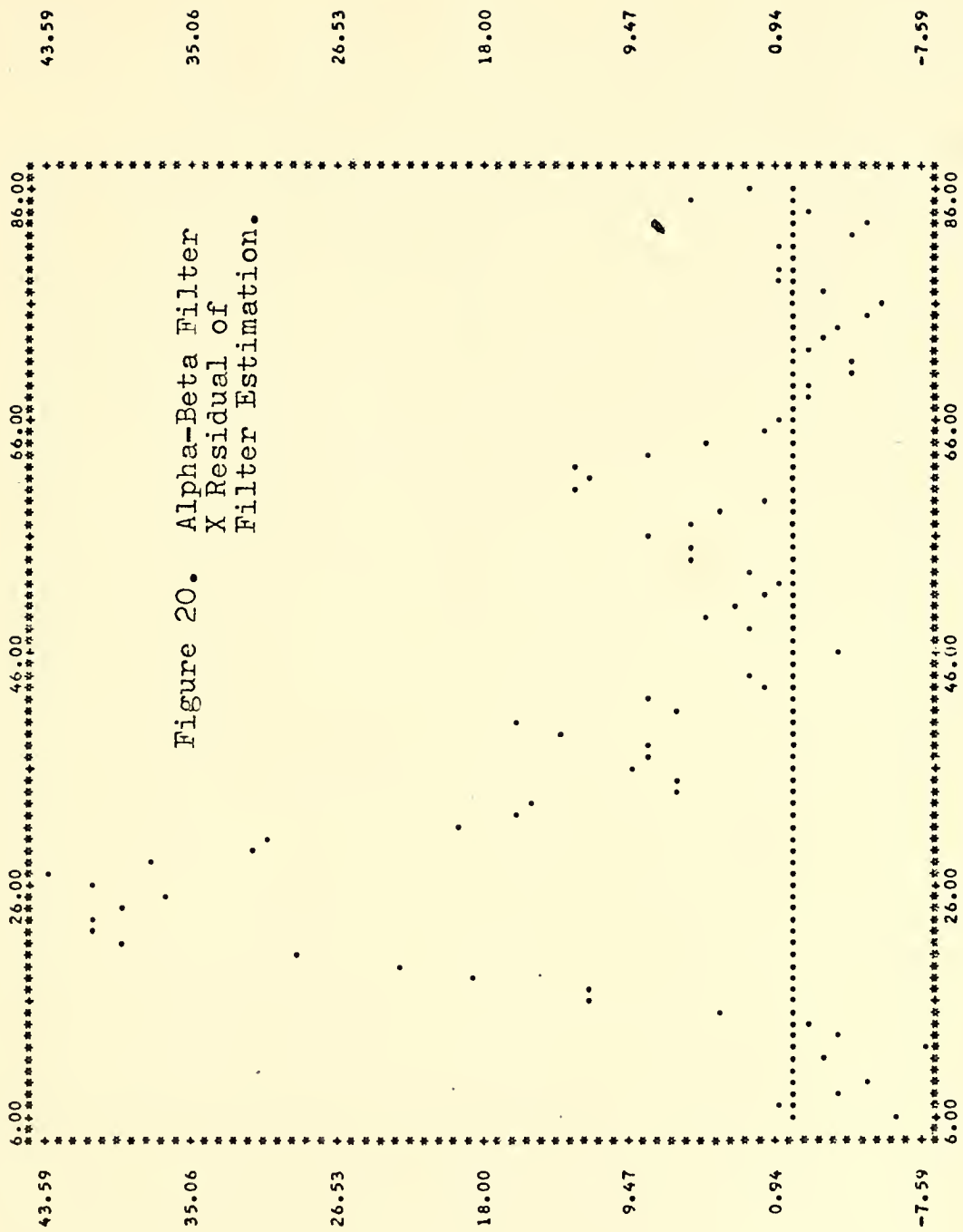
In theory, even if the alpha-beta filter had effects of deterministic forcing included, the Kalman filter would perform in a superior manner, due to its having an "optimal" gain schedule to give a minimum state covariance of error.

## 2. Bombing Accuracy and Time Response Comparison

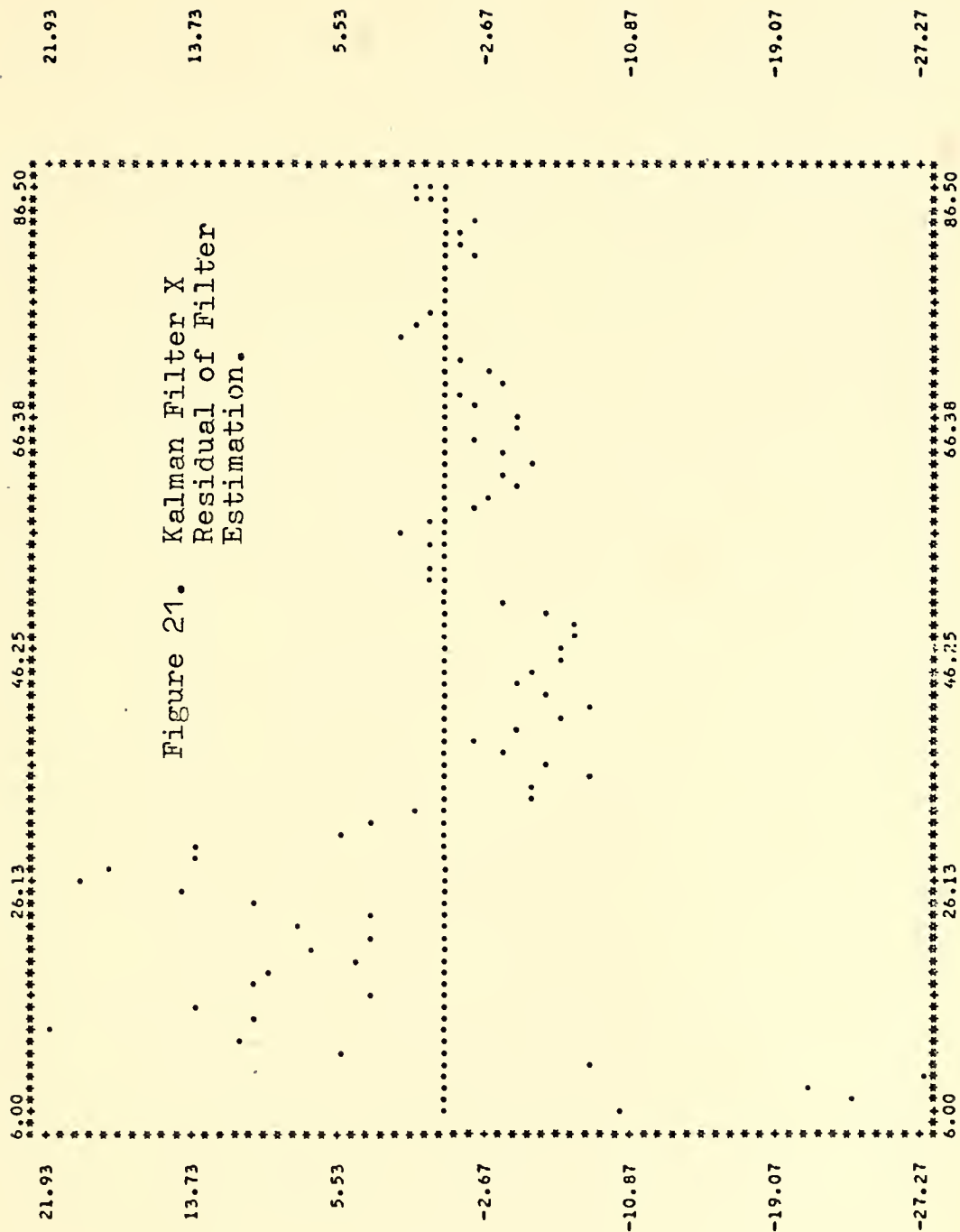
Two performance parameters on the overall Precision Guidance routine were observed and minimized throughout program development. The importance of actual bombing accuracy is obvious. A less obvious but very important parameter



X RESIDUAL VS. T

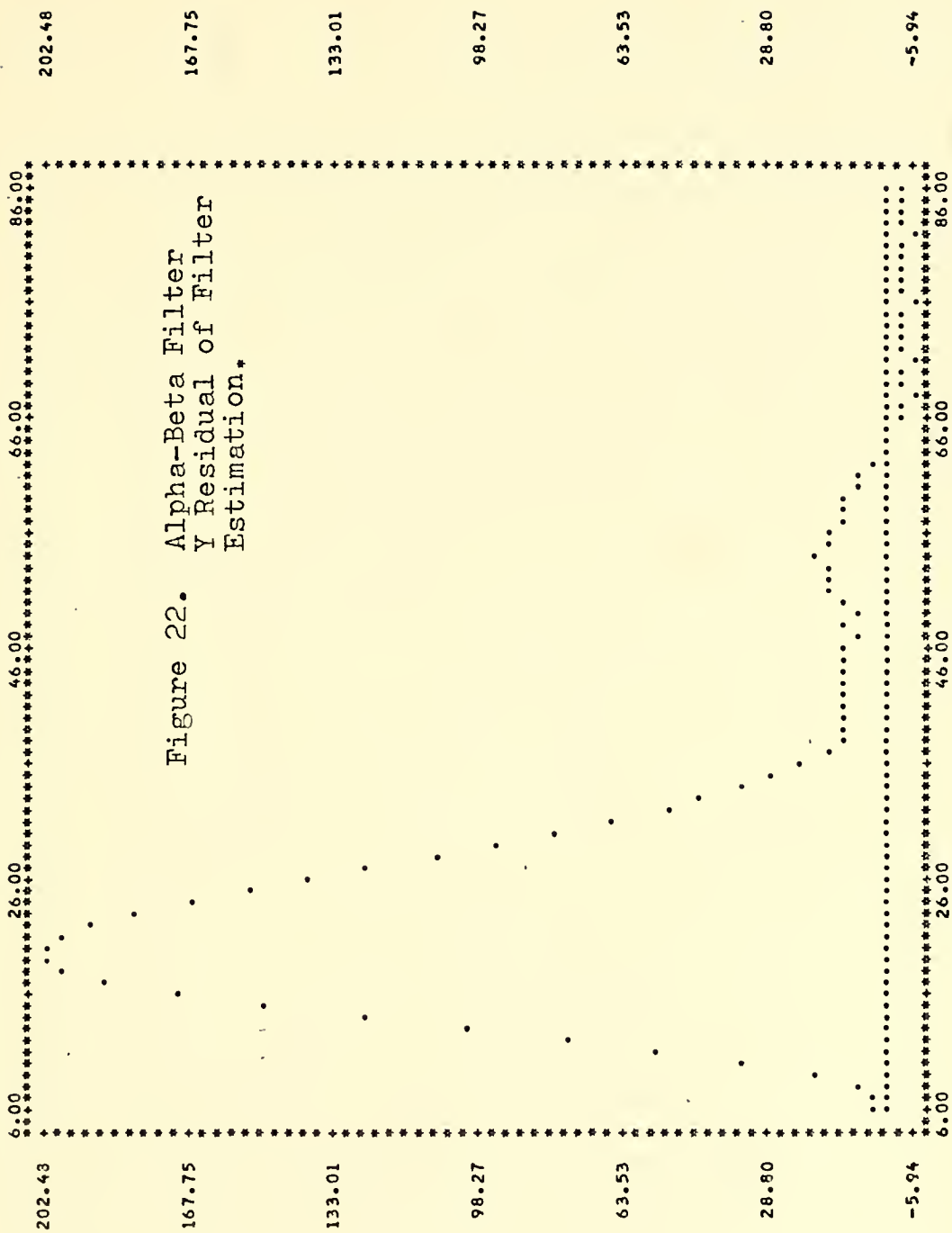






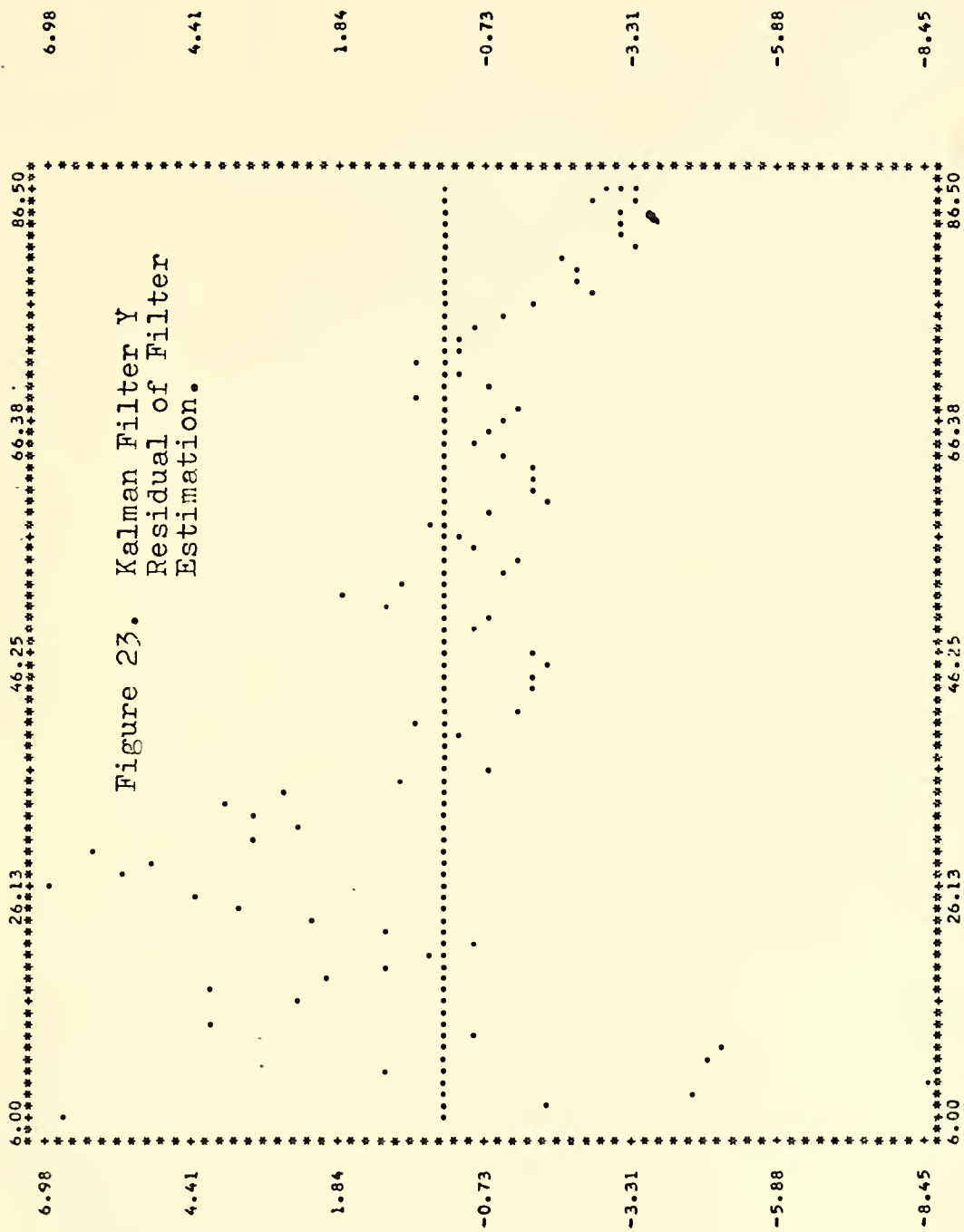


Y RESIDUAL VS. T











is the time required on the final bombing leg in order to achieve "sufficient" accuracy. The longer that a pilot is required to fly a straight path toward a target, the more his chances of being shot down increase. It is then desirable to swing onto the final leg from Coarse Guidance and complete the mission as soon as possible.

This time, to be designated T, was difficult to measure directly. It is a strong function of the amount of heading angle change required from Precision Guidance initialization. By varying the angles and distances to the target in the runs (1 through 10), it is possible to observe the amount of time required for the lateral error to reach some threshold minimum acceptable value, under which, in an absolute value sense, the bomb impact will be scored a successful mission. For the purpose of this study, this value was arbitrarily set at 70 feet.

Table II presents a summary of data from the simulation runs illustrating bombing accuracy and the time response parameter T. Note that most of the lists of bombing accuracies have a letter designation at the top of the respective columns. There are referenced on Figures 24 and 25, where comparisons of the bombing accuracies are presented graphically.

The inaccuracies resulting from those runs which start relatively close to the target are due to the fact that the aircraft cannot turn at a high enough rate to get on a bombing line passing near the target before it must drop the bomb. A



| Run No. Initial<br>x3 | ORIGINAL VERSION   |    |       |                    |      |       | IMPROVED VERSION   |       |       |                    |       |      |
|-----------------------|--------------------|----|-------|--------------------|------|-------|--------------------|-------|-------|--------------------|-------|------|
|                       | $\tau_b = 2$       |    |       | $\phi_b = 3^\circ$ |      |       | $\tau_b = 2$       |       |       | $\phi_b = 3^\circ$ |       |      |
|                       | $\phi_b = 0^\circ$ | T  | RI    | $\phi_b = 0^\circ$ | T    | RI    | $\phi_b = 0^\circ$ | T     | RI    | $\phi_b = 0^\circ$ | T     | RI   |
| <u>y3 = 20,000 ft</u> |                    |    | A     |                    |      | B     |                    |       | C     |                    |       | D    |
| 1. -50,000            | --                 | -- | 86    | --                 | --   | 90    | 22.5               | 12    | 12    | 19.5               | 28    | 23.5 |
| 2. -40,000            | --                 | -- | 151   | --                 | --   | 270   | 26.5               | 8     | 8     | 22.5               | 46    | 27   |
| 3. -30,000            | --                 | -- | 212   | --                 | --   | 331   | 32.5               | 9     | 9     | --                 | 126   | --   |
| 4. -20,000            | --                 | -- | 3457  | --                 | --   | 1283  | --                 | 2208  | 2208  | --                 | 199   | --   |
| 5. -10,000            | --                 | -- | 20130 | --                 | --   | 20104 | --                 | 20394 | 20394 | --                 | 20147 | --   |
| <u>y3 = 5,000 ft</u>  |                    |    | E     |                    |      |       |                    |       | F     |                    |       |      |
| 6. -50,000            | 68                 | -- | 41    | 13.5               | 9    |       | 13.5               | 9     |       |                    |       |      |
| 7. -40,000            | --                 | -- | 92    | 13.5               | 8    |       | 13.5               | 8     |       |                    |       |      |
| 8. -30,000            | --                 | -- | 98    | 14.5               | 30   |       | 14.5               | 30    |       |                    |       |      |
| 9. -20,000            | --                 | -- | 1120  | 19                 | 29   |       | 19                 | 29    |       |                    |       |      |
| 10. -10,000           | --                 | -- | 20435 | --                 | 6398 |       | --                 | 6398  |       |                    |       |      |

Table II. Precision Guidance Simulation Results. RI is bomb impact miss distance. T is time into run at which the lateral error dropped below 70 ft.



Figure 24. Illustration of Improvement in Bomb Impact Miss Distance for Varying Run Lengths. Initial y3 = 20,000 ft.  
Original Program Results: Curves A,B  
Improved Program Results: Curves C,D

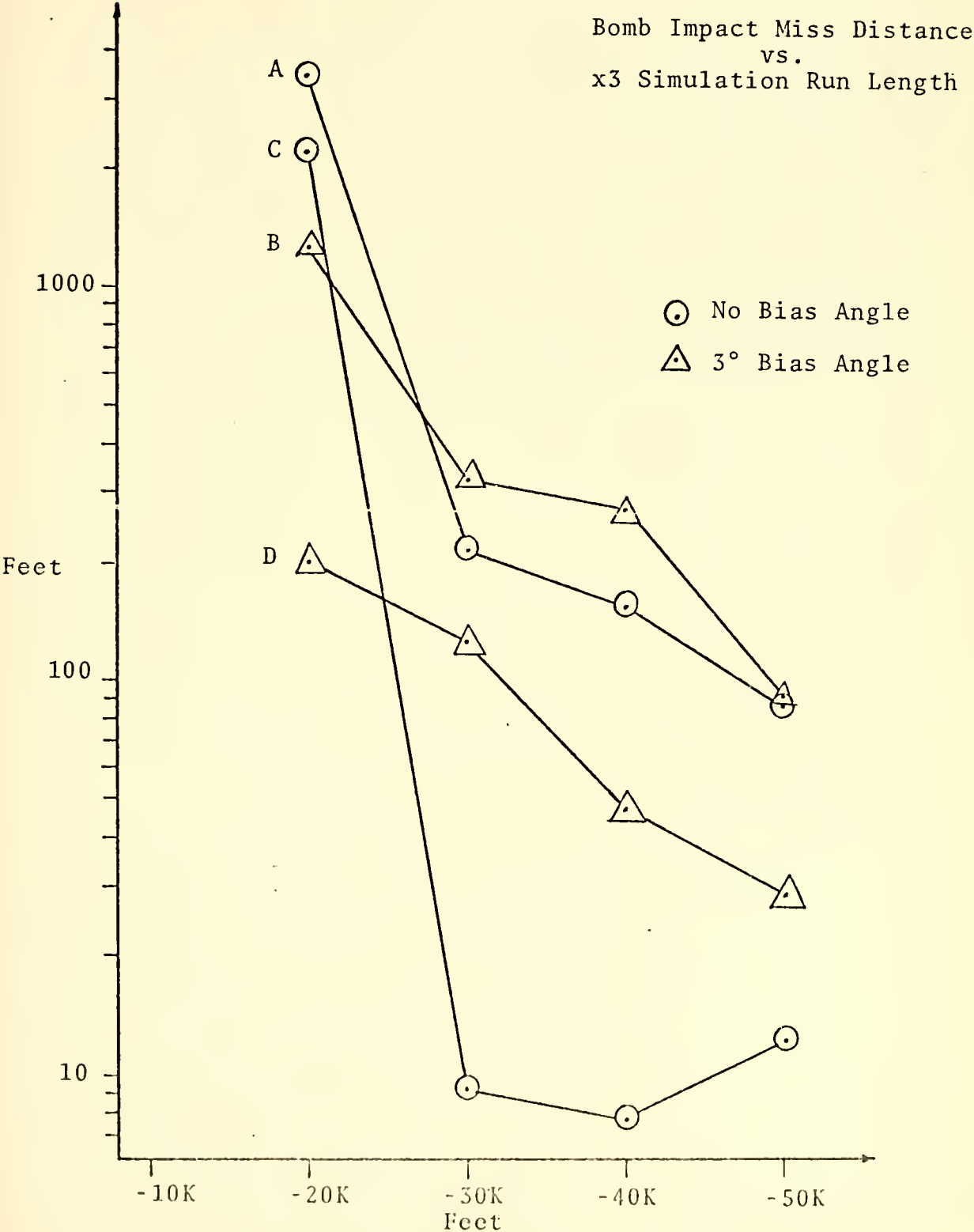
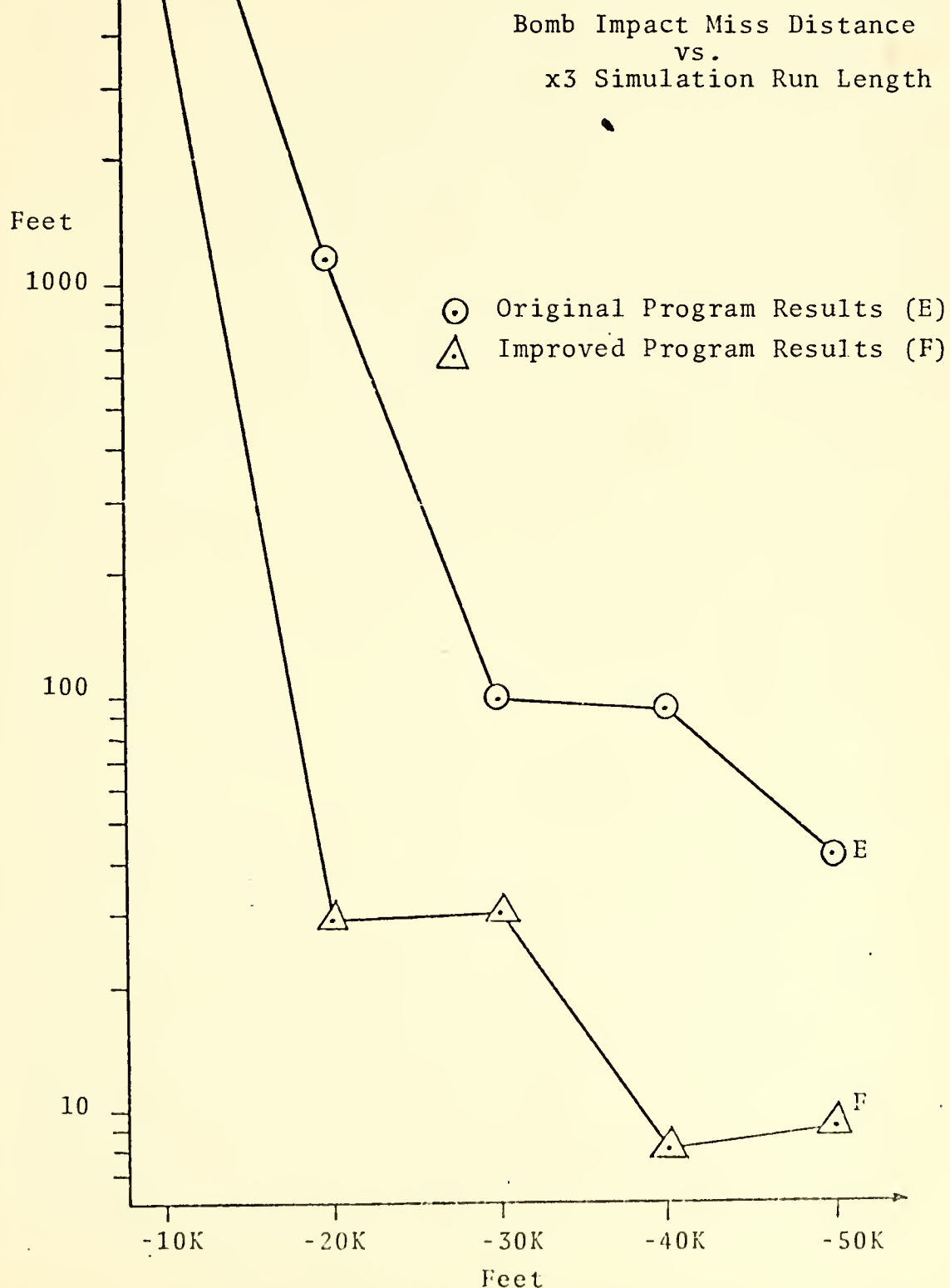
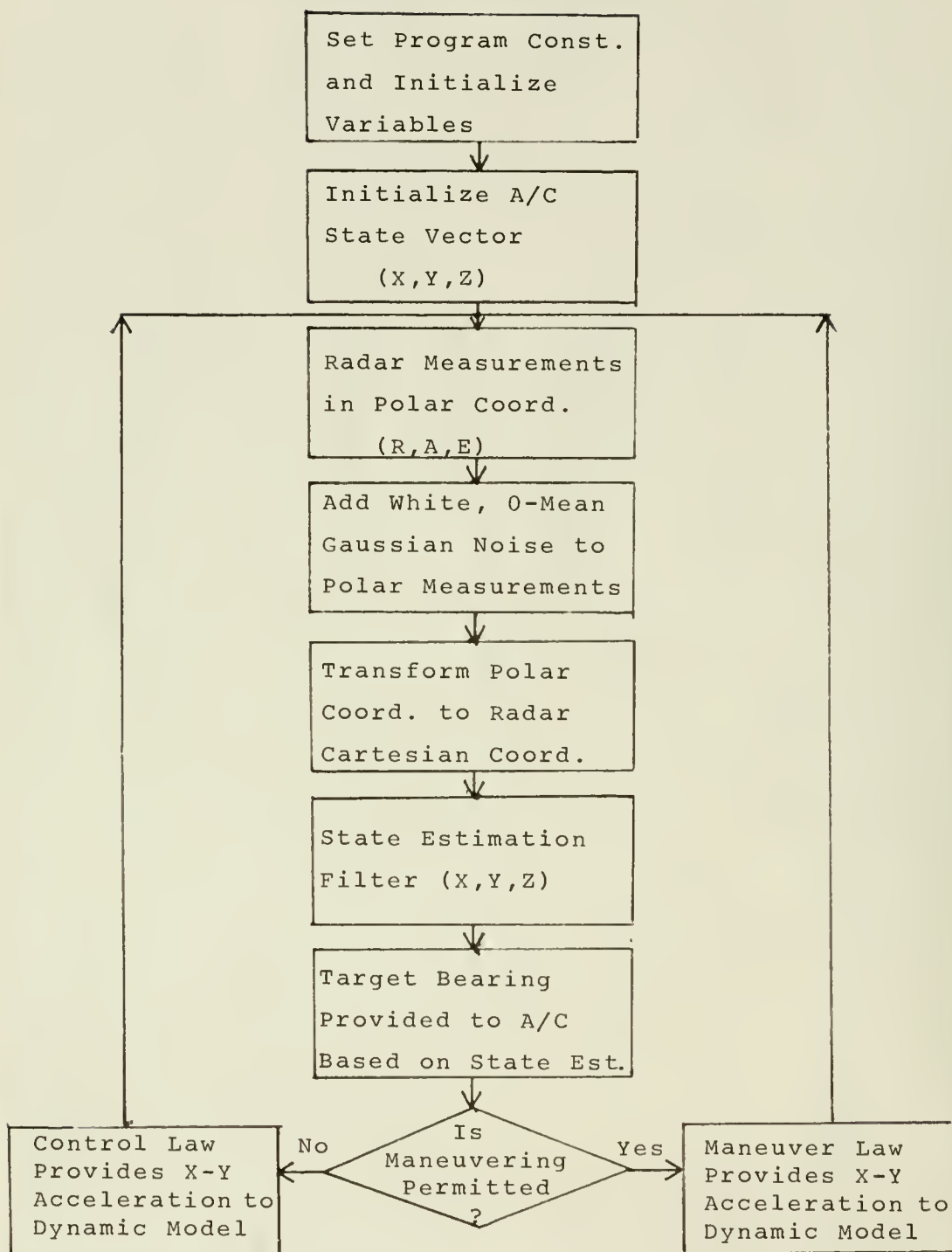






Figure 25. Illustration of Improvement  
in Bomb Impact Miss Distance  
for Varying Run Lengths.  
Initial  $y_3 = 5000$  ft.  
No bias angles.





large part of the error improvement which can be seen in these two figures is due to the filter improvement. However, the controller also has a large effect on the overall response of the aircraft. The use of angle rate feedback helps to drive the lateral error to zero faster than in the original version. This is presented graphically in Fig. 26. Note also that while the original version suffers the effect of a large overshoot past zero lateral error, the improved version does not. This is fundamentally the result of the rate feedback acting as a damper.

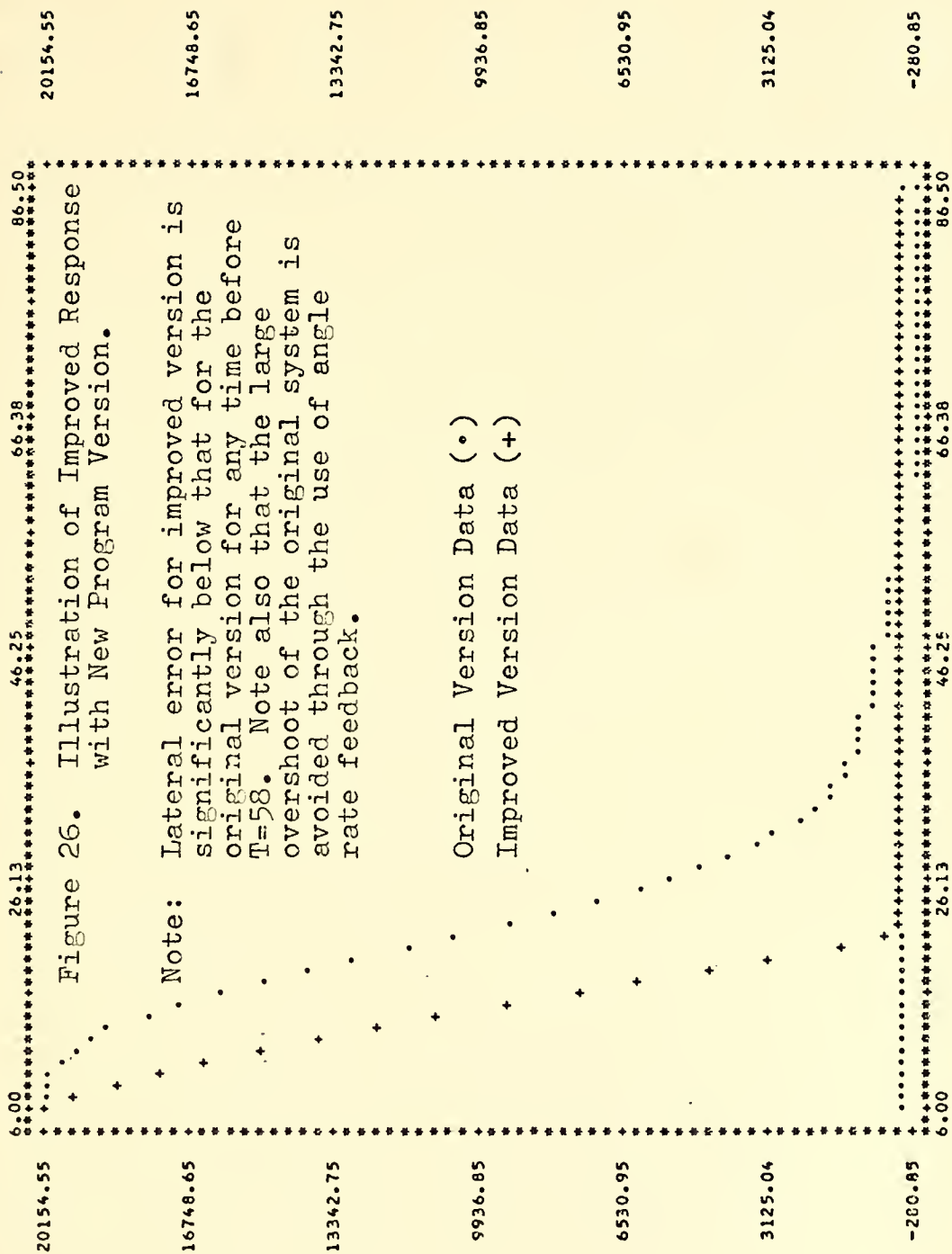
Examination of T in Table II will show that the original simulation program achieved a lateral error below 70 feet only once in the simulation trials run. The improved version reached the acceptable error 9 out of 15 times. Inspection of the times will show that very little time is required to achieve this figure of accuracy, including those runs which are initialized with rather extreme initial error angles (e.g., 3, 8, and 9). Use of the new algorithms to estimate position and control the aircraft should result in a marked improvement in overall accuracy in bombing and in time on the final leg required to achieve this accuracy.

#### B. COARSE GUIDANCE PERFORMANCE

No contrasting performance tests were performed for the Coarse Guidance mode. The primary reason for this is the lack of sufficient program documentation on the original version of Coarse Guidance. Thus, the Coarse Guidance results



# LATERAL ERROR (XE) COMPARISON PLOT





presented must stand on their own merit, on an absolute instead of a relative performance scale.

As was the case for Precision Guidance, a large number of Coarse Guidance simulation runs were completed in the process of obtaining the final program version. A sample of some of the representative track plots with the RMS track deviations for those runs are presented in Figs. 27 through 30. The significant aspects of each of these runs are discussed below.

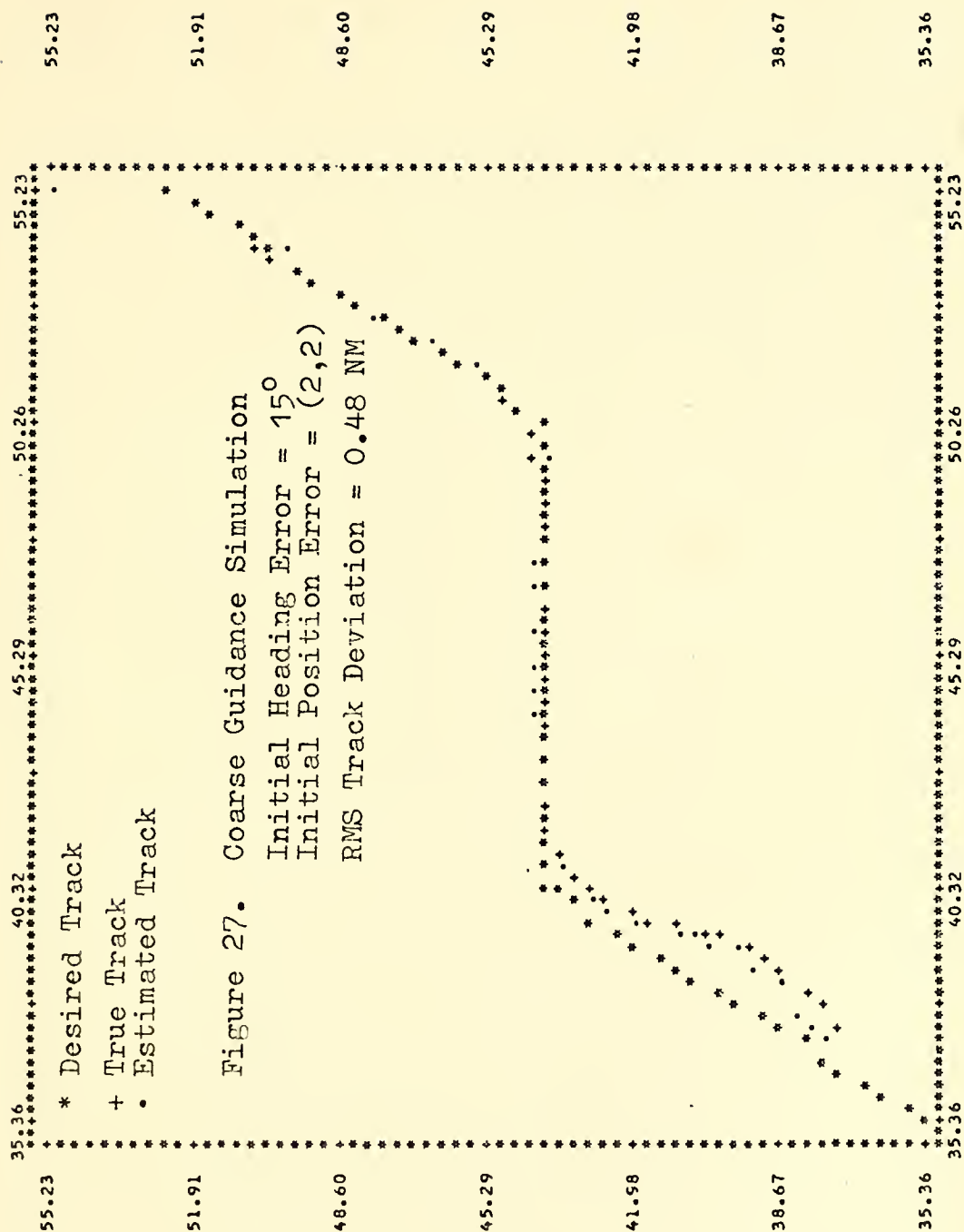
Figure 27 represents a rather simple track to follow, and is probably the most realistic track of the four presented. The turns to be executed and the initial heading and position errors are not excessive. The control and turn logic caused the aircraft to follow the desired path very closely.

The scale on Fig. 28 is about half of that for Fig. 27 and thus the initial errors are more obvious. The track deviation figure is higher here than before due to the fact that the initial errors tend to take the aircraft away from the desired track, vice in the track's general direction, as was the case for Fig. 27. Note that the control logic has caused the aircraft to fly toward the second waypoint. At the appropriate time, the aircraft begins a command turn in order to be aligned properly on the second leg upon turn completion. The error from this point on is minimal, never exceeding 0.28 NM on the final leg.

Figure 29 illustrates a most unlikely track to be encountered in practice, but one which checks out the program

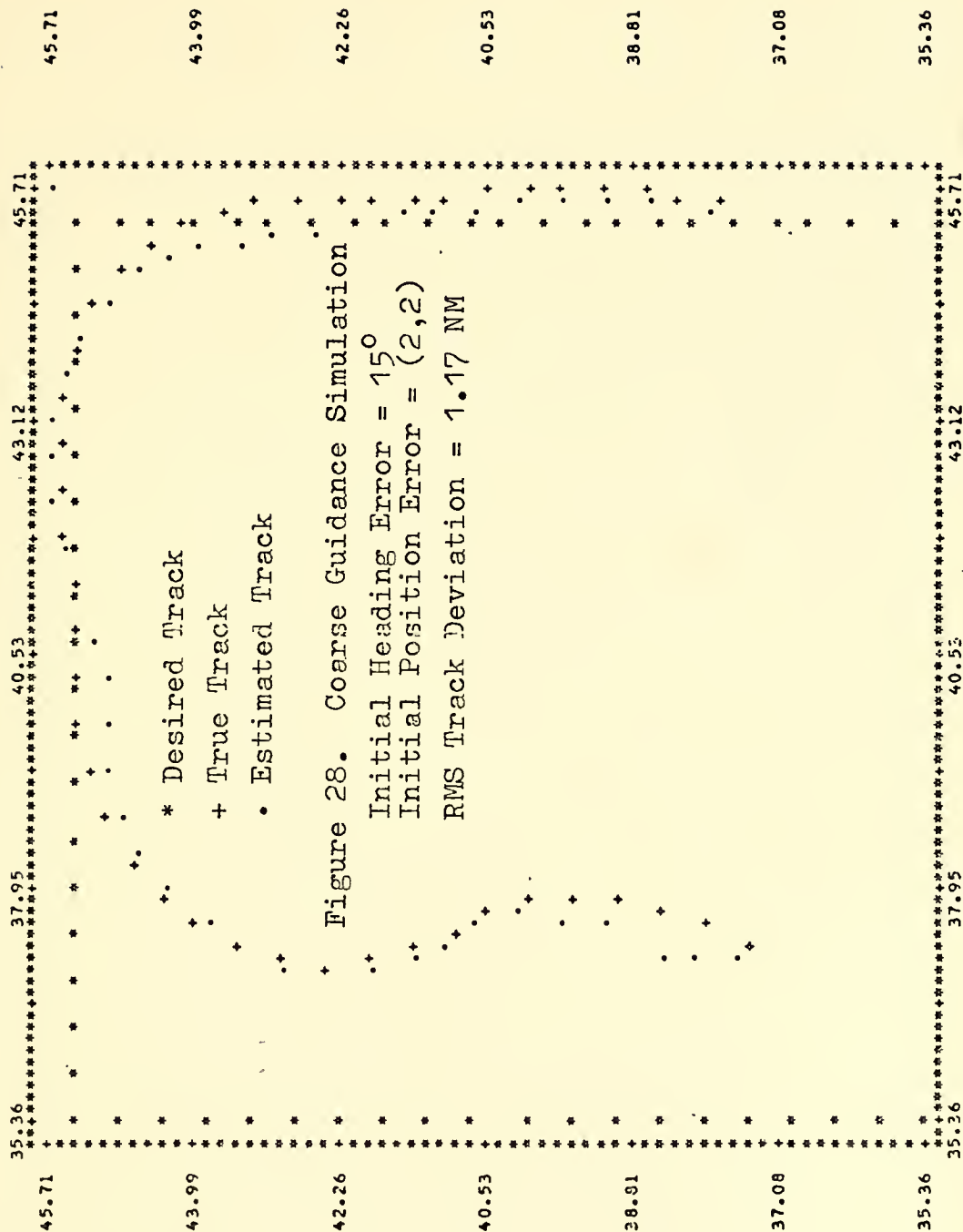




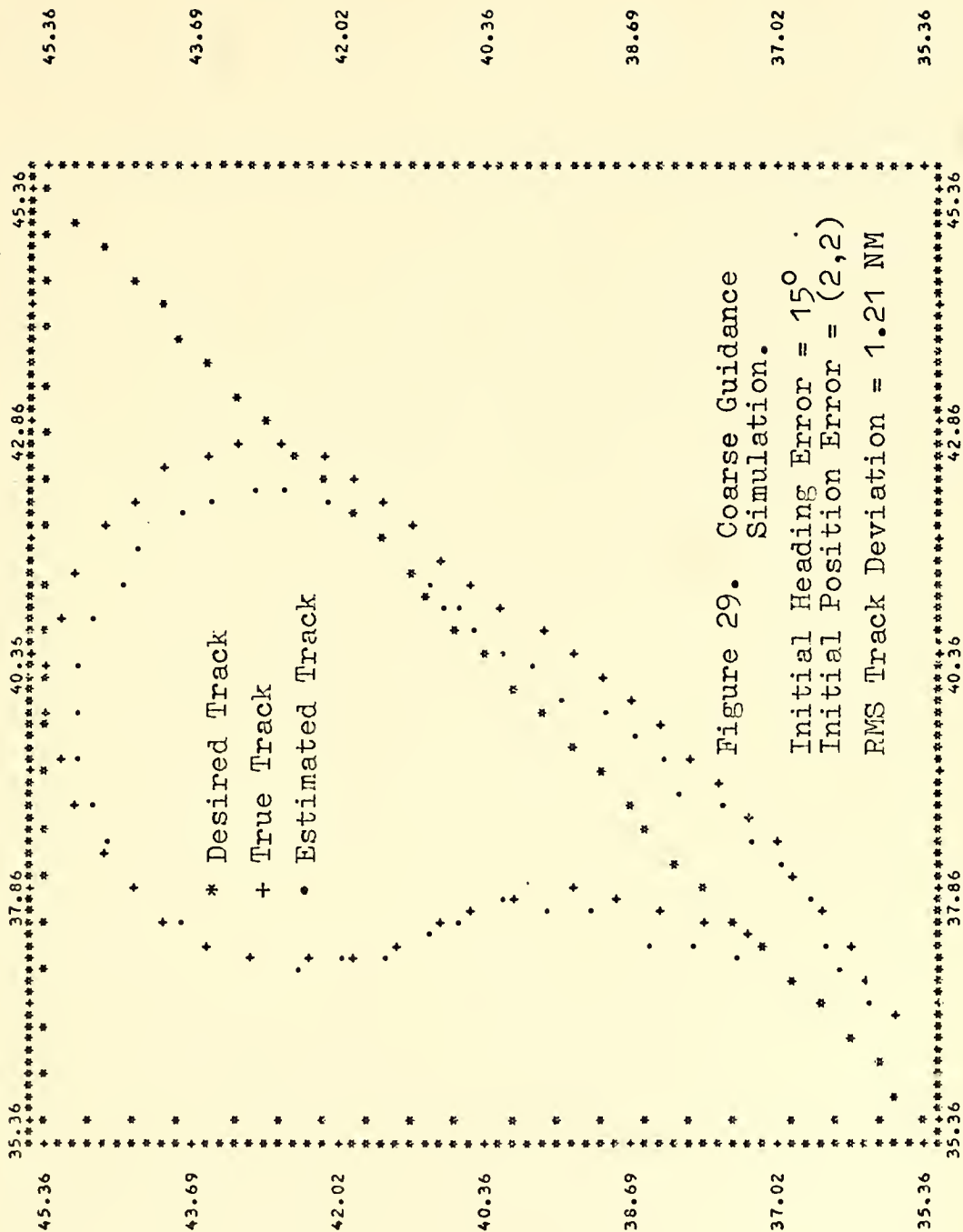




DESIRED, TRUE, AND ESTIMATED POSITION









algorithms quite well. The initial errors are as before. In this case, the aircraft exists from the first command turn only to note through turning logic that it is already a few seconds behind schedule to be able to make the correct turn onto the final leg. This is because of the combined condition of a relatively short leg length remaining and a requirement to execute  $135^\circ$  change in heading. It can be seen from the plot that the aircraft was not able to come to the correct final leg heading of  $225^\circ$  from the command turn control alone. Another effect which is evident from this run is the lack of position update information in the filter during a command turn, due to poor radar return simulation.

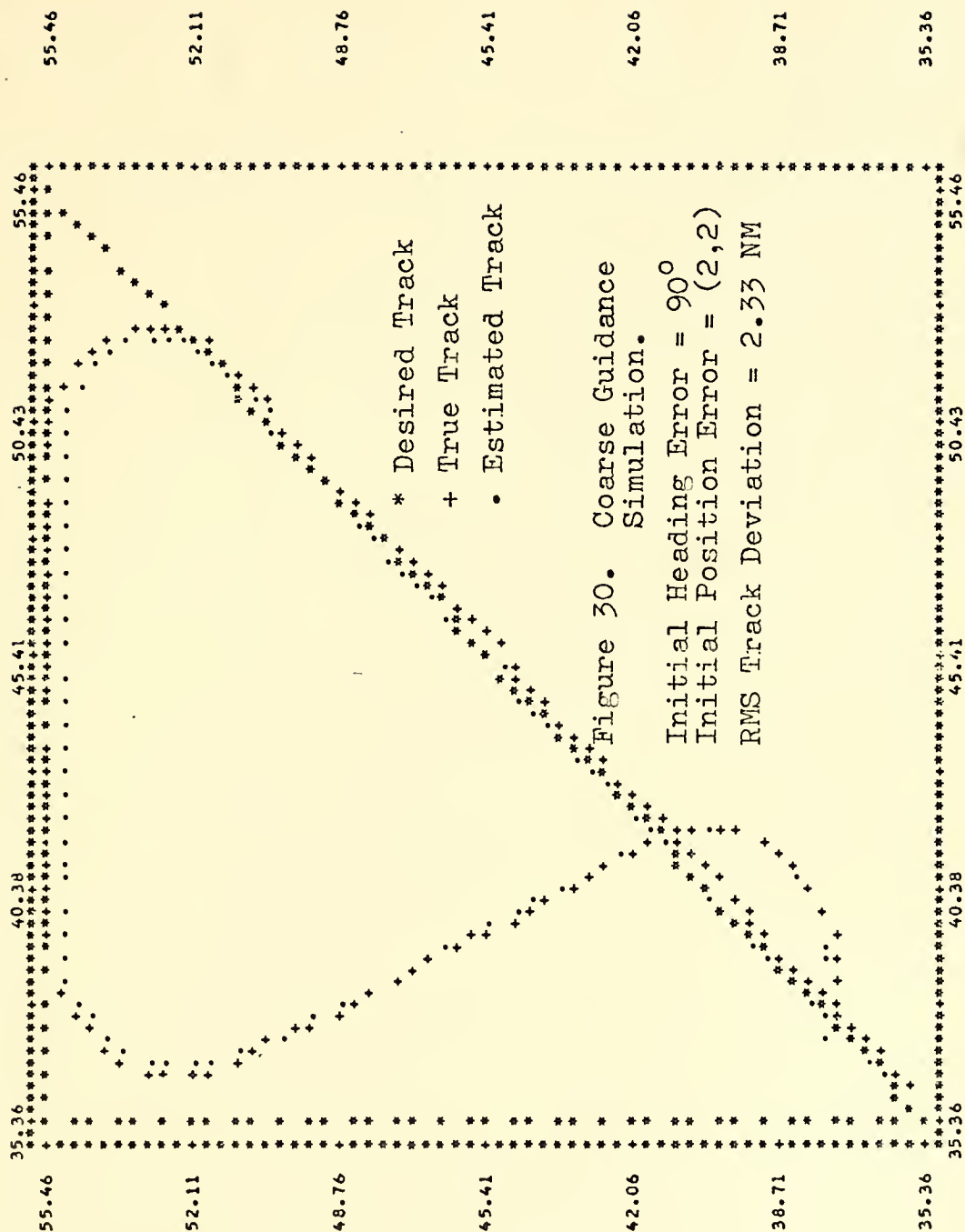
Figure 30 is the result of a track of the same shape as that used in Fig. 29, except the legs are twice as long. The initial position error is also the same as that for Fig. 29, but the initial heading error from the desired track in this case is  $90^\circ$ . The purpose of this track is to show that the program's algorithm can handle effectively a case such as that in Fig. 29, provided the given physical constraints of the system permit time to react.

Note that the aircraft performs the correct course change and heads for the second waypoint, and from that point on is nearly coincident with the desired track. The relatively high track deviation figure for this run is due almost entirely to the effects of the initial heading and position errors.





DESIRED, TRUE, AND ESTIMATED POSITION





Each of these runs was made with a minimum error heading for correction,  $H_{\text{ermin}}$ , of  $5^\circ$ . Use of this number on runs for which excessive initial errors were not present, i.e., Figs. 27 and 28, resulted in a command correction being sent less than 10 percent of the time during which command turns and initial error corrections were not in progress. This indicates a vast improvement towards the goal of decreasing the numbers of mid-course corrections being sent to the pilot during this phase of the problem.

Autopilot control of the aircraft during this phase was assumed because it was not known how to realistically model the effects of a pilot receiving an instruction to come to a new heading. If pilot control of the aircraft is desired, the algorithms used provide a heading error which could be used. In fact, it is this value which is used to compute the bank angle correction.

In summary, the improved Coarse Guidance algorithms appear to yield a greatly simplified and accurate technique for guiding the aircraft onto the final leg. In addition, the errors in position and heading as the aircraft enters the final leg are such that the Precision Guidance filter can be initialized with valid nonzero velocities, and thus the time required on the final leg can be reduced even further, since the requirement for a full six seconds without control could be reduced.



# APPENDIX A: LIST OF PRINCIPLE VARIABLES FOR THE PRECISION AND COARSE GUIDANCE SIMULATION PROGRAMS

## A. PRECISION GUIDANCE MAIN ROUTINE

|               |  |
|---------------|--|
| ATITLE-ZTITLE | Titles of the plots  |
| BIS           | Means of RADAR9 R, $\theta$ , and $\phi$ noise   |
| BFF           | Bomb ballistics form factor  |
| D             | Bomb diameter  |
| DEG           | Radian/degree conversion factor  |
| DT            | Radar sampling interval  |
| DTCON         | Control update interval  |
| EM1           | Matrix to convert from target to radar reference frame   |
| EM2           | Matrix to convert from radar to target frame   |
| EM3           | Matrix to rotate from X5 to X6 reference frame   |
| EV1           | Translation matrix to go from target to radar reference frame  |
| FILRES        | Contains estimation error in radar frame for x,y,z, and radial   |
| G             | Gravitational constant, 32.2 ft/sec <sup>2</sup>   |
| HDE           | Heading error angle  |
| HDEDOT        | Time derivative of HDE   |
| HA            | Height of target above sea level   |
| IB1           | Equal to 0 in level bombing mode   |
| IDTCON        | Integer relating DT to DTCON   |
| ITAB1         | Counter for number of points to plot   |
| ITH           | Equal to the number of times through main processing loop, except on last time through, when equal to -1 |
| IU            | Seed for random number generator, NORMAL   |
| KTH           | Counter to indicate time for integration for RA and TF calculations                                      |
| MWLD          | Number of "wild points" to be thrown out by RADAR9 as invalid  |



|                 |  |
|-----------------|--|
| NWLD            | Set equal to MWLD at time TWLD and decremented as "wild points" are used |
| NTB             | Number of bombing constant table to be used                              |
| PH              | True bank angle  |
| PH1             | Estimated bank angle   |
| PHD             | Desired feedback command   |
| PHD1            | Desired feedback command from HDE  |
| PHD2            | Desired feedback command from HDEDOT                                     |
| PHDAVG          | Command to be ordered for last two seconds before bomb release           |
| PHB             | Autopilot bias bank angle  |
| PHC             | Command bank angle sent  |
| PS              | True aircraft heading angle in target frame                              |
| PS1             | Estimated aircraft heading angle in radar frame                          |
| PSD             | True aircraft turning rate   |
| RE              | Radius of the Earth  |
| RBT             | Distance from aircraft (estimated) to the target                         |
| SIG(1) - SIG(3) | Standard deviations of R, $\theta$ , and $\phi$                          |
| SIG(4) - SIG(6) | Initial radar velocity estimates   |
| SIGW            | Standard deviations of random forcing to be assumed for calculation of Q |
| T               | Time into the simulation run   |
| TB              | $\tau_b$ , the aircraft roll response time constant                      |
| TG              | Time-to-Go to release bomb   |
| TF              | Time of fall for the bomb  |
| TLVL            | Time for required level flight before bomb release; equal to two seconds |
| TLVL1           | Equal to TLVL +1   |
| VE              | Total airspeed   |
| VEH             | Horizontal airspeed  |
| W               | Weight of bomb in pounds   |
| WH              | Estimated wind in target frame   |
| WR              | Estimated wind in radar frame  |
| WT              | True wind in target frame  |





|             |   |
|-------------|---|
| X1,XD1,XDD1 | Estimated position, velocity and acceleration in radar frame  |
| X2,XD2      | True position and velocity in radar frame   |
| X3,XD3      | True position and velocity in target frame  |
| X5,XD5      | Estimated position and relative velocity of target with respect to the aircraft; "primed system"  |
| X6,XD6      | X5,XD5 system rotated to align the YD6 axis pointing at the target; for printing and plotting purposes, this vector contains the error between true and estimated position in the X3/X5 frame |
| XE          | Lateral error   |
| XGC         | X bomb impact point in X6 frame   |
| XXA-XXG     | Arrays used to store variables for plotting at program end  |
| YYA-YYU     | Arrays used to store variables for plotting at program end  |
| YGC         | Y bomb impact point in the X6 frame   |

#### B. SUBROUTINE ARCRFT

|           |   |
|-----------|---|
| CA1 - CA5 | Constants used in aircraft motion equations                                 |
| DT        | Radar sampling interval; also interval of update for aircraft true position |
| DEG       | Radian/degree conversion factor   |
| DT3       | Equal to DT/2   |
| G         | Gravitational acceleration, 32 ft/sec <sup>2</sup>                          |
| ITH       | Equal to number times through loop, except on last time when ITH = -1       |
| IB1       | Equal to zero for level flight mode   |
| PH        | True bank angle   |
| PHB       | Bank angle bias   |
| PHC       | Command bank angle  |
| PHN       | New bank angle  |
| PS        | Heading angle   |
| PSD       | Heading angle rate  |
| PSDN      | New heading angle rate  |



|     |  |
|-----|--|
| PSN | New heading angle                          |
| T   | Elapsed time since start of run            |
| TB  | $\tau_b$ , the roll response time constant |
| TG  | Time to go to release bomb                 |
| VT  | Horizontal airspeed                        |
| WT  | True wind vector                           |
| X3  | Aircraft position in target frame          |
| XD3 | Aircraft velocity in target frame          |

#### C. SUBROUTINES RADAR6 AND RADAR9

|                     |   |
|---------------------|---|
| A                   | Azimuth angle   |
| ADDSUB              | Subroutine entry to add or subtract two matrices                              |
| ADUM                | Temporary array used in matrix arithmetic                                     |
| ANGMAX              | Maximum angle, used to prevent overflow                                       |
| ANGMIN              | Minimum angle, used to prevent underflow                                      |
| BIS                 | Range, azimuth, and elevation noise bias                                      |
| BDUM                | Temporary array used for matrix arithmetic                                    |
| CA1,CA4,CA5<br>CAA2 | Constants used in aircraft motion equations                                   |
| DEG                 | Radian/degree conversion constant   |
| DT                  | Radar sampling interval in RADAR9   |
| DTRAD               | Radar sampling interval in RADAR6   |
| DTCUM               | Accumulator to determine next time to sample position in RADAR6               |
| DT2                 | Equal to $DT^2/2$   |
| DTRAD2              | Equal to $DTRAD^2/2$  |
| DT3                 | Equal to $DT/2$   |
| DT4                 | Equal to $DT^3/6$   |
| E                   | Elevation angle   |
| E1,E2,E3            | Difference between predicted position and data sample during state estimation |
| G                   | Gain matrix   |



|                 |  |
|-----------------|--|
| GG              | Gravitational acceleration, 32 ft/sec <sup>2</sup>   |
| GAMMA           | $\Gamma$ matrix  |
| GNX, GNY, GNZ   | G(1,1), G(4,2), and G(7,3) terms of the gain matrix  |
| H               | Measurement matrix   |
| HT              | Measurement matrix transposed  |
| INVERT          | Subroutine entry to invert a matrix  |
| ITH             | Equal to number of times through main processing loop, except on last time through when ITH = -1 |
| IU              | Seed for random number generator, NORMAL   |
| NORMAL          | Subroutine to generate normally distributed random variables to be used as noise                 |
| PE              | Covariance of estimation error matrix  |
| PH1             | Estimated bank angle   |
| PHC             | Command bank angle   |
| PHI             | State transition matrix used for gain generation only  |
| PHITRN          | Transpose of PHI   |
| PROD            | Subroutine entry to perform the product of two matrices  |
| PS1             | Estimated heading angle with respect to the wind   |
| PSN             | Predicted new heading angle before acceleration estimate correction                              |
| PSD1            | Estimated turning rate   |
| Q               | Array resulting from expected random forcing assumption  |
| R               | Range to target  |
| RAN             | Contains random numbers from NORMAL  |
| SIG(1) - SIG(3) | Standard deviation for R, $\theta$ , and $\phi$  |
| SIG(4) - SIG(6) | Initial velocity estimates for prediction  |
| SIGW            | Standard deviations of random forcing in x, y, and z of radar frame                              |
| TB              | Roll response time constant, $\tau_b$  |
| TRANS           | Subroutine entry to perform the transpose of an array  |



|                |   |
|----------------|---|
| VT1            | Estimate of horizontal airspeed                                 |
| VARR,VART,VARP | Variances of R, $\theta$ , and $\phi$                           |
| WR             | Estimated wind vector in the radar frame                        |
| X1,XD1,XDD1    | Estimated state vector in radar frame (XDD1 not used in RADAR6) |
| X2,XD2         | True state position and velocity in the radar frame             |
| X1P,XD1P,XDD1P | Predicted state vector in radar frame                           |
| XDATA          | Cartesian radar observation with noise                          |
| XIDENT         | Identity matrix   |

#### D. COARSE GUIDANCE MAIN ROUTINE

|               |  |
|---------------|--|
| ATITLE-ETITLE | Titles for plots                                       |
| AZ            | Array for storing average leg azimuths                 |
| AZI           | Initial azimuth for first leg                          |
| BIS           | Array for RADAR6 noise biases                          |
| DEG           | Degree to radian conversion factor                     |
| DEL           | Initial displacement vector for true aircraft position |
| DT            | Set equal to DTCON                                     |
| DTCON         | Control update interval                                |
| DTRAD         | Radar sampling interval                                |
| DTG           | Distance from X1 to leg intersection                   |
| EEST          | Estimated aircraft deviation from leg                  |
| ETRUE         | True aircraft deviation from leg                       |
| FEET          | Feet-to-nautical mile conversion factor                |
| G             | Gravitational acceleration constant                    |
| G1            | HDE gain constant, $G_1$                               |
| G2            | HDEDOT gain constant, $G_2$                            |
| H             | Array of desired air headings                          |
| HEA           | Estimated aircraft air heading                         |
| HTA           | True aircraft air heading                              |
| HEG           | Estimated aircraft ground heading                      |





|                 |  |
|-----------------|--|
| HTG             | True aircraft ground heading   |
| HDE             | Heading angle error  |
| HDEDOT          | Heading angle error rate   |
| HERMIN          | Minimum error angle for which commands will be sent  |
| I               | Equal to the index on the current leg  |
| IDTRAD          | Integer relating DTCON and DTRAD   |
| IEND            | Equal to 0 except on last leg  |
| ITH             | Equal to the number of times through the main processing loop                              |
| IU              | Seed for the random number generator   |
| NLEG            | Number of legs for the run   |
| PHB             | Bias angle; assumed zero   |
| PHC             | Command bank angle   |
| PHD             | Desired bank angle from controller   |
| PLENGTH         | Length of each leg   |
| RAD             | Radian to degree conversion factor   |
| RMSEST          | RMS value of EEST  |
| RMSETR          | RMS value of ETRUE   |
| RANGE           | Array containing average range to each leg   |
| RANGEI          | Range to start of first leg from the radar   |
| SIG(1) - SIG(3) | Standard deviations for R, $\theta$ , and $\phi$   |
| SIG(4) - SIG(6) | Initial velocities for filter prediction   |
| SIGW            | Standard deviations for assumed random forcing; assumed zero for all runs in this study    |
| T               | Time into simulation run   |
| TB              | True aircraft roll response time constant  |
| TAUH            | Estimated aircraft roll response time constant; set equal to TB for all runs in this study |
| TINTRN          | Time into a command turn   |
| THETA           | Array containing azimuths of each leg  |
| THETW           | Direction toward which true wind blows   |



|         |   |
|---------|---|
| THETWH  | Direction toward which estimated wind blows             |
| TLEG    | Array containing desired time to cover each leg         |
| TLEG1   | Estimated time remaining on a leg                       |
| TSTOP   | Time at which problem ends                              |
| TSTPTN  | Time at which a zero bank command is sent to end a turn |
| TTOTTN  | Time at which a turn is completely over                 |
| TG      | Time to go to start a turn                              |
| VA      | True airspeed   |
| VAH     | Estimated airspeed                                      |
| VEG     | Estimated ground speed                                  |
| VTG     | True ground speed                                       |
| VW      | True wind speed   |
| VWH     | Estimated wind speed                                    |
| WR      | Equal to WH; components of estimated wind               |
| WT      | Components of true wind                                 |
| X1,XD1  | Estimated aircraft position and velocity                |
| X2,XD2  | Desired track data; used for plotting only              |
| X3,XD3  | True aircraft position and velocity                     |
| XWP     | Array containing x waypoint coordinates                 |
| XXA-XXE | Arrays for use in plotting                              |
| YYA-YYE | Arrays for use in plotting                              |
| YWP     | Array containing y waypoint coordinates                 |

Note: There are several variables with the suffix NM. These variables correspond to the variable without the suffix, except the NM indicates the value stored is in nautical miles.



# APPENDIX B: PRECISION GUIDANCE INPUT DATA FORMAT DEFINITION

| <u>CARD</u> | <u>COLUMNS</u> | <u>FORMAT</u> | <u>VARIABLE</u> | <u>REMARKS</u>              |
|-------------|----------------|---------------|-----------------|-----------------------------|
| 1           | 1-10           | F10.3         | WT(1)           | True wind in target frame   |
|             | 11-20          |               | WT(2)           | x,y, and z directions;WT(3) |
|             | 21-30          |               | WT(3)           | is usually zero             |
|             | 31-40          |               | WH(1)           | Estimated wind in target    |
|             | 41-50          |               | WH(2)           | frame;WH(3) is usually      |
|             | 51-60          |               | WH(3)           | zero                        |
| 2           | 1-10           |               | BIS(1)          | Bias on range, azimuth      |
|             | 11-20          |               | BIS(2)          | and elevation noise         |
|             | 21-30          |               | BIS(3)          |                             |
|             | 31-40          |               | SIG(4)          | Initial velocity estimates  |
|             | 41-50          |               | SIG(5)          | for filter prediction       |
|             | 51-60          |               | SIG(6)          |                             |
| 3           | 1-10           |               | SIG(1)          | Standard deviations on      |
|             | 11-20          |               | SIG(2)          | range, azimuth, and         |
|             | 21-30          |               | SIG(3)          | elevation noise             |
| 4           | 1-10           |               | SIGW(1)         | Standard deviations of      |
|             | 11-20          |               | SIGW(2)         | assumed random forcing in   |
|             | 21-30          |               | SIGW(3)         | x,y,and z of radar frame    |
| 5           | 1-10           |               | X3(1)           | Initial position (x,y,z)    |
|             | 11-20          |               | X3(2)           | of aircraft in target       |
|             | 21-30          |               | X3(3)           | frame                       |
| 7           | 1-10           |               | PHB             | Autopilot bias angle        |
|             | 11-20          |               | TB              | Roll response time constant |
|             | 21-30          |               | DT              | Radar sampling interval     |
|             | 31-40          |               | DTCON           | Control update interval     |
|             | 41-50          |               | PHI             | Latitude of target          |
|             | 51-60          | F10.3         | TWLD            | Time to start wild points   |
|             | 61-63          | I3            | MWLD            | Number of wild points       |
|             |                |               |                 |                             |



| <u>CARD</u> | <u>COLUMNS</u> | <u>FORMAT</u> | <u>VARIABLE</u>   | <u>REMARKS</u>  |
|-------------|----------------|---------------|-------------------|---|
| 8           | 1-10           | F10.3         | T3                | Nominal dive duration   |
|             | 11-20          |               | THNM              | Combine to give angle   |
|             | 21-30          |               | THDM              | radar and target  |
|             | 31-40          |               | THD               | Nominal dive angle  |
|             | 41-50          |               | ATT               | True tang. accel. during dive   |
|             | 51-60          |               | ATH               | Est. tang. accel. during dive   |
| 9           | 1-10           |               | ANH               | Max. aircraft normal accel.   |
|             | 11-20          |               | TUP               | Aircraft pitch time constant  |
|             | 21-30          |               | HTOL              | Angle and altitude tolerances   |
|             | 31-40          |               | ATOL              | for dive pullout  |
|             | 41-50          | F10.3         | S                 | Equal to 9999   |
|             | 51-53          | I3            | IB1               | Equal to zero for level flight  |
|             | 54-56          | I3            | IACC              | Equal to zero for no acceleration compensation                                |
| 40-49       | 1-48           | 6A8           | ATITLE-<br>ZTITLE | Titles for plots. Two cards per plot for two lines of title per plot          |
| 50          | 1-10           | F10.3         | WBLX              | Ballistic wind in x   |
|             | 11-20          |               | WBLY              | Ballistic wind in y   |
|             | 21-30          |               | BFF               | Ballistic form factor   |
|             | 31-40          |               | D                 | Bomb diameter, inches   |
|             | 41-50          | F10.3         | W                 | Bomb weight, pounds   |
|             | 51-53          | I3            | NTB               | Number of bombing table to be used  |
| 51-...      |                |               |                   | Bombing table data as supplied with original program; this remains unchanged. |





# APPENDIX C: COARSE GUIDANCE INPUT DATA FORMAT DEFINITION

| <u>CARD</u>      | <u>COLUMNS</u> | <u>FORMAT</u> | <u>VARIABLE</u> | <u>REMARKS</u>  |
|------------------|----------------|---------------|-----------------|---|
| 1                | 1              | I1            | NLEG            | Number of legs  |
|                  | 2-10           | F9.2          | RANGEI          | Range of first leg from radar                             |
|                  | 11-20          | F10.4         | AZI             | Azimuth of first leg from radar                           |
|                  | 21-30          |               | VA              | True airspeed   |
|                  | 31-40          |               | VAH             | Est. airspeed   |
|                  | 41-50          |               | VW              | True wind speed   |
|                  | 51-60          |               | VWH             | Est. wind speed   |
|                  | 61-70          |               | THETW           | True direction of wind                                    |
|                  | 71-80          |               | THETWH          | Est. direction of wind                                    |
| 2                | 1-10           | F10.3         | PLENGTH(i)      | Length of the ith leg                                     |
| thru<br>NLEG+1   | 11-20          |               | THETA(i)        | and its associated azimuth where i=1, NLEG                |
| NLEG+2           | 1-10           |               | HTG             | True initial ground heading                               |
|                  | 11-20          |               | DELNM(1)        | Displacement of true position from RANGEI, AZI in x and y |
|                  | 21-30          |               | DELNM(2)        |   |
|                  | 31-40          |               | DELNM(3)        | DELNM(3) is altitude of aircraft in NM                    |
| NLEG+3<br>NLEG+4 | 1-48           | 6A8           | ATITLE          | Title for plot of true, estimated and desired paths       |

Note: All angles are in degrees from North, clockwise angles positive 0 - 360 degrees. All speeds in ft/sec. All lengths are in nautical miles on entry.



## AN:TPU-27 SIMULATION

## INITIAL CONDITIONS :

```

ISSUE WINO AT TARGET = 0.0 0.0 0.0 0.0
ESTIMATED WINO AT TARGET = 0.0 0.0 0.0 0.0

RADAR DATA
NUMBER OF NOISY POINTS(MWLD) = 0.0
START TIME OF WLD POINTS = 0.0
MEASUREMENT SIGMAS(RF,F,AZ,WRAD),E(LMSAO)} = 1.500000 01
WEASUREMENT BIASES( = 0.0 0.0 0.0 0.0 0.0 0.0
INITIAL VELOCITY MEASUREMENT VALUES = 0.0 0.0 0.0 0.0
RANDOM FORECAST ASSUMPTION VALUES (SIGMA) = 0.0 0.0 0.0 0.0
RADAR SAMPLING INTERVAL = 0.1250

INITIAL POSITION OF A/C IN TARGET SYSTEM = -3.000000 04 5.000000 03 1.000000 04
INITIAL VELOCITY OF A/C IN TARGET SYSTEM = 5.000000 02 0.0 0.0

```

✈ AIRCRAFT PASSENGERS :

$\text{pH}_B = 2.00000$        $\text{pH}_S = 0.0$

## CONTROL PARAMETERS:

OTCON = 0.12500  
G1 = 75.0000  
G2 = 75.0000

### BALLISTIC TABLE PARAMETERS:

RELUCTANT WIND VAS: IFC (WBLX-WALY) = 0.0 0.0

| Q: VFE | BCMBING | MCOE | PARAMETERS: |
|--------|---------|------|-------------|
| 1      | 1       | 1    | 1           |
| 2      | 2       | 2    | 2           |
| 3      | 3       | 3    | 3           |
| 4      | 4       | 4    | 4           |
| 5      | 5       | 5    | 5           |
| 6      | 6       | 6    | 6           |
| 7      | 7       | 7    | 7           |
| 8      | 8       | 8    | 8           |
| 9      | 9       | 9    | 9           |
| 10     | 10      | 10   | 10          |
| 11     | 11      | 11   | 11          |
| 12     | 12      | 12   | 12          |
| 13     | 13      | 13   | 13          |
| 14     | 14      | 14   | 14          |
| 15     | 15      | 15   | 15          |
| 16     | 16      | 16   | 16          |
| 17     | 17      | 17   | 17          |
| 18     | 18      | 18   | 18          |
| 19     | 19      | 19   | 19          |
| 20     | 20      | 20   | 20          |
| 21     | 21      | 21   | 21          |
| 22     | 22      | 22   | 22          |
| 23     | 23      | 23   | 23          |
| 24     | 24      | 24   | 24          |
| 25     | 25      | 25   | 25          |
| 26     | 26      | 26   | 26          |
| 27     | 27      | 27   | 27          |
| 28     | 28      | 28   | 28          |
| 29     | 29      | 29   | 29          |
| 30     | 30      | 30   | 30          |
| 31     | 31      | 31   | 31          |
| 32     | 32      | 32   | 32          |
| 33     | 33      | 33   | 33          |
| 34     | 34      | 34   | 34          |
| 35     | 35      | 35   | 35          |
| 36     | 36      | 36   | 36          |
| 37     | 37      | 37   | 37          |
| 38     | 38      | 38   | 38          |
| 39     | 39      | 39   | 39          |
| 40     | 40      | 40   | 40          |
| 41     | 41      | 41   | 41          |
| 42     | 42      | 42   | 42          |
| 43     | 43      | 43   | 43          |
| 44     | 44      | 44   | 44          |
| 45     | 45      | 45   | 45          |
| 46     | 46      | 46   | 46          |
| 47     | 47      | 47   | 47          |
| 48     | 48      | 48   | 48          |
| 49     | 49      | 49   | 49          |
| 50     | 50      | 50   | 50          |
| 51     | 51      | 51   | 51          |
| 52     | 52      | 52   | 52          |
| 53     | 53      | 53   | 53          |
| 54     | 54      | 54   | 54          |
| 55     | 55      | 55   | 55          |
| 56     | 56      | 56   | 56          |
| 57     | 57      | 57   | 57          |
| 58     | 58      | 58   | 58          |
| 59     | 59      | 59   | 59          |
| 60     | 60      | 60   | 60          |
| 61     | 61      | 61   | 61          |
| 62     | 62      | 62   | 62          |
| 63     | 63      | 63   | 63          |
| 64     | 64      | 64   | 64          |
| 65     | 65      | 65   | 65          |
| 66     | 66      | 66   | 66          |
| 67     | 67      | 67   | 67          |
| 68     | 68      | 68   | 68          |
| 69     | 69      | 69   | 69          |
| 70     | 70      | 70   | 70          |
| 71     | 71      | 71   | 71          |
| 72     | 72      | 72   | 72          |
| 73     | 73      | 73   | 73          |
| 74     | 74      | 74   | 74          |
| 75     | 75      | 75   | 75          |
| 76     | 76      | 76   | 76          |
| 77     | 77      | 77   | 77          |
| 78     | 78      | 78   | 78          |
| 79     | 79      | 79   | 79          |
| 80     | 80      | 80   | 80          |
| 81     | 81      | 81   | 81          |
| 82     | 82      | 82   | 82          |
| 83     | 83      | 83   | 83          |
| 84     | 84      | 84   | 84          |
| 85     | 85      | 85   | 85          |
| 86     | 86      | 86   | 86          |
| 87     | 87      | 87   | 87          |
| 88     | 88      | 88   | 88          |
| 89     | 89      | 89   | 89          |
| 90     | 90      | 90   | 90          |
| 91     | 91      | 91   | 91          |
| 92     | 92      | 92   | 92          |
| 93     | 93      | 93   | 93          |
| 94     | 94      | 94   | 94          |
| 95     | 95      | 95   | 95          |
| 96     | 96      | 96   | 96          |
| 97     | 97      | 97   | 97          |
| 98     | 98      | 98   | 98          |
| 99     | 99      | 99   | 99          |
| 100    | 100     | 100  | 100         |

|      |      |      |      |
|------|------|------|------|
| THO  | 0.00 | ATT  | 1.00 |
| ATP  | 1.00 | ANH  | 1.00 |
| ATUL | 1.00 | HTOL | 1.00 |
| THCC | 0.00 | IRI  | 5.00 |

## H ARRAY

A 10x10 grid of circles. The patterns are as follows:

- Row 1: All circles empty.
- Row 2: All circles empty.
- Row 3: All circles empty.
- Row 4: All circles empty.
- Row 5: All circles empty.
- Row 6: All circles empty.
- Row 7: All circles empty.
- Row 8: All circles empty.
- Row 9: All circles empty.
- Row 10: All circles empty.



# GAMMA ARRAY

|          |          |         |     |     |     |     |     |     |     |
|----------|----------|---------|-----|-----|-----|-----|-----|-----|-----|
| 0.00033  | 0.0      | 0.0     | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.00181  | 0.0      | 0.0     | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.012500 | 0.0      | 0.00033 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0      | 0.0      | 0.00781 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0      | 0.0      | 0.02500 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0      | 0.0      | 0.00033 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0      | 0.00781  | 0.0     | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0      | 0.012500 | 0.0     | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |

# C ARRAY

|     |     |     |     |     |     |     |     |     |     |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |

# PP ARRAY

|               |               |               |               |               |               |               |               |               |               |
|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|
| 1000000.00000 | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           |
| 0.0           | 1000000.00000 | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           |
| 0.0           | 0.0           | 1000000.00000 | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           |
| 0.0           | 0.0           | 0.0           | 1000000.00000 | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           |
| 0.0           | 0.0           | 0.0           | 0.0           | 1000000.00000 | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           |
| 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 1000000.00000 | 0.0           | 0.0           | 0.0           | 0.0           |
| 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 1000000.00000 | 0.0           | 0.0           | 0.0           |
| 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 1000000.00000 | 0.0           | 0.0           |
| 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 1000000.00000 | 0.0           |
| 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 1000000.00000 |

# PHI ARRAY

|        |        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 1.0000 | 0.1250 | 0.0078 | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    |
| 0.0    | 1.0000 | 0.1250 | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    |
| 0.0    | 0.0    | 1.0000 | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    |
| 0.0    | 0.0    | 0.0    | 1.0000 | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    |
| 0.0    | 0.0    | 0.0    | 0.0    | 1.0000 | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    |
| 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 1.0000 | 0.0    | 0.0    | 0.0    | 0.0    |
| 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 1.0000 | 0.0    | 0.0    | 0.0    |
| 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 1.0000 | 0.0    | 0.0    |
| 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 1.0000 | 0.0    |
| 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 0.0    | 1.0000 |

# R ARRAY

|            |            |     |     |     |     |     |     |     |     |
|------------|------------|-----|-----|-----|-----|-----|-----|-----|-----|
| 955.94368  | 71.15930   | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 71.15930   | 1181.55355 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1181.55355 | -19.0      | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| -19.0      | 0.0        | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0        | 0.0        | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0        | 0.0        | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0        | 0.0        | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0        | 0.0        | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0        | 0.0        | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0        | 0.0        | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |



## OUTPUT FORMAT

[illegible]





113









115



### OUTPUT FORMAT

| X1 | X2 | X3 | X4 | X5 | X6 | PH01 | PH | XE | Y1 | Y2 | Y3 | Y4 | Y5 | Y6 | PH01 | PHI | DXE | Z1 | Z2 | Z3 | Z4 | Z5 | Z6 | Z7 | Z8 | Z9 | Z10 | Z11 | Z12 | Z13 | Z14 | Z15 | Z16 | Z17 | Z18 | Z19 | Z20 | Z21 | Z22 | Z23 | Z24 | Z25 | Z26 | Z27 | Z28 | Z29 | Z30 | Z31 | Z32 | Z33 | Z34 | Z35 | Z36 | Z37 | Z38 | Z39 | Z40 | Z41 | Z42 | Z43 | Z44 | Z45 | Z46 | Z47 | Z48 | Z49 | Z50 | Z51 | Z52 | Z53 | Z54 | Z55 | Z56 | Z57 | Z58 | Z59 | Z60 | Z61 | Z62 | Z63 | Z64 | Z65 | Z66 | Z67 | Z68 | Z69 | Z70 | Z71 | Z72 | Z73 | Z74 | Z75 | Z76 | Z77 | Z78 | Z79 | Z80 | Z81 | Z82 | Z83 | Z84 | Z85 | Z86 | Z87 | Z88 | Z89 | Z90 | Z91 | Z92 | Z93 | Z94 | Z95 | Z96 | Z97 | Z98 | Z99 | Z100 | Z101 | Z102 | Z103 | Z104 | Z105 | Z106 | Z107 | Z108 | Z109 | Z110 | Z111 | Z112 | Z113 | Z114 | Z115 | Z116 | Z117 | Z118 | Z119 | Z120 | Z121 | Z122 | Z123 | Z124 | Z125 | Z126 | Z127 | Z128 | Z129 | Z130 | Z131 | Z132 | Z133 | Z134 | Z135 | Z136 | Z137 | Z138 | Z139 | Z140 | Z141 | Z142 | Z143 | Z144 | Z145 | Z146 | Z147 | Z148 | Z149 | Z150 | Z151 | Z152 | Z153 | Z154 | Z155 | Z156 | Z157 | Z158 | Z159 | Z160 | Z161 | Z162 | Z163 | Z164 | Z165 | Z166 | Z167 | Z168 | Z169 | Z170 | Z171 | Z172 | Z173 | Z174 | Z175 | Z176 | Z177 | Z178 | Z179 | Z180 | Z181 | Z182 | Z183 | Z184 | Z185 | Z186 | Z187 | Z188 | Z189 | Z190 | Z191 | Z192 | Z193 | Z194 | Z195 | Z196 | Z197 | Z198 | Z199 | Z200 | Z201 | Z202 | Z203 | Z204 | Z205 | Z206 | Z207 | Z208 | Z209 | Z210 | Z211 | Z212 | Z213 | Z214 | Z215 | Z216 | Z217 | Z218 | Z219 | Z220 | Z221 | Z222 | Z223 | Z224 | Z225 | Z226 | Z227 | Z228 | Z229 | Z230 | Z231 | Z232 | Z233 | Z234 | Z235 | Z236 | Z237 | Z238 | Z239 | Z240 | Z241 | Z242 | Z243 | Z244 | Z245 | Z246 | Z247 | Z248 | Z249 | Z250 | Z251 | Z252 | Z253 | Z254 | Z255 | Z256 | Z257 | Z258 | Z259 | Z260 | Z261 | Z262 | Z263 | Z264 | Z265 | Z266 | Z267 | Z268 | Z269 | Z270 | Z271 | Z272 | Z273 | Z274 | Z275 | Z276 | Z277 | Z278 | Z279 | Z280 | Z281 | Z282 | Z283 | Z284 | Z285 | Z286 | Z287 | Z288 | Z289 | Z290 | Z291 | Z292 | Z293 | Z294 | Z295 | Z296 | Z297 | Z298 | Z299 | Z300 | Z301 | Z302 | Z303 | Z304 | Z305 | Z306 | Z307 | Z308 | Z309 | Z310 | Z311 | Z312 | Z313 | Z314 | Z315 | Z316 | Z317 | Z318 | Z319 | Z320 | Z321 | Z322 | Z323 | Z324 | Z325 | Z326 | Z327 | Z328 | Z329 | Z330 | Z331 | Z332 | Z333 | Z334 | Z335 | Z336 | Z337 | Z338 | Z339 | Z340 | Z341 | Z342 | Z343 | Z344 | Z345 | Z346 | Z347 | Z348 | Z349 | Z350 | Z351 | Z352 | Z353 | Z354 | Z355 | Z356 | Z357 | Z358 | Z359 | Z360 | Z361 | Z362 | Z363 | Z364 | Z365 | Z366 | Z367 | Z368 | Z369 | Z370 | Z371 | Z372 | Z373 | Z374 | Z375 | Z376 | Z377 | Z378 | Z379 | Z380 | Z381 | Z382 | Z383 | Z384 | Z385 | Z386 | Z387 | Z388 | Z389 | Z390 | Z391 | Z392 | Z393 | Z394 | Z395 | Z396 | Z397 | Z398 | Z399 | Z400 | Z401 | Z402 | Z403 | Z404 | Z405 | Z406 | Z407 | Z408 | Z409 | Z410 | Z411 | Z412 | Z413 | Z414 | Z415 | Z416 | Z417 | Z418 | Z419 | Z420 | Z421 | Z422 | Z423 | Z424 | Z425 | Z426 | Z427 | Z428 | Z429 | Z430 | Z431 | Z432 | Z433 | Z434 | Z435 | Z436 | Z437 | Z438 | Z439 | Z440 | Z441 | Z442 | Z443 | Z444 | Z445 | Z446 | Z447 | Z448 | Z449 | Z450 | Z451 | Z452 | Z453 | Z454 | Z455 | Z456 | Z457 | Z458 | Z459 | Z460 | Z461 | Z462 | Z463 | Z464 | Z465 | Z466 | Z467 | Z468 | Z469 | Z470 | Z471 | Z472 | Z473 | Z474 | Z475 | Z476 | Z477 | Z478 | Z479 | Z480 | Z481 | Z482 | Z483 | Z484 | Z485 | Z486 | Z487 | Z488 | Z489 | Z490 | Z491 | Z492 | Z493 | Z494 | Z495 | Z496 | Z497 | Z498 | Z499 | Z500 | Z501 | Z502 | Z503 | Z504 | Z505 | Z506 | Z507 | Z508 | Z509 | Z510 | Z511 | Z512 | Z513 | Z514 | Z515 | Z516 | Z517 | Z518 | Z519 | Z520 | Z521 | Z522 | Z523 | Z524 | Z525 | Z526 | Z527 | Z528 | Z529 | Z530 | Z531 | Z532 | Z533 | Z534 | Z535 | Z536 | Z537 | Z538 | Z539 | Z540 | Z541 | Z542 | Z543 | Z544 | Z545 | Z546 | Z547 | Z548 | Z549 | Z550 | Z551 | Z552 | Z553 | Z554 | Z555 | Z556 | Z557 | Z558 | Z559 | Z560 | Z561 | Z562 | Z563 | Z564 | Z565 | Z566 | Z567 | Z568 | Z569 | Z570 | Z571 | Z572 | Z573 | Z574 | Z575 | Z576 | Z577 | Z578 | Z579 | Z580 | Z581 | Z582 | Z583 | Z584 | Z585 | Z586 | Z587 | Z588 | Z589 | Z590 | Z591 | Z592 | Z593 | Z594 | Z595 | Z596 | Z597 | Z598 | Z599 | Z600 | Z601 | Z602 | Z603 | Z604 | Z605 | Z606 | Z607 | Z608 | Z609 | Z610 | Z611 | Z612 | Z613 | Z614 | Z615 | Z616 | Z617 | Z618 | Z619 | Z620 | Z621 | Z622 | Z623 | Z624 | Z625 | Z626 | Z627 | Z628 | Z629 | Z630 | Z631 | Z632 | Z633 | Z634 | Z635 | Z636 | Z637 | Z638 | Z639 | Z640 | Z641 | Z642 | Z643 | Z644 | Z645 | Z646 | Z647 | Z648 | Z649 | Z650 | Z651 | Z652 | Z653 | Z654 | Z655 | Z656 | Z657 | Z658 | Z659 | Z660 | Z661 | Z662 | Z663 | Z664 | Z665 | Z666 | Z667 | Z668 | Z669 | Z670 | Z671 | Z672 | Z673 | Z674 | Z675 | Z676 | Z677 | Z678 | Z679 | Z680 | Z681 | Z682 | Z683 | Z684 | Z685 | Z686 | Z687 | Z688 | Z689 | Z690 | Z691 | Z692 | Z693 | Z694 | Z695 | Z696 | Z697 | Z698 | Z699 | Z700 | Z701 | Z702 | Z703 | Z704 | Z705 | Z706 | Z707 | Z708 | Z709 | Z710 | Z711 | Z712 | Z713 | Z714 | Z715 | Z716 | Z717 | Z718 | Z719 | Z720 | Z721 | Z722 | Z723 | Z724 | Z725 | Z726 | Z727 | Z728 | Z729 | Z730 | Z731 | Z732 | Z733 | Z734 | Z735 | Z736 | Z737 | Z738 | Z739 | Z740 | Z741 | Z742 | Z743 | Z744 | Z745 | Z746 | Z747 | Z748 | Z749 | Z750 | Z751 | Z752 | Z753 | Z754 | Z755 | Z756 | Z757 | Z758 | Z759 | Z760 | Z761 | Z762 | Z763 | Z764 | Z765 | Z766 | Z767 | Z768 | Z769 | Z770 | Z771 | Z772 | Z773 | Z774 | Z775 | Z776 | Z777 | Z778 | Z779 | Z780 | Z781 | Z782 | Z783 | Z784 | Z785 | Z786 | Z787 | Z788 | Z789 | Z790 | Z791 | Z792 | Z793 | Z794 | Z795 | Z796 | Z797 | Z798 | Z799 | Z800 | Z801 | Z802 | Z803 | Z804 | Z805 | Z806 | Z807 | Z808 | Z809 | Z810 | Z811 | Z812 | Z813 | Z814 | Z815 | Z816 | Z817 | Z818 | Z819 | Z820 | Z821 | Z822 | Z823 | Z824 | Z825 | Z826 | Z827 | Z828 | Z829 | Z830 | Z831 | Z832 | Z833 | Z834 | Z835 | Z836 | Z837 | Z838 | Z839 | Z840 | Z841 | Z842 | Z843 | Z844 | Z845 | Z846 | Z847 | Z848 | Z849 | Z850 | Z851 | Z852 | Z853 | Z854 | Z855 | Z856 | Z857 | Z858 | Z859 | Z860 | Z861 | Z862 | Z863 | Z864 | Z865 | Z866 | Z867 | Z868 | Z869 | Z870 | Z871 | Z872 | Z873 | Z874 | Z875 | Z876 | Z877 | Z878 | Z879 | Z880 | Z881 | Z882 | Z883 | Z884 | Z885 | Z886 | Z887 | Z888 | Z889 | Z890 | Z891 | Z892 | Z893 | Z894 | Z895 | Z896 | Z897 | Z898 | Z899 | Z900 | Z901 | Z902 | Z903 | Z904 | Z905 | Z906 | Z907 | Z908 | Z909 | Z910 | Z911 | Z912 | Z913 | Z914 | Z915 | Z916 | Z917 | Z918 | Z919 | Z920 | Z921 | Z922 | Z923 | Z924 | Z925 | Z926 | Z927 | Z928 | Z929 | Z930 | Z931 | Z932 | Z933 | Z934 | Z935 | Z936 | Z937 | Z938 | Z939 | Z940 | Z941 | Z942 | Z943 | Z944 | Z945 | Z946 | Z947 | Z948 | Z949 | Z950 | Z951 | Z952 | Z953 | Z954 | Z955 | Z956 | Z957 | Z958 | Z959 | Z960 | Z961 | Z962 | Z963 | Z964 | Z965 | Z966 | Z967 | Z968 | Z969 | Z970 | Z971 | Z972 | Z973 | Z974 | Z975 | Z976 | Z977 | Z978 | Z979 | Z980 | Z981 | Z982 | Z983 | Z984 | Z985 | Z986 | Z987 | Z988 | Z989 | Z990 | Z991 | Z992 | Z993 | Z994 | Z995 | Z996 | Z997 | Z998 | Z999 | Z1000 | Z1001 | Z1002 | Z1003 | Z1004 | Z1005 | Z1006 | Z1007 | Z1008 | Z1009 | Z1010 | Z1011 | Z1012 | Z1013 | Z1014 | Z1015 | Z1016 | Z1017 | Z1018 | Z1019 | Z1020 | Z1021 | Z1022 | Z1023 | Z1024 | Z1025 | Z1026 | Z1027 | Z1028 | Z1029 | Z1030 | Z1031 | Z1032 | Z1033 | Z1034 | Z1035 | Z1036 | Z1037 | Z1038 | Z1039 | Z1040 | Z1041 | Z1042 | Z1043 | Z1044 | Z1045 | Z1046 | Z1047 | Z1048 | Z1049 | Z1050 | Z1051 | Z1052 | Z1053 | Z1054 | Z1055 | Z1056 | Z1057 | Z1058 | Z1059 | Z1060 | Z1061 | Z1062 | Z1063 | Z1064 | Z1065 | Z1066 | Z1067 | Z1068 | Z1069 | Z1070 | Z1071 | Z1072 | Z1073 | Z1074 | Z1075 | Z1076 | Z1077 | Z1078 | Z1079 | Z1080 | Z1081 | Z1082 | Z1083 | Z1084 | Z1085 | Z1086 | Z1087 | Z1088 | Z1089 | Z1090 | Z1091 | Z1092 | Z1093 | Z1094 | Z1095 | Z1096 | Z1097 | Z1098 | Z1099 | Z1100 | Z1101 | Z1102 | Z1103 | Z1104 | Z1105 | Z1106 | Z1107 | Z1108 | Z1109 | Z1110 | Z1111 | Z1112 | Z1113 | Z1114 | Z1115 | Z1116 | Z1117 | Z1118 | Z1119 | Z1120 | Z1121 | Z1122 | Z1123 | Z1124 | Z1125 | Z1126 | Z1127 | Z1128 | Z1129 | Z1130 | Z1131 | Z1132 | Z1133 | Z1134 | Z1135 | Z1136 | Z1137 | Z1138 | Z1139 | Z1140 | Z1141 | Z1142 | Z1143 | Z1144 | Z1145 | Z1146 | Z1147 | Z1148 | Z1149 | Z1150 | Z1151 | Z1152 | Z1153 | Z1154 | Z1155 | Z1156 | Z1157 | Z1158 | Z1159 | Z1160 | Z1161 | Z1162 | Z1163 | Z1164 | Z1165 | Z1166 | Z1167 | Z1168 | Z1169 | Z1170 | Z1171 | Z1172 | Z1173 | Z1174 | Z1175 | Z1176 | Z1177 | Z1178 | Z1179 | Z1180 | Z1181 | Z1182 | Z1183 | Z1184 | Z1185 | Z1186 | Z1187 | Z1188 | Z1189 | Z1190 | Z1191 | Z1192 | Z1193 | Z1194 | Z1195 | Z1196 | Z1197 | Z1198 | Z1199 | Z1200 | Z1201 | Z1202 | Z1203 | Z1204 | Z1205 | Z1206 | Z1207 | Z1208 | Z1209 | Z1210 | Z1211 | Z1212 | Z1213 | Z1214 | Z1215 | Z1216 | Z1217 | Z1218 | Z1219 | Z1220 | Z1221 | Z1222 | Z1223 | Z1224 | Z1225 | Z1226 | Z1227 | Z1228 | Z1229 | Z1230 | Z1231 | Z1232 | Z1233 | Z1234 | Z1235 | Z1236 | Z1237 | Z1238 | Z1239 | Z1240 | Z1241 | Z1242 | Z1243 | Z1244 | Z1245 | Z1246 | Z1247 | Z1248 | Z1249 | Z1250 | Z1251 | Z1252 | Z1253 | Z1254 | Z1255 | Z1256 | Z1257 | Z1258 | Z1259 | Z1260 | Z1261 | Z1262 | Z1263 | Z1264 | Z1265 | Z1266 | Z1267 | Z1268 | Z1269 | Z1270 | Z1271 | Z1272 | Z1273 | Z1274 | Z1275 | Z1276 | Z1277 | Z1278 | Z1279 | Z1280 | Z1281 | Z1282 | Z1283 | Z1284 | Z1285 | Z1286 | Z1287 | Z1288 | Z1289 | Z1290 | Z1291 | Z1292 | Z1293 | Z1294 | Z1295 | Z1296 | Z1297 | Z1298 | Z1299 | Z1300 | Z1301 | Z1302 | Z1303 | Z1304 | Z1305 | Z1306 | Z1307 | Z1308 | Z1309 | Z1310 | Z1311 | Z1312 | Z1313 | Z1314 | Z1315 | Z1316 | Z1317 | Z1318 | Z1319 | Z1320 | Z1321 | Z1322 | Z1323 | Z1324 | Z1325 | Z1326 | Z1327 | Z1328 | Z1329 | Z1330 | Z1331 | Z1332 | Z1333 | Z1334 | Z1335 | Z1336 | Z1337 | Z1338 | Z1339 | Z1340 | Z1341 | Z1342 | Z1343 | Z1344 | Z1345 | Z1346 | Z1347 | Z1348 | Z1349 | Z1350 | Z1351 | Z1352 | Z1353 | Z1354 | Z1355 | Z1356 | Z1357 | Z1358 | Z1359 | Z1360 | Z1361 | Z1362 | Z1363 | Z1364 | Z1365 | Z1366 | Z1367 | Z1368 | Z1369 | Z1370 | Z1371 | Z1372 | Z1373 | Z1374 | Z1375 | Z1376 | Z1377 | Z1378 | Z1379 | Z1380 | Z1381 | Z1382 | Z1383 | Z1384 | Z1385 | Z1386 | Z1387 | Z1388 | Z1389 | Z1390 | Z1391 | Z1392 | Z1393 | Z1394 | Z1395 | Z1396 | Z1397 | Z1398 | Z1399 | Z1400 | Z1401 | Z1402 | Z1403 | Z1404 | Z1405 | Z1406 | Z1407 | Z1408 | Z1409 | Z1410 | Z1411 | Z1412 | Z1413 | Z1414 | Z1415 | Z1416 | Z1417 | Z1418 | Z1419 | Z1420 | Z1421 | Z1422 | Z1423 | Z1424 | Z1425 | Z1426 | Z1427 | Z1428 | Z1429 | Z1430 | Z1431 | Z1432 | Z1433 | Z1434 | Z1435 | Z1436 | Z1437 | Z1438 | Z1439 | Z1440 | Z1441 | Z1442 | Z1443 | Z1444 | Z1445 | Z1446 | Z1447 | Z1448 | Z1449 | Z1450 | Z1451 | Z1452 | Z1453 | Z1454 | Z1455 | Z1456 | Z1457 | Z1458 | Z1459 | Z1460 | Z1461 | Z1462 | Z1463 | Z1464 | Z1465 | Z1466 | Z1467 | Z1468 | Z1469 | Z1470 | Z1471 | Z1472 | Z1473 | Z1474 | Z1475 | Z1476 | Z1477 | Z1478 | Z1479 | Z1480 | Z1481 | Z1482 | Z1483 | Z1484 | Z1485 | Z |
|----|----|----|----|----|----|------|----|----|----|----|----|----|----|----|------|-----|-----|----|----|----|----|----|----|----|----|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|
|----|----|----|----|----|----|------|----|----|----|----|----|----|----|----|------|-----|-----|----|----|----|----|----|----|----|----|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|





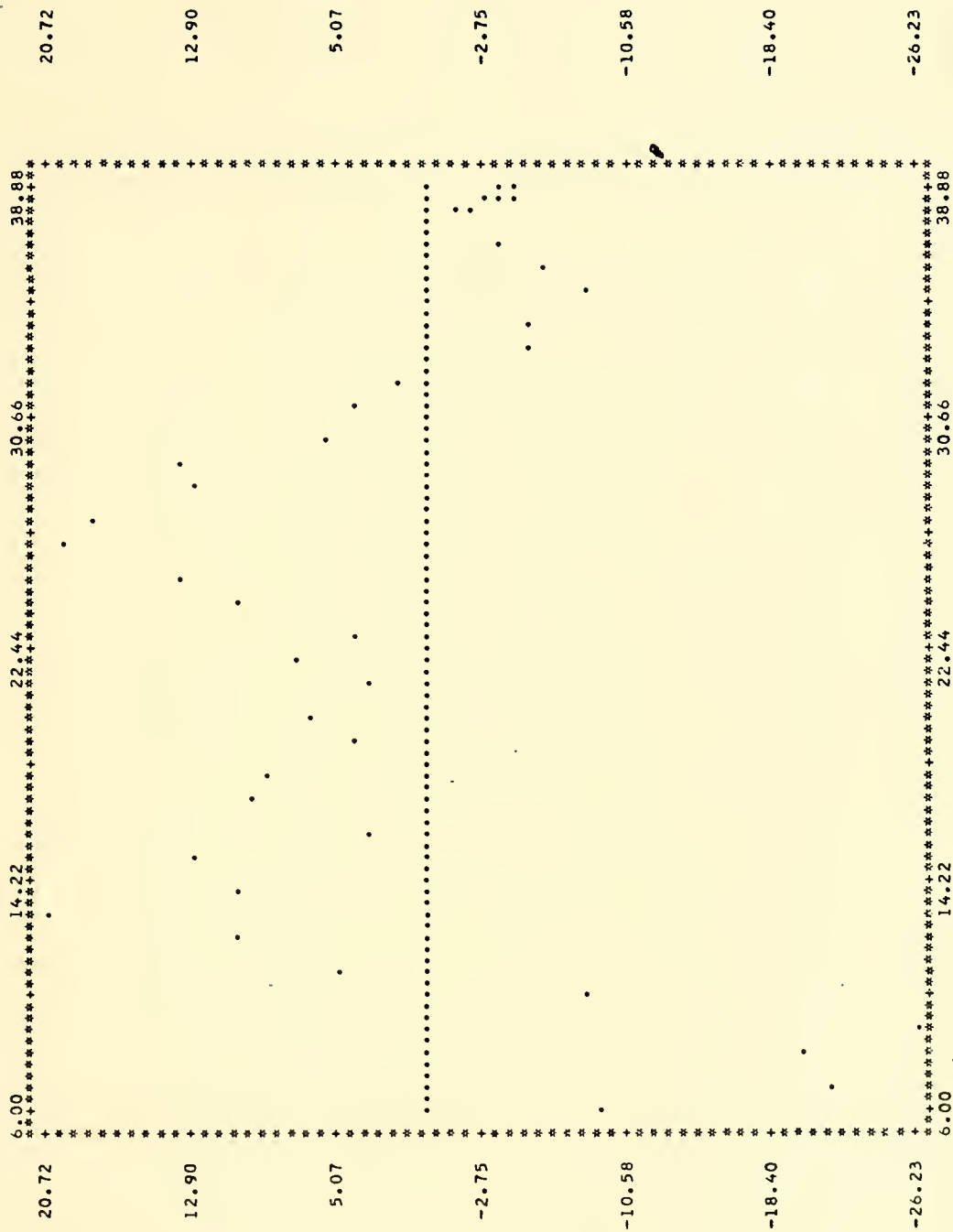
[illegible]
$$x_1 = 2.978490 \quad 01 \quad y_1 = -4.080130 \quad 00 \quad q_1 = 3.006310 \quad 01$$

AVG X RESIDUAL = 13.5116      AVG Y RESIDUAL = 4.4865      AVG Z RESIDUAL = 10.6162

AVG RADIAL FESIOUAL = 17.7594



X RESIDUAL VS. T  
LENTZ AN/TPQ-27

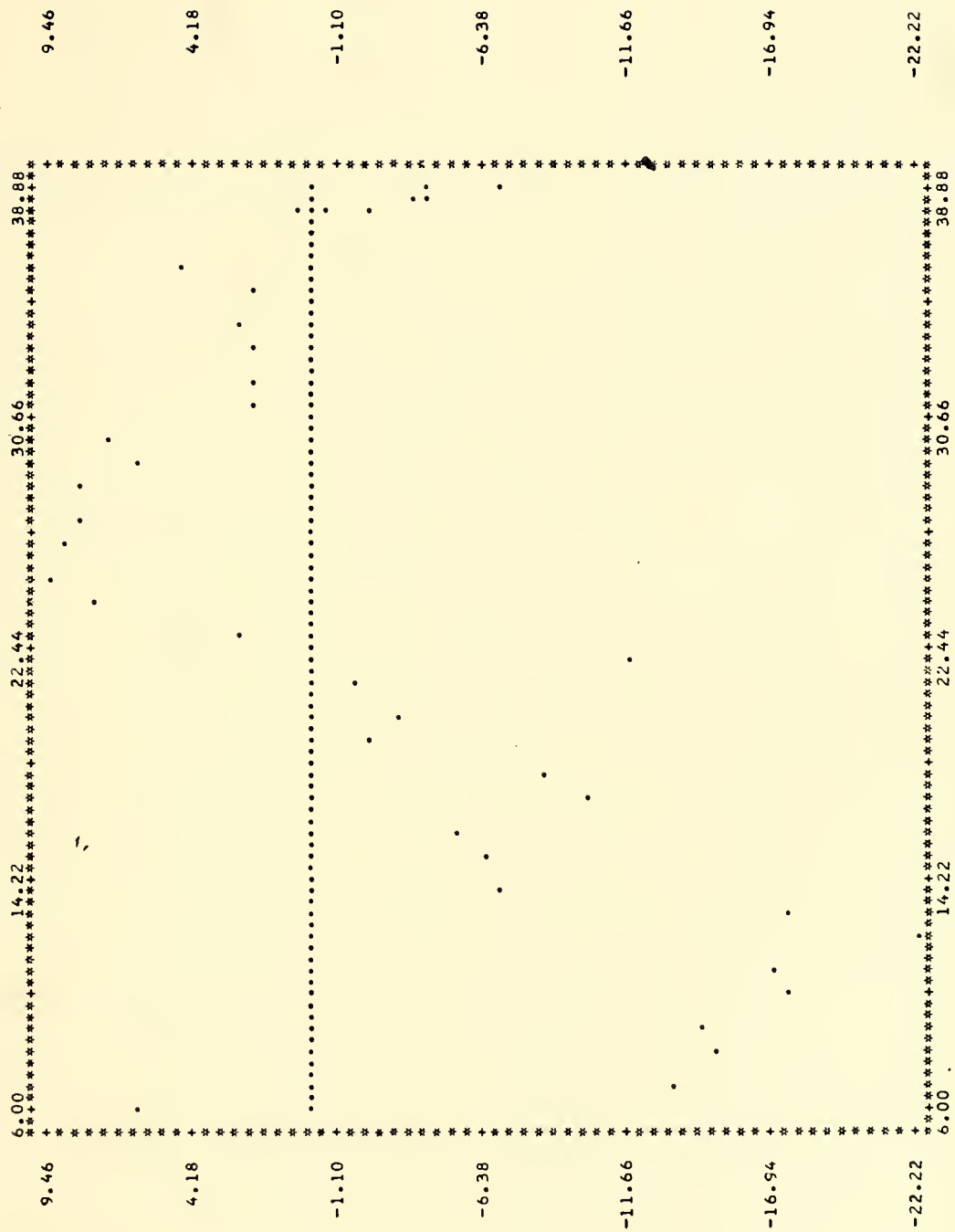








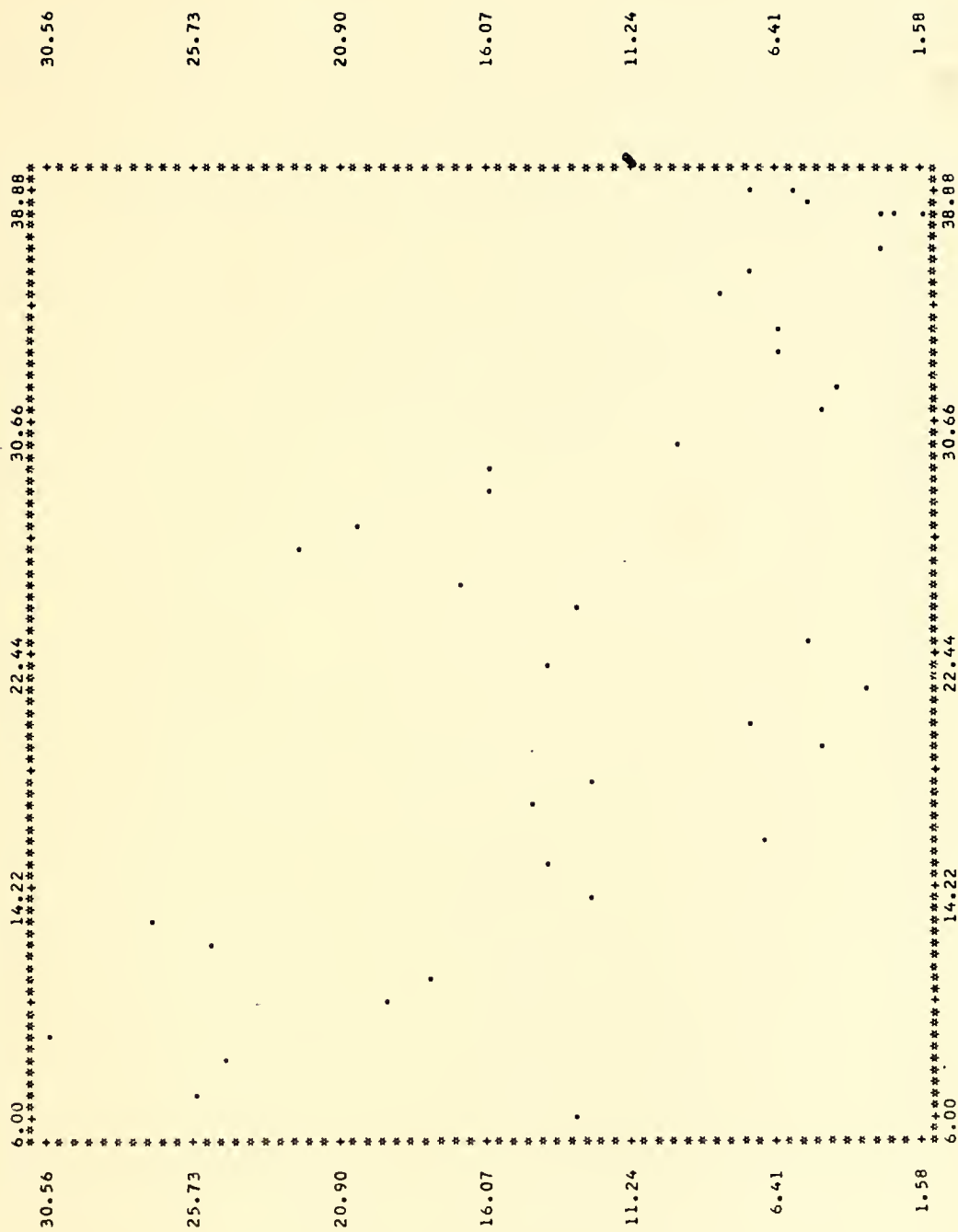
Z RESIDUAL VS. T  
LENTZ AN/TPQ-27





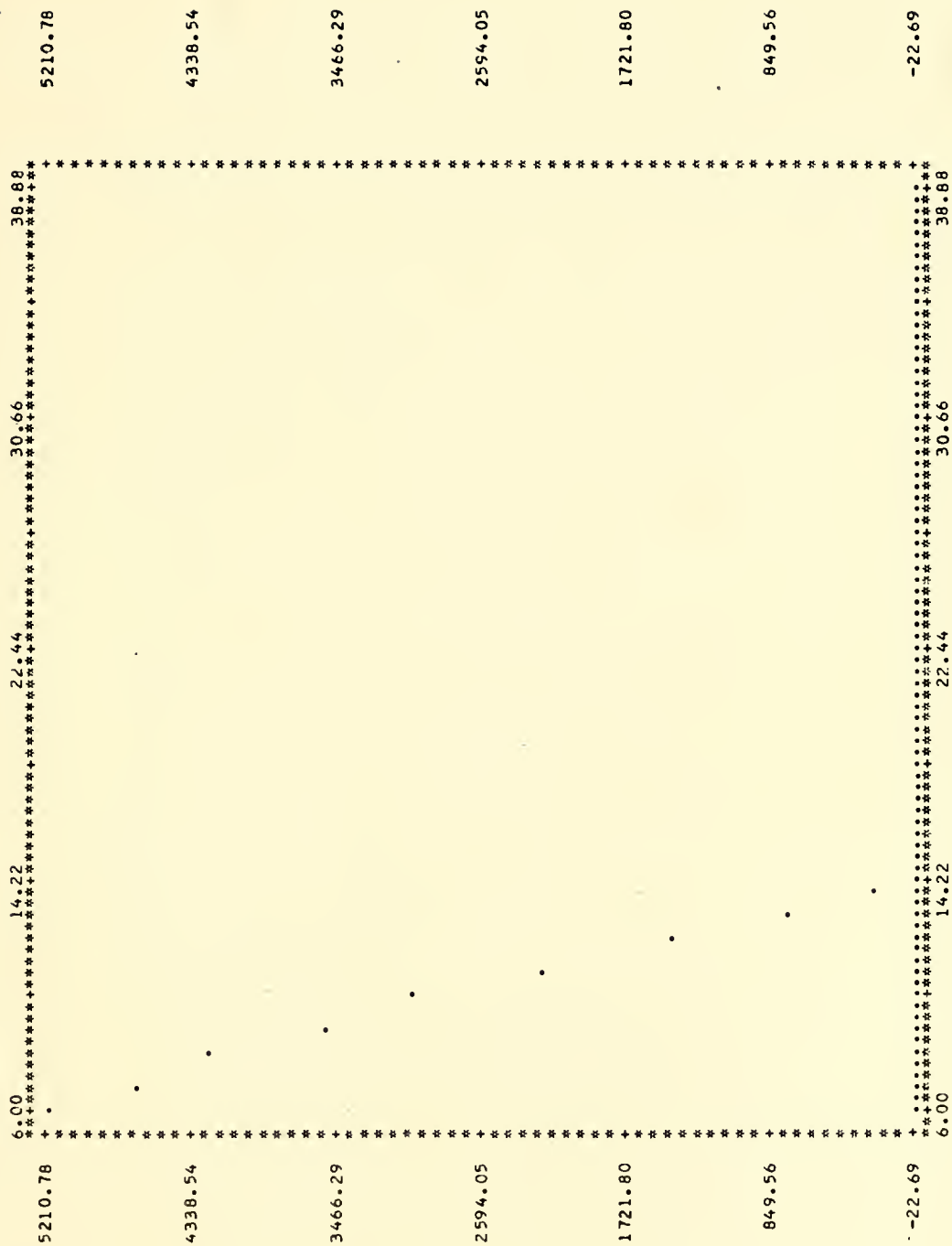


RADIAL RESIDUAL VS. T  
LENTZ AN/T00-27





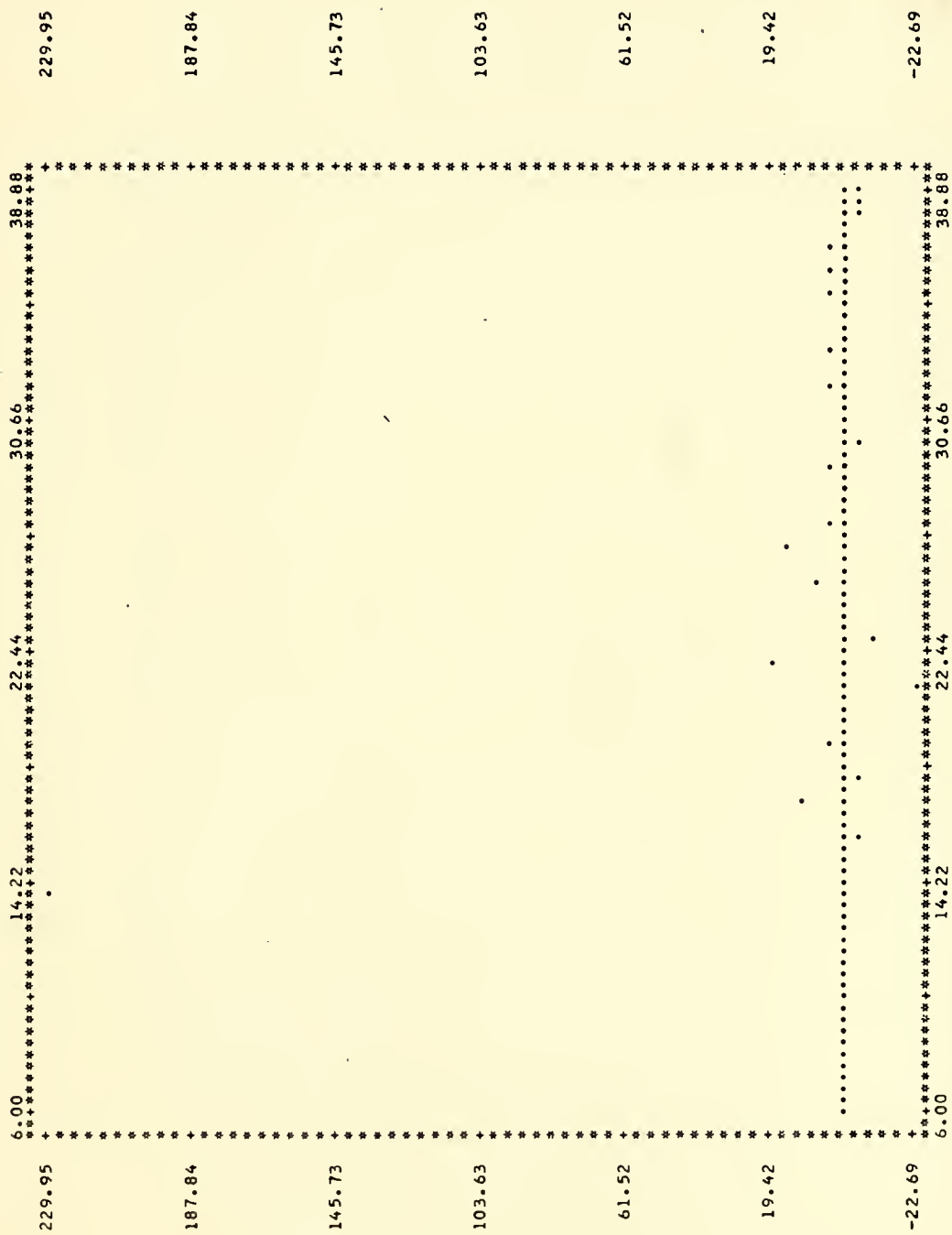
LATERAL ERROR (XE) VS. T  
LENTZ AN/TPQ-27





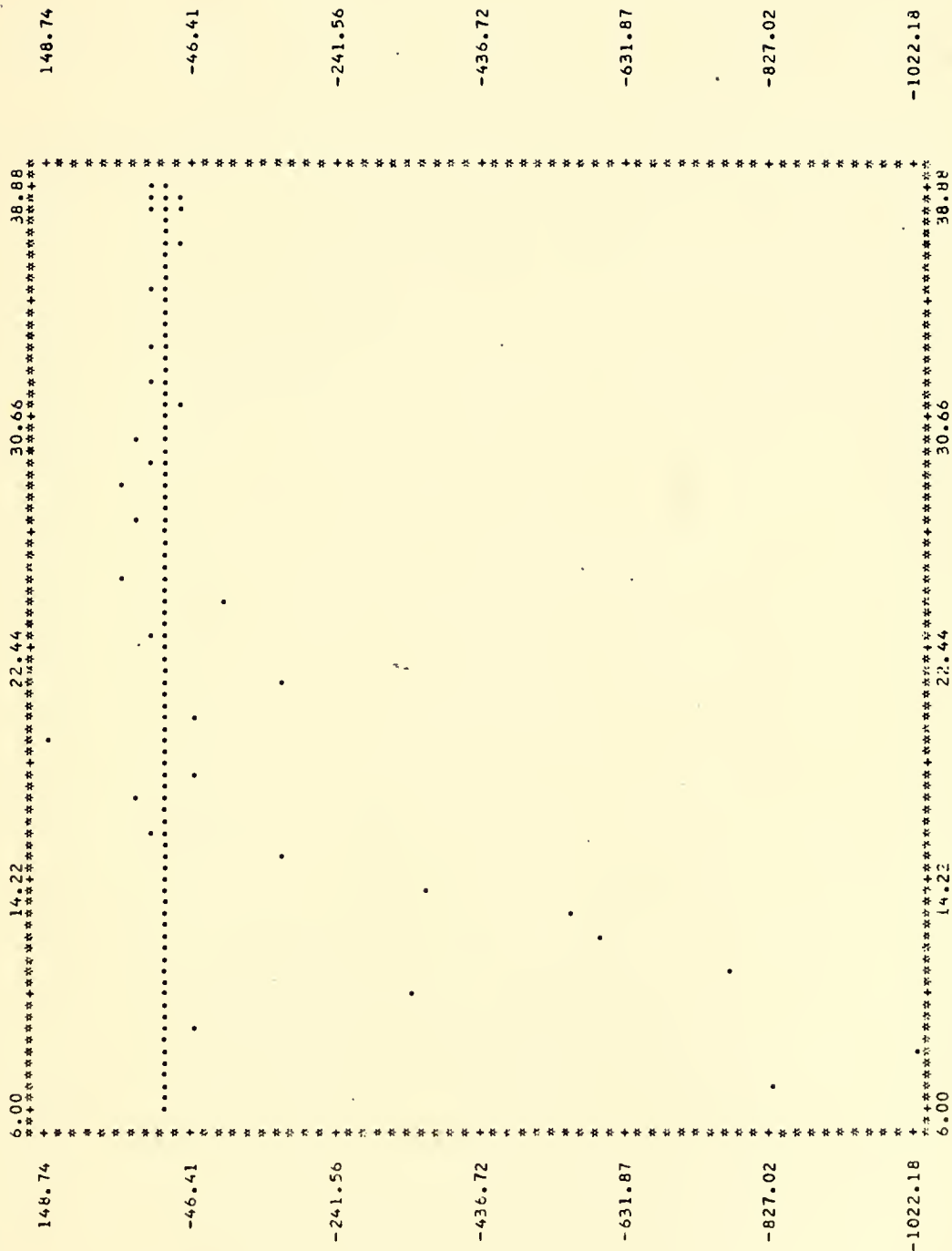
# LATERAL ERROR (EXPANDED SCALE) VS. T

LENTZ AN/TPQ-27





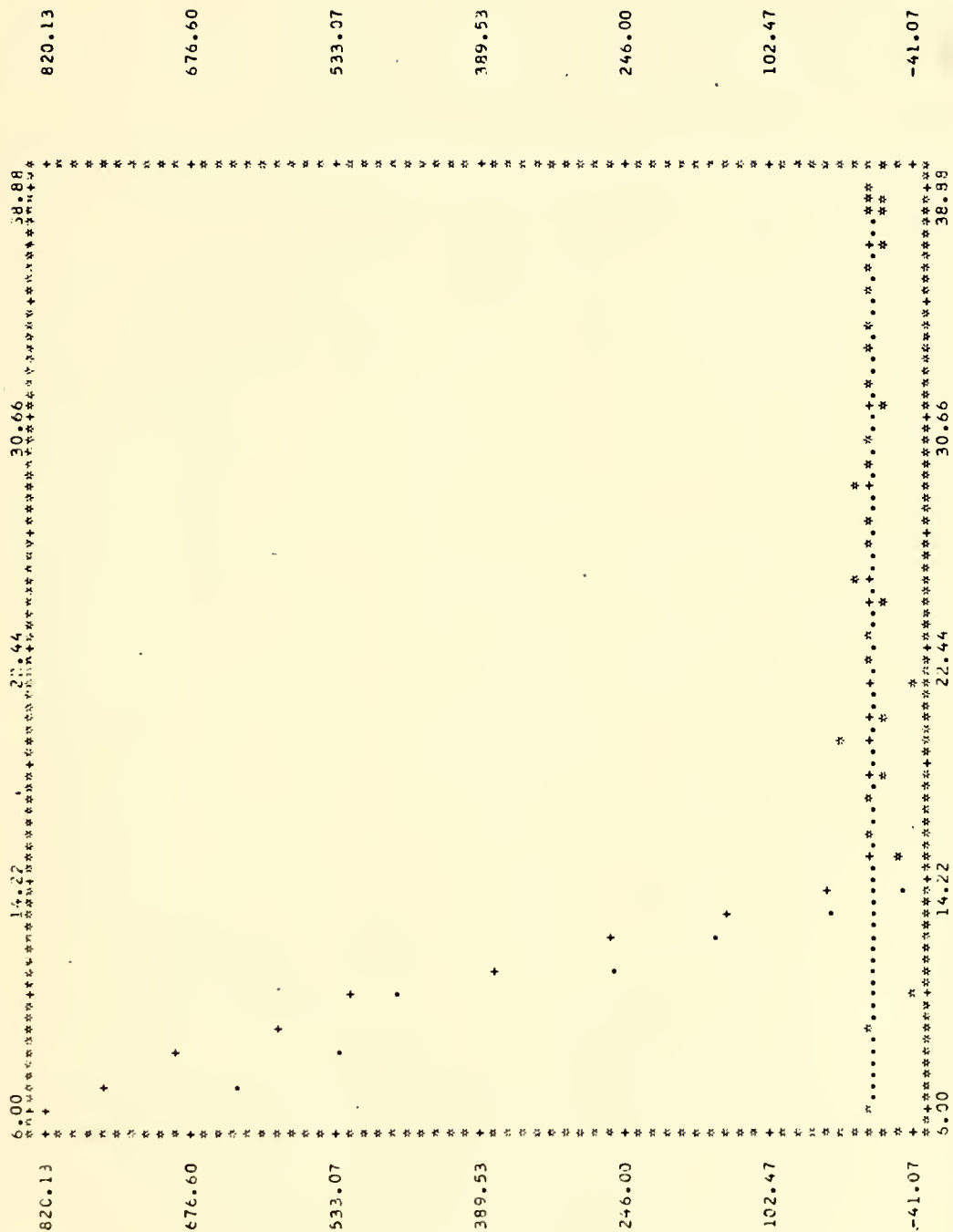
LATERAL ERROR RATE (DXE) VS. T  
LENTZ AN/TPQ-27





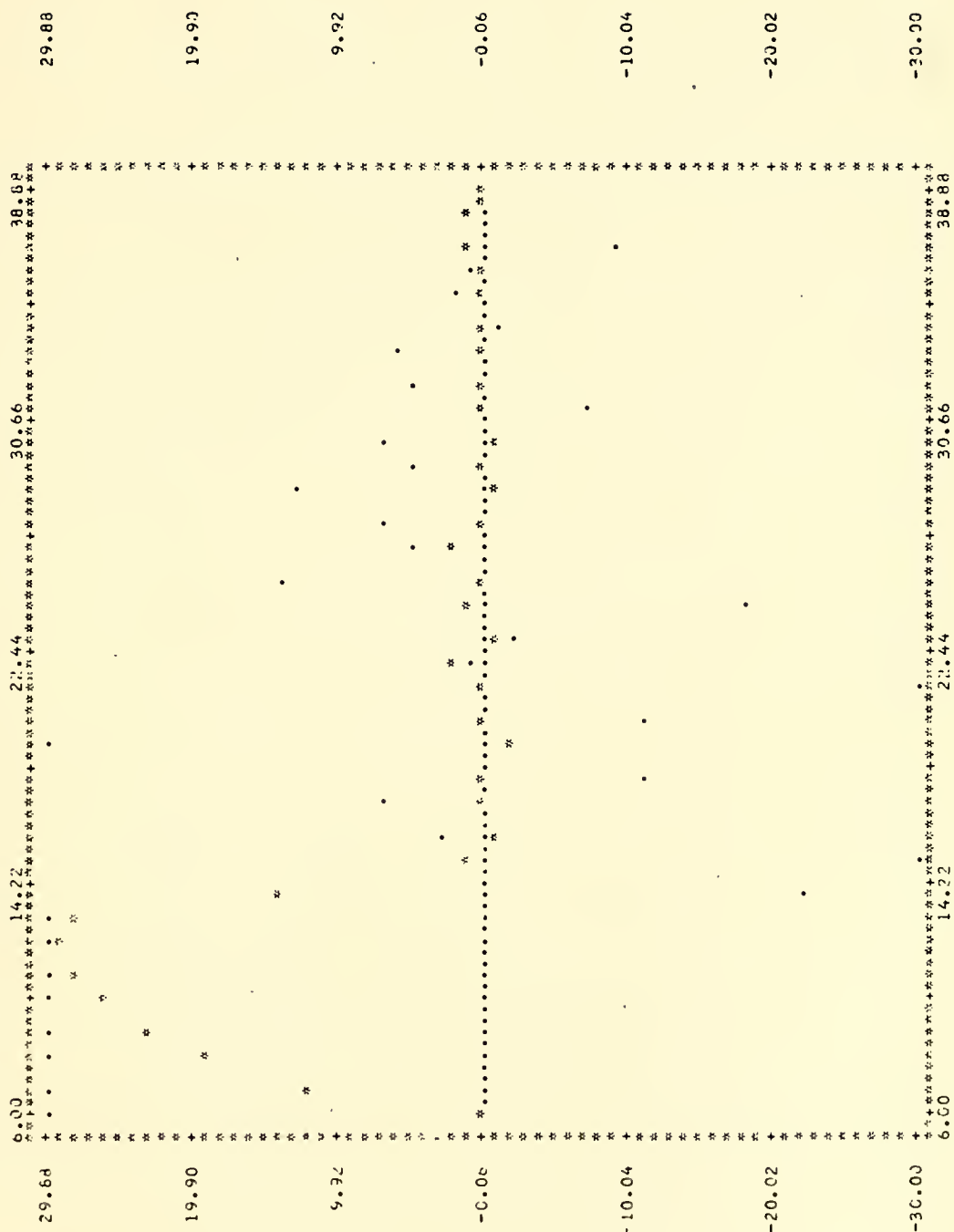


PH0,PH01, AND PH02 VS. T  
LENTZ AN/TP0-27



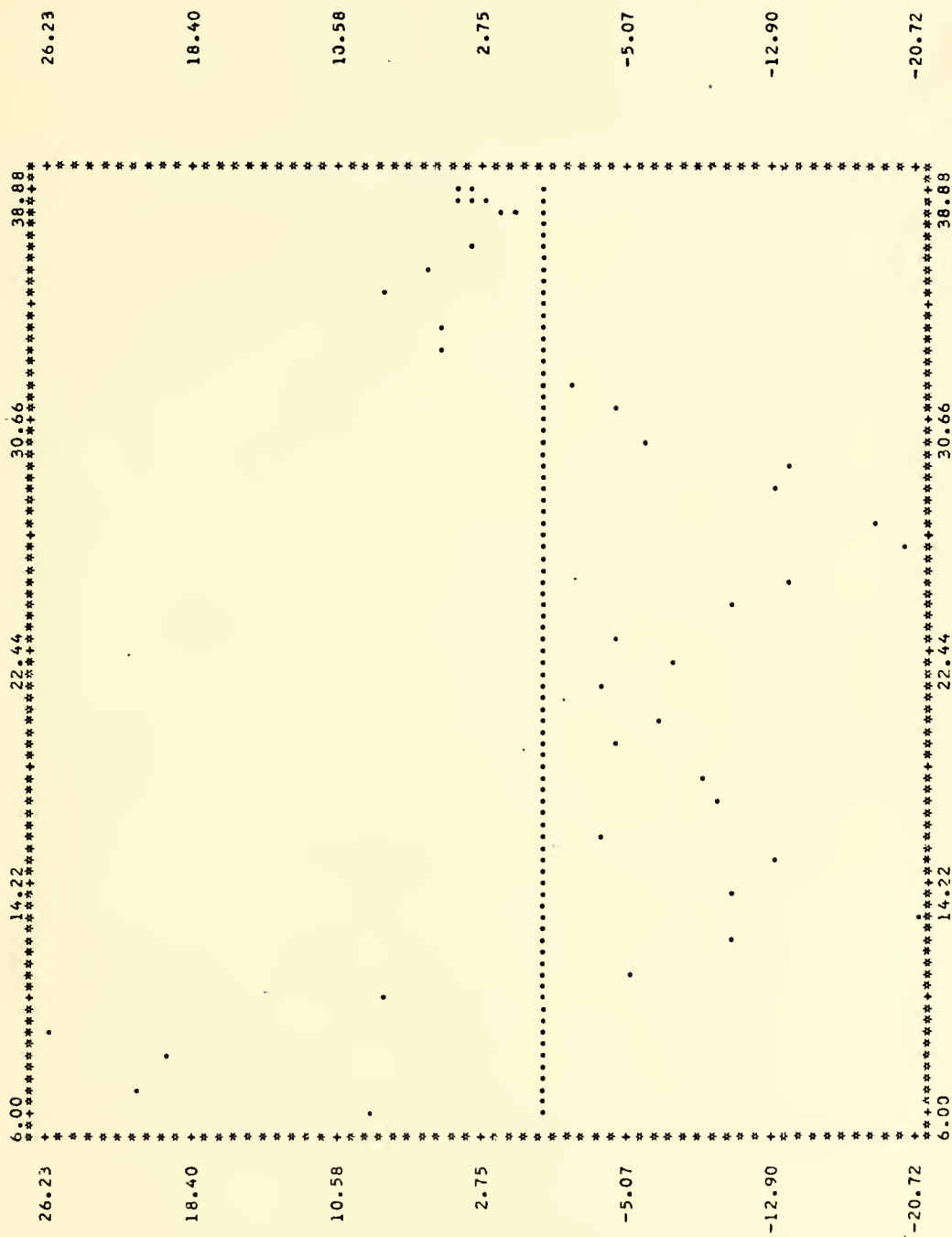


ROLL ANGLE (COMMAND, ACTUAL, RECT) VS. T  
LENTZ AN/TPQ-27



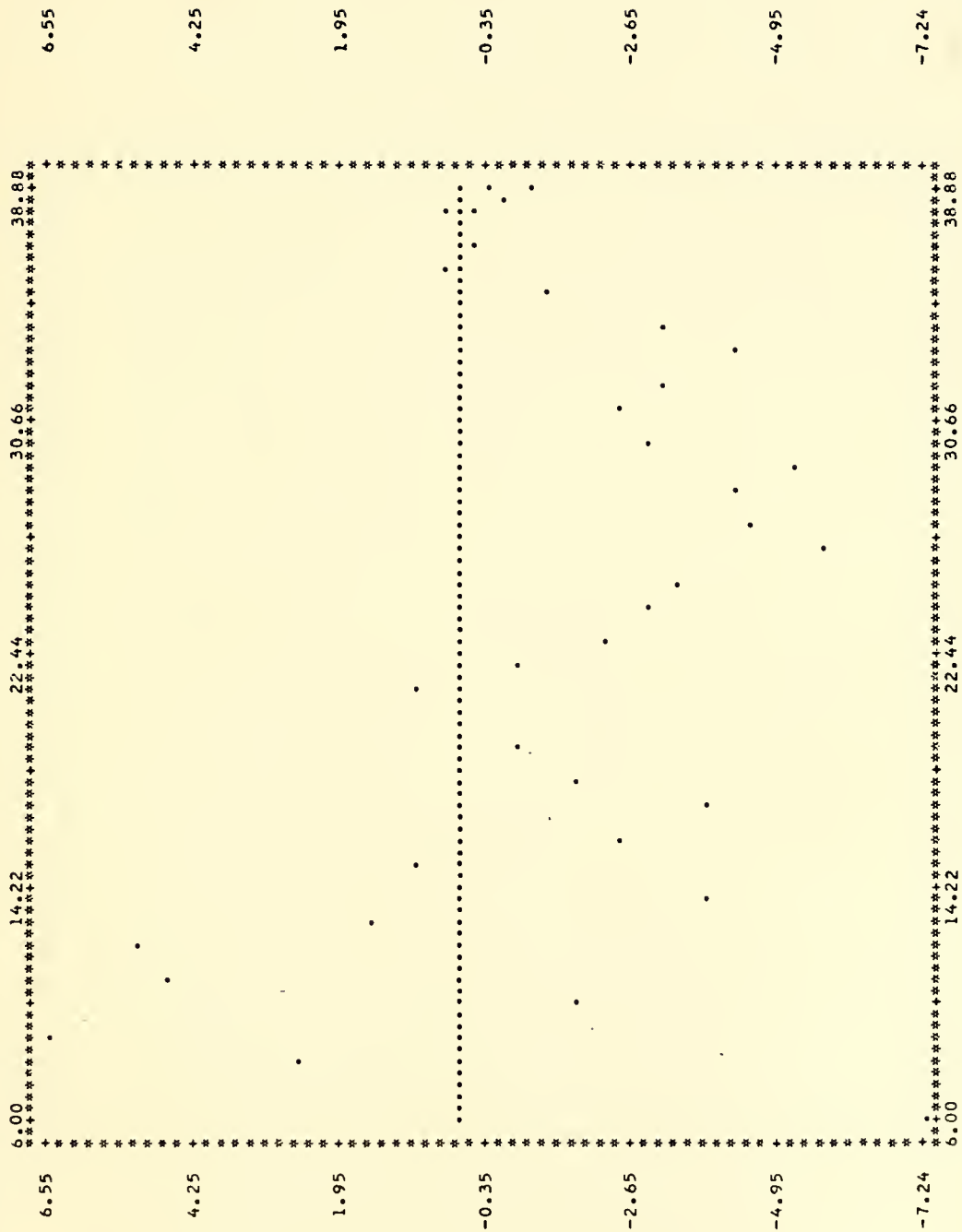


X6(1) VS. T  
LENTZ AN/TPQ-27





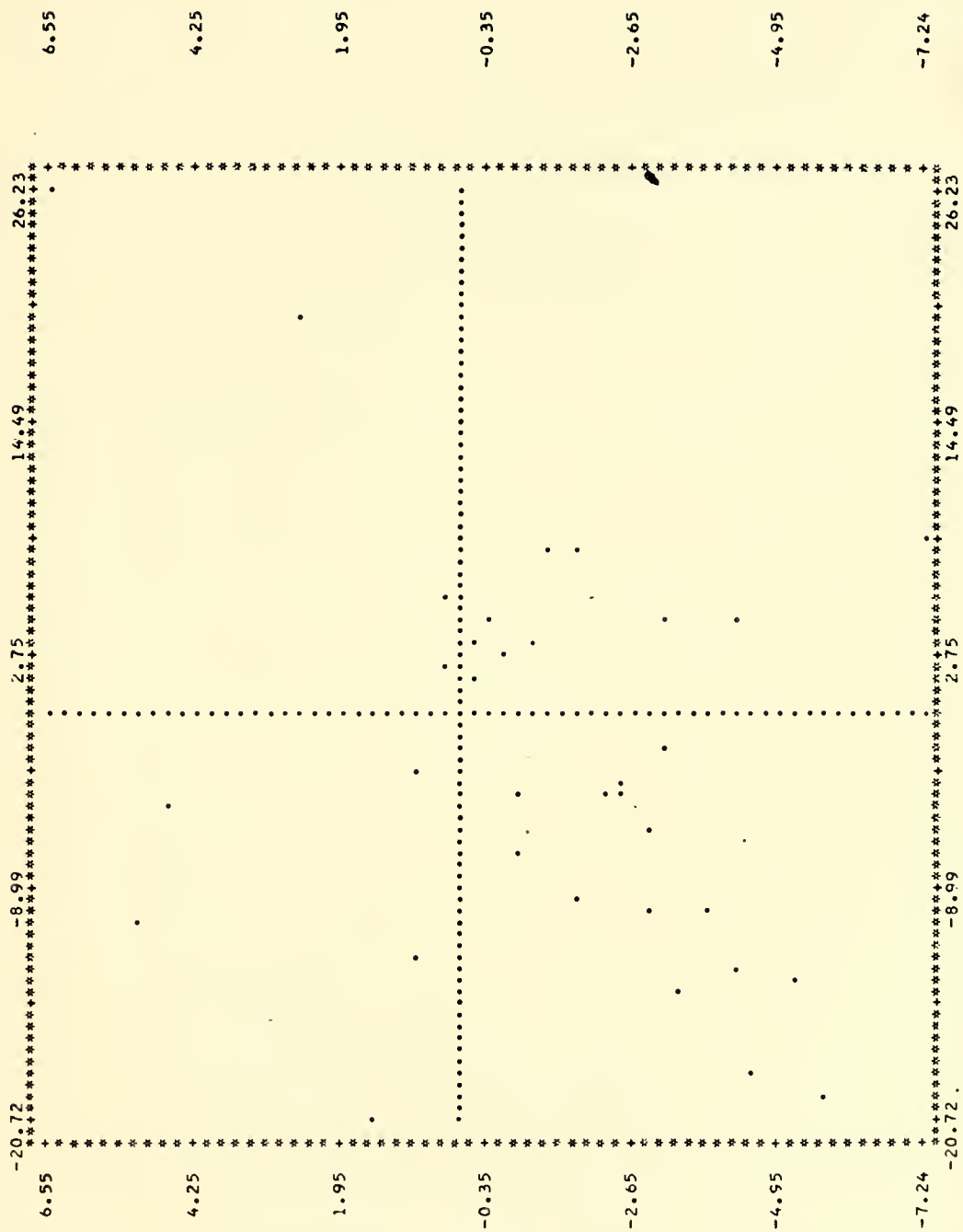
X6121 VS.  $\tau$   
LENTZ AN/TPQ-27





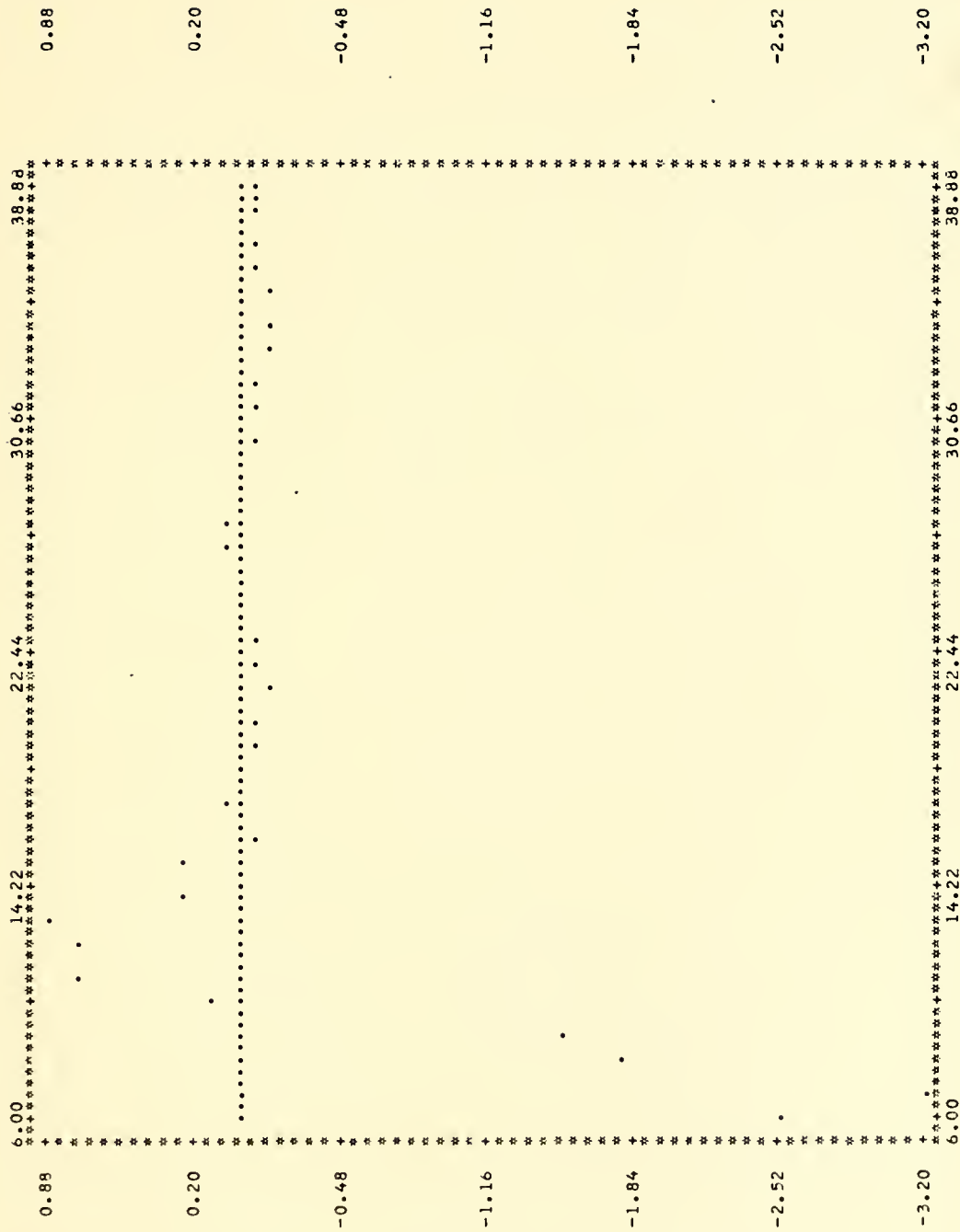


X6(12) VS. X6(1)  
LENTZ AN/TPQ-27



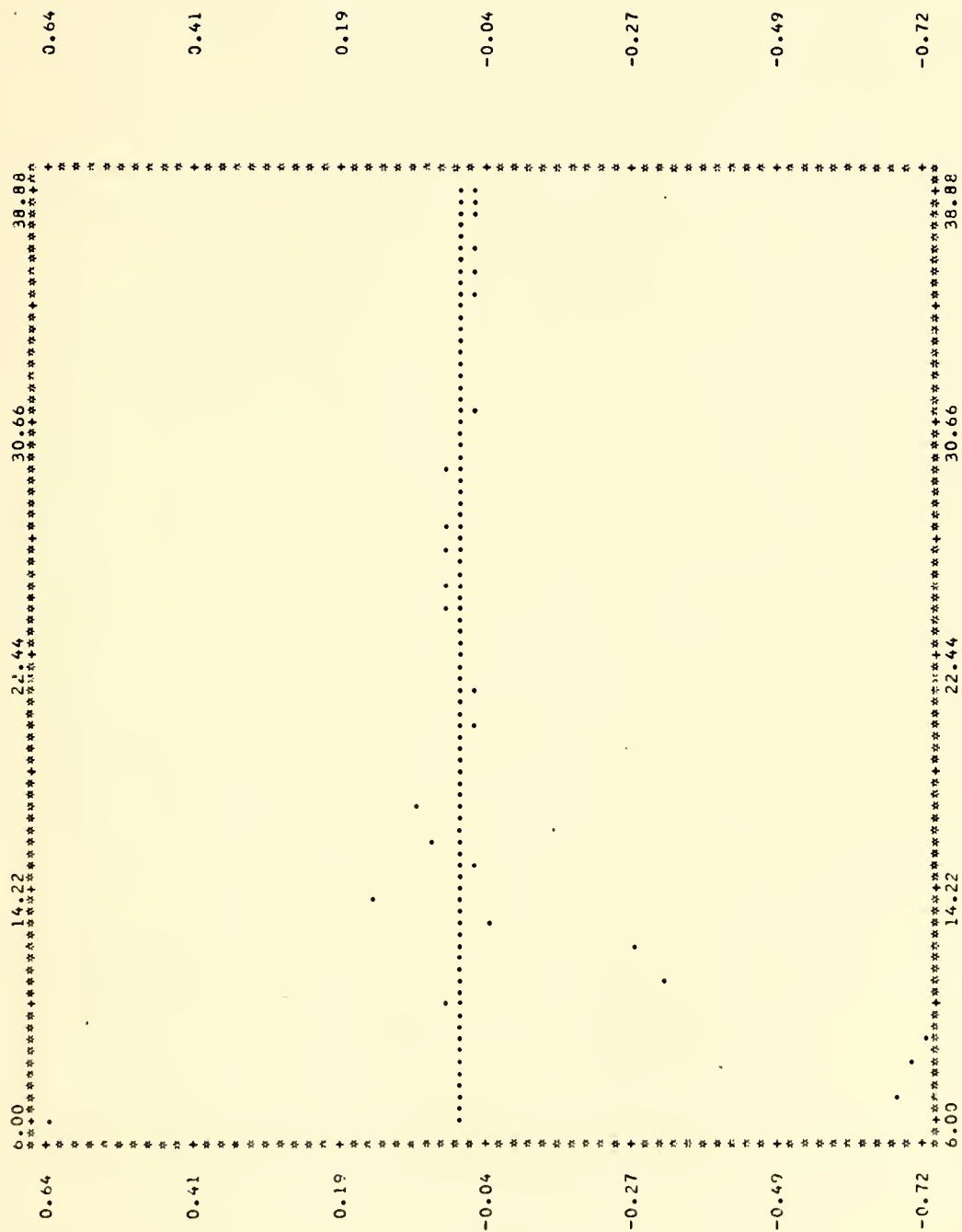


X ACCELERATION ESTIMATE(XDDI(1)) VS. T  
LENTZ AN/TPQ-27



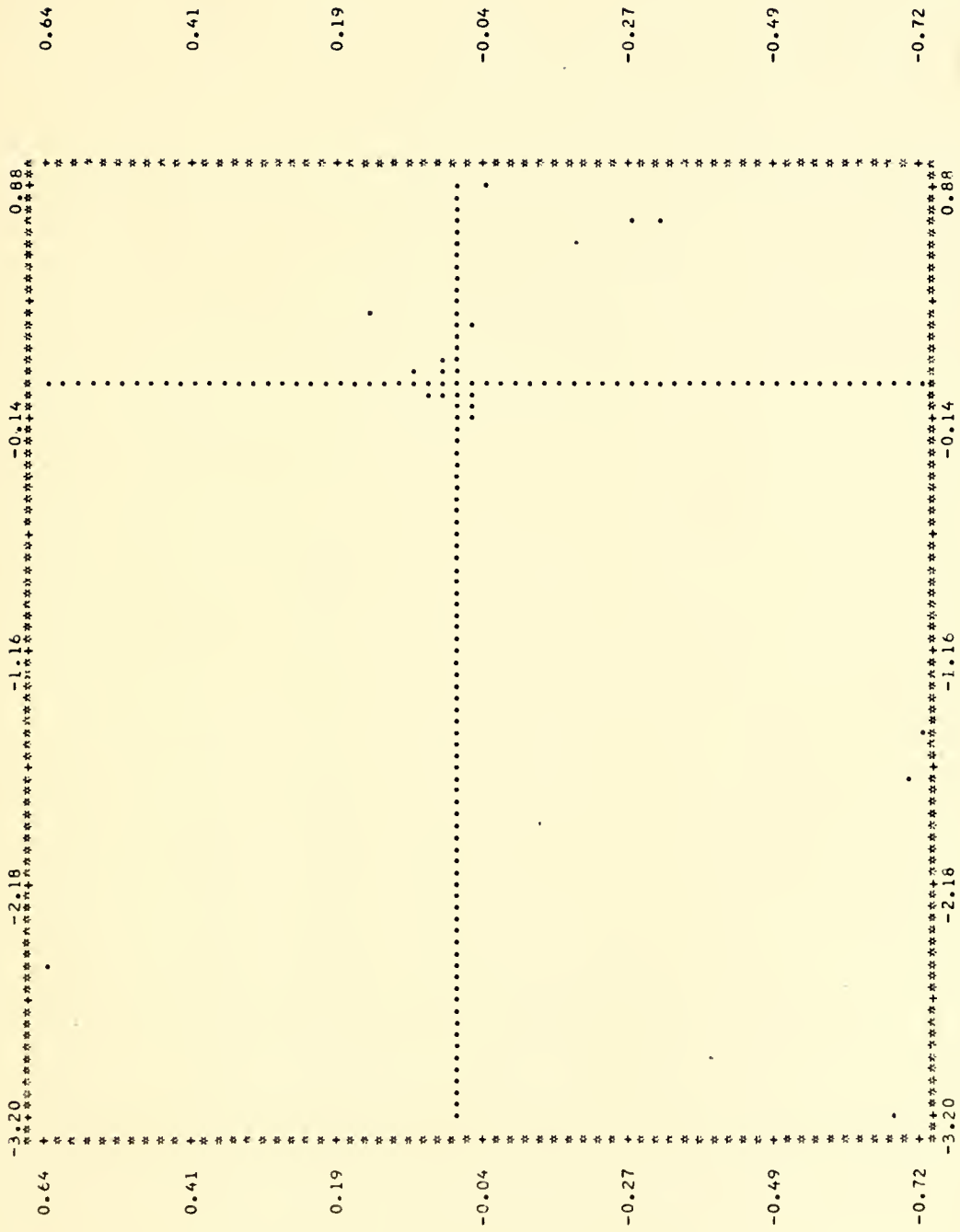


Y ACCELERATION ESTIMATE(X001(2)) VS. T  
LENTZ AN/TPQ-27





X ACCELERATION VS. Y ACCELERATION  
LENTZ AN/TPQ-27







AN/TPJ-27 SIMULATION  
COARSE GUIDANCE MODE WITH KALMAN FILTERING

INITIAL CONDITIONS :

TRUE WIND = 50.00 FT/SEC AT 45.00 DEGREES  
TRUE WIND COMPONENTS = 35.36 35.36  
ESTIMATED WIND = 50.00 FT/SEC AT 45.00 DEGREES  
ESTIMATED WIND COMPONENTS = 35.36 35.36

PARA9 DATA

MEASUREMENT SIGMAS (FT., AZ(DEG), EL(DEG)) = 9.000000 02 4.000000-01  
MEASUREMENT BIAS ( ) = 0.0 0.0 0.0  
INITIAL VELOCITY MEASUREMENT VALUES = 0.0 0.0 0.0  
RANGE-FOOTING ASSUMPTION VALUES (L1FW) = 0.0  
SAMPLING INTERVAL FOR RADAR (DRAU) = 6.000

AIRCRAFT DATA

TRUE INITIAL DISPLACEMENT FROM STARTING POINT (NM) = 50.00 2.000 0.0  
TRUE INITIAL GROUND VELOCITY = 550.00 FT/SEC AT 45.00 DEGREES  
TRUE INITIAL GROUND VELOCITY COMPONENTS = 388.91 388.91  
TRUE INITIAL A/P VELOCITY = 500.00 FT/SEC AT 45.00 DEGREES  
PULL RESPONSE PARAMETER (TB) = 3.300

TPACK DATA

NUMBER OF LEGS (NLEGS) = 3  
POSITION OF FIRST LEG = 50.000 NM AT 45.00 DEGREES  
COMPONENTS OF START POINT = 35.355 35.355

CONTROL DATA

CONTROL INTERVAL = 1.000  
MAXIMUM BANK ANGLE = 30.00  
G1 = 4.000  
G2 = 4.000  
MIN HEADING ERROR ANGLE FOR COMMAND CORRECTION = 5.000

LFG NUMBER 1

LEG START POINT (X,Y) = 35.3553 35.3553  
LEG END POINT (X,Y) = 40.3553 44.0152  
LEG LENGTH (NM) = 10.00  
LEG AZIMUTH (DEG) = 33.00  
DESIRED GROUND SPEED (FT/SEC) = 548.13  
DESIRED A/P HEADING (DEG) = 28.52  
AVG RANGE OF LEG FROM RADAR (NM) = 54.84  
AVG AZIMUTH OF LEG FROM RADAR (DEG) = 43.65  
TLEG = 110.852



| Y     | PHC      | PHI      | TLEGI    | TTURNI  | TG21    | TY21    | HTG   | HFG   | HTA   | HEA   | ETUF   | FEST   | PHO1     | PHO2     |
|-------|----------|----------|----------|---------|---------|---------|-------|-------|-------|-------|--------|--------|----------|----------|
| 0.0   | 0.0      | 0.0      | 0.0      | 0.0     | 0.0     | 0.0     | 45.00 | 0.0   | 45.00 | 0.0   | 0.7321 | 0.4312 | 0.0      | 0.0      |
| 1.00  | 0.0      | 0.0      | 0.0      | 0.0     | 0.0     | 0.0     | 45.00 | 0.0   | 45.00 | 0.0   | 0.7555 | 0.4333 | 0.0      | 0.0      |
| 2.00  | 0.0      | 0.0      | 0.0      | 0.0     | 0.0     | 0.0     | 45.00 | 0.0   | 45.00 | 0.0   | 0.7789 | 0.4355 | 0.0      | 0.0      |
| 3.00  | 0.0      | 0.0      | 0.0      | 0.0     | 0.0     | 0.0     | 45.00 | 0.0   | 45.00 | 0.0   | 0.8023 | 0.4376 | 0.0      | 0.0      |
| 4.00  | 0.0      | 0.0      | 0.0      | 0.0     | 0.0     | 0.0     | 45.00 | 0.0   | 45.00 | 0.0   | 0.8258 | 0.4397 | 0.0      | 0.0      |
| 5.00  | 0.0      | 0.0      | 0.0      | 0.0     | 0.0     | 0.0     | 45.00 | 0.0   | 45.00 | 0.0   | 0.8492 | 0.4419 | 0.0      | 0.0      |
| 6.00  | 0.0      | 0.0      | 0.0      | 0.0     | 0.0     | 0.0     | 45.00 | 37.80 | 45.00 | 36.92 | 0.8726 | 0.4926 | 0.0      | 0.0      |
| 7.00  | 0.0      | 0.0      | 0.0      | 0.0     | 0.0     | 0.0     | 45.00 | 37.80 | 45.00 | 36.92 | 0.8960 | 0.5028 | 0.0      | 0.0      |
| 8.00  | 0.0      | 0.0      | 0.0      | 0.0     | 0.0     | 0.0     | 45.00 | 37.80 | 45.00 | 36.92 | 0.9195 | 0.5131 | 0.0      | 0.0      |
| 9.00  | 0.0      | 0.0      | 0.0      | 0.0     | 0.0     | 0.0     | 45.00 | 37.80 | 45.00 | 36.92 | 0.9429 | 0.5233 | 0.0      | 0.0      |
| 10.00 | 0.0      | 0.0      | 0.0      | 0.0     | 0.0     | 0.0     | 45.00 | 37.30 | 45.00 | 36.92 | 0.9663 | 0.5235 | 0.0      | 0.0      |
| 11.00 | 0.0      | 0.0      | 0.0      | 0.0     | 0.0     | 0.0     | 45.00 | 37.80 | 45.00 | 36.92 | 0.9898 | 0.5438 | 0.0      | 0.0      |
| 12.00 | 0.0      | 0.0      | 0.0      | 0.0     | 0.0     | 0.0     | 45.00 | 37.66 | 45.00 | 36.71 | 1.0132 | 0.5467 | 0.0      | 0.0      |
| 13.00 | 0.0      | 0.0      | 100.9142 | 22.2506 | 14.8530 | 18.1395 | 45.00 | 37.66 | 45.00 | 36.71 | 1.0366 | 0.5563 | 0.0      | 0.0      |
| 14.00 | -25.8828 | -7.8121  | 99.5156  | 22.4009 | 14.9419 | 18.2288 | 44.76 | 37.36 | 44.74 | 36.37 | 1.0595 | 0.5657 | -50.9282 | -50.9282 |
| 15.00 | -25.8828 | -13.5819 | 97.5015  | 22.8006 | 15.1705 | 18.4647 | 44.13 | 36.55 | 44.04 | 35.46 | 1.0825 | 0.5743 | -50.2869 | 0.6413   |
| 16.00 | -25.8828 | -17.8433 | 95.1112  | 23.3503 | 15.5198 | 18.8087 | 43.20 | 35.38 | 43.02 | 34.15 | 1.1039 | 0.5818 | -47.6342 | 2.6527   |
| 17.00 | -25.8828 | -20.9907 | 92.5293  | 24.1282 | 15.9473 | 19.2326 | 42.06 | 33.93 | 41.77 | 32.50 | 1.1238 | 0.5876 | -43.4711 | 4.1631   |
| 18.00 | -25.8828 | -23.3153 | 71.7919  | 15.9463 | 13.7697 | 17.0509 | 40.76 | 41.24 | 40.34 | 40.89 | 1.1417 | 0.8513 | -38.1657 | 5.3054   |
| 19.00 | -25.8828 | -25.0322 | 69.4074  | 16.3974 | 14.1419 | 17.4271 | 39.34 | 39.52 | 38.78 | 39.45 | 1.1575 | 0.8691 | -79.8191 | -41.6535 |
| 20.00 | -25.8828 | -26.3003 | 67.0591  | 15.8825 | 14.5409 | 17.8260 | 37.84 | 38.51 | 37.12 | 37.91 | 1.1710 | 0.8646 | -75.3560 | 3.9631   |
| 21.00 | -25.8828 | -27.2368 | 64.7724  | 17.3954 | 14.9549 | 18.2417 | 36.27 | 37.05 | 35.40 | 36.32 | 1.1821 | 0.8973 | -71.5236 | 4.3324   |
| 22.00 | -25.8828 | -27.9286 | 62.5659  | 17.9318 | 15.3813 | 18.6698 | 34.65 | 35.54 | 33.62 | 34.67 | 1.1907 | 0.5094 | -66.8956 | 4.6289   |
| 23.00 | -25.8823 | -28.4354 | 60.4443  | 18.4886 | 15.8159 | 19.1068 | 33.00 | 34.00 | 31.81 | 32.99 | 1.1568 | 0.3164 | -62.0270 | 4.8686   |
| 24.00 | -25.8828 | -28.8168 | 60.8346  | 20.1649 | 16.5708 | 19.8628 | 31.32 | 31.39 | 29.97 | 30.08 | 1.2002 | 0.3835 | -56.9569 | 5.0701   |
| 25.00 | -25.8828 | -29.0955 | 58.8568  | 20.8197 | 17.0392 | 20.3323 | 29.62 | 29.73 | 28.10 | 28.27 | 1.2009 | 0.8844 | -45.2054 | 11.7516  |
| 26.00 | -29.8828 | -29.3013 | 56.9715  | 21.4929 | 17.5115 | 20.8055 | 27.91 | 28.06 | 26.22 | 26.44 | 1.1950 | 0.8826 | -39.3605 | 5.8449   |
| 27.00 | -27.1875 | -26.7487 | 55.1841  | 22.1753 | 17.9807 | 21.2755 | 26.20 | 26.41 | 24.36 | 24.63 | 1.1944 | 0.8781 | -33.3610 | 5.9995   |
| 28.00 | -21.0939 | -26.7475 | 53.5113  | 22.8402 | 10.4236 | 21.7241 | 24.58 | 24.82 | 22.53 | 22.90 | 1.1871 | 0.3710 | -27.2995 | 6.0615   |
| 29.00 | -15.4688 | -23.7990 | 51.9636  | 23.4569 | 18.8361 | 22.1321 | 23.09 | 23.38 | 20.95 | 21.33 | 1.1774 | 0.8615 | -21.4292 | 5.8703   |
| 30.00 | 0.0      | -17.5774 | 51.5945  | 22.5681 | 18.3402 | 21.6445 | 21.88 | 25.09 | 19.63 | 23.21 | 1.1656 | 0.5711 | -16.0244 | 5.4048   |
| 31.00 | -25.8828 | -20.7943 | 50.1836  | 23.0290 | 13.6581 | 21.9539 | 20.75 | 22.99 | 18.39 | 22.02 | 1.1521 | 0.9622 | -29.3795 | -13.3550 |
| 32.00 | -21.6797 | -21.0258 | 48.7759  | 23.5369 | 19.9035 | 22.2896 | 19.51 | 22.81 | 17.05 | 20.72 | 1.1367 | 0.9515 | -25.5689 | 3.8106   |
| 33.00 | -16.8750 | -19.9407 | 47.4133  | 24.0413 | 19.3214 | 22.6179 | 18.31 | 21.64 | 15.73 | 19.46 | 1.1195 | 0.5389 | -21.3068 | 4.2620   |
| 34.00 | 0.0      | -14.7277 | 46.1350  | 24.4717 | 19.5912 | 22.8940 | 17.29 | 20.66 | 14.62 | 18.39 | 1.1005 | 0.9246 | -17.0651 | 4.2418   |



| T  | PHC     | PHI      | TLEGI   | TTURN1  | TQ21    | TY21    | HTG   | HEG   | HTA   | HEA   | ETRUE  | SEST   | PHU1     | PHQ2    |
|--|---------|----------|---------|---------|---------|---------|-------|-------|-------|-------|--------|--------|----------|---------|
| 25.00                                    | 0.0     | -10.8775 | 44.9454 | 24.7934 | 19.8010 | 23.0979 | 16.54 | 19.94 | 13.81 | 17.61 | 1.0602 | 0.9039 | -13.4621 | 3.5829  |
| 36.00                                    | 0.0     | -8.0339  | 43.4188 | 25.7809 | 20.3710 | 23.0694 | 15.98 | 17.92 | 13.20 | 15.40 | 1.0590 | 0.8204 | -10.3596 | 2.6225  |
| 37.00                                    | 0.0     | -5.9326  | 42.3371 | 25.9649 | 20.4835 | 23.7810 | 15.57 | 17.52 | 12.76 | 14.97 | 1.0370 | 0.6007 | 1.2609   | 12.1205 |
| 38.00                                    | 0.0     | -4.2825  | 41.2798 | 26.1000 | 20.5616 | 23.6634 | 15.27 | 17.23 | 12.43 | 14.65 | 1.0145 | 0.7805 | 2.8953   | 1.6349  |
| 39.00                                    | 0.0     | -3.2368  | 40.2393 | 26.2007 | 20.6266 | 23.9243 | 15.05 | 17.01 | 12.13 | 14.42 | 0.9916 | 0.7599 | 4.1518   | 1.2560  |
| 40.00                                    | 0.0     | -2.5906  | 39.2106 | 26.2754 | 20.6715 | 23.9192 | 14.83 | 16.85 | 12.00 | 14.24 | 0.9684 | 0.7390 | 5.1303   | 0.9790  |
| 41.00                                    | 0.0     | -1.7656  | 38.1902 | 26.3306 | 20.7047 | 24.0024 | 14.76 | 16.74 | 11.87 | 14.12 | 0.9451 | 0.7179 | 5.9083   | 0.7775  |
| 42.00                                    | 0.0     | -1.3041  | 41.6014 | 27.3408 | 20.5276 | 23.8252 | 14.67 | 17.51 | 11.77 | 14.80 | 0.9215 | 0.7513 | 6.5402   | 0.6319  |
| 43.00                                    | 0.0     | -0.9632  | 40.5884 | 27.3744 | 20.5469 | 23.8445 | 14.60 | 17.45 | 11.70 | 14.73 | 0.8979 | 0.7724 | -0.3351  | -6.8752 |
| 44.00                                    | 0.0     | -0.7114  | 39.5790 | 27.3995 | 20.5611 | 23.8587 | 14.55 | 17.39 | 11.65 | 14.67 | 0.8741 | 0.7533 | -0.0676  | 0.2674  |
| 45.00                                    | 0.0     | -0.5254  | 38.5723 | 27.4171 | 20.5716 | 23.9692 | 14.52 | 17.36 | 11.61 | 14.63 | 0.8503 | 0.7342 | 0.1344   | 0.2020  |
| 46.00                                    | 0.0     | -0.3880  | 37.5675 | 27.4313 | 20.5743 | 23.8769 | 14.49 | 17.33 | 11.58 | 14.60 | 0.8264 | 0.7151 | 0.2884   | 0.1540  |
| 47.00                                    | 0.0     | -0.2866  | 36.5640 | 27.4413 | 20.5810 | 23.8627 | 14.47 | 17.31 | 11.56 | 14.58 | 0.8026 | 0.6959 | 0.2584   | 0.1540  |
| 48.00                                    | 0.0     | -0.2117  | 37.3147 | 28.0422 | 20.5317 | 23.8293 | 14.45 | 17.58 | 11.54 | 14.78 | 0.7786 | 0.7190 | 0.2884   | 0.1540  |
| 49.00                                    | 0.0     | -0.1563  | 36.8127 | 28.0481 | 20.5349 | 23.8325 | 14.44 | 17.57 | 11.53 | 14.77 | 0.7547 | 0.7007 | 0.2884   | 0.1540  |
| 50.00                                    | 0.0     | -0.1195  | 35.8112 | 28.0523 | 20.5373 | 23.8349 | 14.44 | 17.56 | 11.52 | 14.76 | 0.7308 | 0.6824 | 0.2884   | 0.1540  |
| 51.00                                    | 0.0     | -0.0853  | 34.8102 | 28.0555 | 20.5370 | 23.8266 | 14.43 | 17.55 | 11.51 | 14.76 | 0.7068 | 0.6641 | 0.2884   | 0.1540  |
| 52.00                                    | 0.0     | -0.0630  | 33.8095 | 28.0576 | 20.5402 | 23.8379 | 14.43 | 17.55 | 11.51 | 14.75 | 0.6828 | 0.6458 | 0.2884   | 0.1540  |
| 53.00                                    | 0.0     | -0.0465  | 32.8090 | 28.0596 | 20.5415 | 23.8385 | 14.42 | 17.54 | 11.51 | 14.75 | 0.6589 | 0.6275 | 0.2884   | 0.1540  |
| 54.00                                    | 0.0     | -0.0344  | 29.4487 | 28.5495 | 21.1103 | 24.4033 | 14.42 | 15.47 | 11.50 | 12.55 | 0.6349 | 0.4501 | 0.2884   | 0.1540  |
| 55.00                                    | 0.0     | -0.0234  | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 14.42 | 15.47 | 11.50 | 12.55 | 0.6109 | 0.4284 | 0.2884   | 0.1540  |
| STARTING TURN: T = 56.00      TURN = 0.0 |         |          |         |         |         |         |       |       |       |       |        |        |          |         |
| 56.00                                    | 30.0000 | 7.8240   | 28.4485 | 28.5504 | 21.1103 | 24.4088 | 14.66 | 15.72 | 11.77 | 12.82 | 0.5871 | 0.4068 | 0.2884   | 0.1540  |
| 57.00                                    | 30.0000 | 13.6213  | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 15.30 | 16.38 | 12.46 | 13.54 | 0.5639 | 0.3658 | 0.2884   | 0.1540  |
| 58.00                                    | 30.0000 | 17.9031  | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 16.24 | 17.35 | 13.45 | 14.60 | 0.5415 | 0.3561 | 0.2884   | 0.1540  |
| 59.00                                    | 30.0000 | 21.0655  | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 17.40 | 18.54 | 14.74 | 15.90 | 0.5215 | 0.3479 | 0.2884   | 0.1540  |
| 60.00                                    | 30.0000 | 23.4012  | 28.4485 | 28.5504 | 21.1109 | 24.4088 | 18.72 | 19.90 | 16.18 | 17.38 | 0.5029 | 0.3316 | 0.2884   | 0.1540  |
| 61.00                                    | 30.0000 | 25.1263  | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 20.15 | 21.37 | 17.74 | 19.00 | 0.4865 | 0.3174 | 0.2884   | 0.1540  |
| 62.00                                    | 30.0000 | 26.4004  | 28.4485 | 28.5504 | 21.1109 | 24.4088 | 21.67 | 22.94 | 19.40 | 20.71 | 0.4723 | 0.3055 | 0.2884   | 0.1540  |
| 63.00                                    | 30.0000 | 27.3414  | 28.4485 | 28.5504 | 21.1106 | 24.4088 | 23.26 | 24.57 | 21.13 | 22.50 | 0.4605 | 0.2950 | 0.2884   | 0.1540  |
| 64.00                                    | 30.0000 | 28.0364  | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 24.89 | 26.25 | 22.92 | 24.34 | 0.4512 | 0.2890 | 0.2884   | 0.1540  |
| 65.00                                    | 30.0000 | 28.5497  | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 26.55 | 27.96 | 24.74 | 26.23 | 0.4445 | 0.2846 | 0.2884   | 0.1540  |
| 66.00                                    | 30.0000 | 28.9289  | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 28.24 | 29.70 | 26.59 | 28.14 | 0.4404 | 0.2828 | 0.2884   | 0.1540  |
| 67.00                                    | 30.0000 | 29.2089  | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 29.95 | 31.46 | 28.46 | 30.07 | 0.4390 | 0.2837 | 0.2884   | 0.1540  |
| 68.00                                    | 30.0000 | 29.4157  | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 31.67 | 33.23 | 30.35 | 32.02 | 0.4402 | 0.2873 | 0.2884   | 0.1540  |



| T     | PHC     | PHI     | TLFGL   | TURN1   | TQ21    | TT21    | HTG   | HEG   | HTA   | HEA   | ETQUE  | EEST   | PHD1   | PHO2   |
|-------|---------|---------|---------|---------|---------|---------|-------|-------|-------|-------|--------|--------|--------|--------|
| 69.00 | 30.0000 | 29.5685 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 33.40 | 35.01 | 32.24 | 33.98 | 0.4442 | 0.2936 | 0.2884 | 0.1540 |
| 70.00 | 30.0000 | 29.4813 | 28.4495 | 28.5504 | 21.1108 | 24.4088 | 35.13 | 36.80 | 34.15 | 35.95 | 0.4509 | 0.3026 | 0.2884 | 0.1540 |
| 71.00 | 30.0000 | 29.7646 | 28.4435 | 28.5504 | 21.1108 | 24.4088 | 36.87 | 38.59 | 36.06 | 37.93 | 0.4604 | 0.3144 | 0.2884 | 0.1540 |
| 72.00 | 30.0000 | 29.8261 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 38.62 | 40.35 | 37.98 | 39.91 | 0.4726 | 0.3288 | 0.2884 | 0.1540 |
| 73.00 | 30.0000 | 29.8716 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 40.36 | 42.15 | 39.90 | 41.90 | 0.4875 | 0.3460 | 0.2884 | 0.1540 |
| 74.00 | 30.0000 | 29.9052 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 42.11 | 43.99 | 41.92 | 43.88 | 0.5051 | 0.3659 | 0.2884 | 0.1540 |
| 75.00 | 30.0000 | 29.9300 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 43.86 | 45.79 | 43.75 | 45.87 | 0.5255 | 0.3885 | 0.2884 | 0.1540 |
| 76.00 | 30.0000 | 29.9483 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 45.61 | 47.60 | 45.68 | 47.86 | 0.5485 | 0.4137 | 0.2884 | 0.1540 |
| 77.00 | 30.0000 | 29.9618 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 47.37 | 49.40 | 47.60 | 49.86 | 0.5742 | 0.4416 | 0.2884 | 0.1540 |
| 78.00 | 30.0000 | 29.9718 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 49.12 | 51.21 | 49.53 | 51.85 | 0.6025 | 0.4721 | 0.2884 | 0.1540 |
| 79.00 | 30.0000 | 29.9792 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 50.87 | 53.02 | 51.47 | 53.84 | 0.6305 | 0.5051 | 0.2884 | 0.1540 |
| 80.00 | 30.0000 | 29.9846 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 52.63 | 54.83 | 53.39 | 55.87 | 0.6577 | 0.5407 | 0.2884 | 0.1540 |
| 81.00 | 30.0000 | 29.9886 | 28.4435 | 28.5504 | 21.1108 | 24.4088 | 54.39 | 56.64 | 55.32 | 57.83 | 0.6838 | 0.5744 | 0.2884 | 0.1540 |
| 82.00 | 30.0000 | 29.9916 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 56.14 | 58.45 | 57.25 | 59.82 | 0.7083 | 0.6074 | 0.2884 | 0.1540 |
| 83.00 | 30.0000 | 29.9938 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 57.90 | 60.26 | 59.18 | 61.82 | 0.7332 | 0.6428 | 0.2884 | 0.1540 |
| 84.00 | 30.0000 | 29.9954 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 59.66 | 62.07 | 61.11 | 63.81 | 0.7564 | 0.6764 | 0.2884 | 0.1540 |
| 85.00 | 30.0000 | 29.9966 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 61.42 | 63.89 | 63.04 | 65.81 | 0.7781 | 0.7099 | 0.2884 | 0.1540 |
| 86.00 | 30.0000 | 29.9975 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 63.13 | 65.71 | 64.97 | 67.80 | 0.7991 | 0.7427 | 0.2884 | 0.1540 |
| 87.00 | 30.0000 | 29.9982 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 64.95 | 67.53 | 66.90 | 69.80 | 0.8193 | 0.7750 | 0.2884 | 0.1540 |
| 88.00 | 30.0000 | 29.9986 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 66.71 | 69.35 | 68.83 | 71.79 | 0.8392 | 0.8077 | 0.2884 | 0.1540 |
| 89.00 | 30.0000 | 29.9990 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 68.48 | 71.17 | 70.76 | 73.79 | 0.8591 | 0.8392 | 0.2884 | 0.1540 |
| 90.00 | 30.0000 | 29.9993 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 70.25 | 73.00 | 72.69 | 75.78 | 0.8781 | 0.8707 | 0.2884 | 0.1540 |
| 91.00 | 30.0000 | 29.9995 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 72.02 | 74.83 | 74.62 | 77.78 | 0.8971 | 0.9026 | 0.2884 | 0.1540 |
| 92.00 | 30.0000 | 29.9996 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 73.79 | 76.66 | 76.55 | 79.77 | 0.9161 | 0.9271 | 0.2884 | 0.1540 |
| 93.00 | 30.0000 | 29.9997 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 75.57 | 78.50 | 78.43 | 81.77 | 0.9351 | 0.9476 | 0.2884 | 0.1540 |
| 94.00 | 30.0000 | 29.9998 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 77.35 | 80.34 | 80.41 | 83.76 | 0.9541 | 0.9691 | 0.2884 | 0.1540 |
| 95.00 | 30.0000 | 29.9998 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 79.13 | 82.13 | 82.34 | 85.76 | 0.9731 | 0.9941 | 0.2884 | 0.1540 |
| 96.00 | 30.0000 | 29.9999 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 80.91 | 84.02 | 84.27 | 87.75 | 0.9921 | 1.0152 | 0.2884 | 0.1540 |
| 97.00 | 30.0000 | 29.9999 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 82.70 | 85.87 | 86.20 | 89.75 | 1.0111 | 1.0379 | 0.2884 | 0.1540 |
| 98.00 | 30.0000 | 29.9999 | 28.4485 | 28.5504 | 21.1108 | 24.4088 | 84.49 | 87.72 | 88.13 | 91.74 | 1.0301 | 1.0647 | 0.2884 | 0.1540 |

TINTRN = 43.00

TURN ENDING T = 59.00





## LEG NUMBER 2

LEG START POINT (X,Y) = 40.3553 44.0156  
 LEG END POINT (X,Y) = 50.3553 44.0156  
 LEG LENGTH (NM) = 10.00  
 LEG AZIMUTH (DEG) = 90.00

DESIGED GROUND SPEED (FT/SEC) = 524.10

DESIGED AIR HEADING (DEG) = 94.05

AVG RANGE OF LEG FROM RADAR (NM) = 63.20

AVG AZIMUTH OF LEG FROM RADAR (DEG) = 43.86

\*LEG = 113.762

| T                                       | PHC | FHI     | TLEGL   | TTURN1  | T021    | *T21    | HTG   | HEG   | HTA   | HEA   | ETQUE   | EEST    | PH01     | PH02     |
|---|-----|---------|---------|---------|---------|---------|-------|-------|-------|-------|---------|---------|----------|----------|
| 99.00                                   | 0.0 | 22.1573 | 95.8523 | 21.7079 | 16.8215 | 20.1140 | 86.04 | 89.32 | 89.80 | 93.46 | -0.0+50 | 0.0833  | 0.2884   | 0.1540   |
| 100.00                                  | 0.0 | 16.3648 | 93.8596 | 22.2024 | 17.1507 | 20.4440 | 87.18 | 90.51 | 91.03 | 94.73 | -0.0502 | 0.0832  | 0.2884   | 0.1540   |
| 101.00                                  | 0.0 | 12.0967 | 92.1754 | 22.5729 | 17.3938 | 20.6876 | 88.03 | 91.38 | 91.54 | 95.67 | -0.0538 | 0.0846  | 0.2884   | 0.1540   |
| 102.00                                  | 0.0 | 8.9269  | 90.6570 | 22.8496 | 17.5734 | 20.8675 | 88.65 | 92.03 | 92.61 | 96.37 | -0.0564 | 0.0872  | 0.2884   | 0.1540   |
| 103.00                                  | 0.0 | 6.5932  | 89.3589 | 23.0556 | 17.7061 | 21.0004 | 89.11 | 92.51 | 93.11 | 96.88 | -0.0581 | 0.0906  | 0.2884   | 0.1540   |
| 104.00                                  | 0.0 | 4.3696  | 88.1180 | 23.2086 | 17.8040 | 21.0985 | 89.46 | 92.86 | 93.47 | 97.26 | -0.0592 | 0.0945  | 0.2884   | 0.1540   |
| TURN COMPLETE T = 105.00 TINTPN = 49.00 |     |         |         |         |         |         |       |       |       |       |         |         |          |          |
| 105.00                                  | 0.0 | 3.5966  | 86.9452 | 23.3222 | 17.8764 | 21.1710 | 89.71 | 93.12 | 93.74 | 97.54 | -0.0598 | 0.0990  | 0.2884   | 0.1540   |
| 106.00                                  | 0.0 | 2.3563  | 85.8208 | 23.4064 | 17.9298 | 21.2245 | 89.89 | 93.32 | 93.94 | 97.74 | -0.0601 | 0.1038  | -15.4525 | -15.7469 |
| 107.00                                  | 0.0 | 1.5619  | 84.7309 | 23.4687 | 17.9693 | 21.2641 | 90.03 | 93.46 | 94.05 | 97.89 | -0.0601 | 0.1098  | -16.4021 | -0.9495  |
| 108.00                                  | 0.0 | 1.4490  | 82.7192 | 22.0452 | 17.3560 | 20.6496 | 90.13 | 91.35 | 94.20 | 95.53 | -0.0600 | -0.0322 | -17.1614 | -0.7593  |
| 109.00                                  | 0.0 | 1.0702  | 81.6678 | 22.0764 | 17.3769 | 20.6706 | 90.21 | 91.43 | 94.28 | 95.61 | -0.0597 | -0.0301 | -4.3890  | 12.7724  |
| 110.00                                  | 0.0 | 0.7994  | 80.6306 | 22.0995 | 17.3974 | 20.6862 | 90.26 | 91.48 | 94.34 | 95.67 | -0.0594 | -0.0279 | -4.7468  | -0.3578  |
| 111.00                                  | 0.0 | 0.5838  | 79.6034 | 22.1166 | 17.4038 | 20.6976 | 90.30 | 91.52 | 94.38 | 95.71 | -0.0589 | -0.0256 | -5.0300  | -0.2832  |
| 112.00                                  | 0.0 | 0.4312  | 78.5937 | 22.1293 | 17.4123 | 20.7061 | 90.34 | 91.55 | 94.41 | 95.74 | -0.0584 | -0.0233 | -5.2586  | -0.2286  |
| 113.00                                  | 0.0 | 0.3185  | 77.5693 | 22.1386 | 17.4185 | 20.7123 | 90.36 | 91.58 | 94.44 | 95.77 | -0.0579 | -0.0209 | -5.4475  | -0.1888  |
| 114.00                                  | 0.0 | 0.2352  | 78.2271 | 21.8555 | 17.1711 | 20.4644 | 90.37 | 90.66 | 94.46 | 94.81 | -0.0574 | -0.0938 | -5.6074  | -0.1600  |
| 115.00                                  | 0.0 | 0.1737  | 77.2189 | 21.8606 | 17.1745 | 20.4678 | 90.39 | 90.68 | 94.47 | 94.83 | -0.0569 | -0.0928 | 0.5077   | 6.1152   |
| 116.00                                  | 0.0 | 0.1283  | 76.2129 | 21.8643 | 17.1770 | 20.4703 | 90.40 | 90.69 | 94.43 | 94.84 | -0.0562 | -0.0917 | 0.4647   | -0.0431  |
| 117.00                                  | 0.0 | 0.0948  | 75.2086 | 21.8671 | 17.1789 | 20.4722 | 90.40 | 90.69 | 94.45 | 94.84 | -0.0556 | -0.0907 | 0.4341   | -0.0306  |
| 118.00                                  | 0.0 | 0.0700  | 74.2054 | 21.8691 | 17.1803 | 20.4736 | 90.41 | 90.70 | 94.45 | 94.85 | -0.0549 | -0.0896 | 0.4128   | -0.0213  |
| 119.00                                  | 0.0 | 0.0517  | 73.2031 | 21.8706 | 17.1813 | 20.4746 | 90.41 | 90.70 | 94.49 | 94.85 | -0.0543 | -0.0886 | 0.3983   | -0.0144  |
| 120.00                                  | 0.0 | 0.0382  | 73.9070 | 21.6439 | 16.9602 | 20.2531 | 90.41 | 89.88 | 94.50 | 94.00 | -0.0537 | -0.1599 | 0.3890   | -0.0092  |
| 121.00                                  | 0.0 | 0.0282  | 72.9057 | 21.6447 | 16.9608 | 20.2536 | 90.42 | 89.88 | 94.50 | 94.00 | -0.0530 | -0.1600 | 6.2915   | 5.9025   |
| 122.00                                  | 0.0 | 0.0208  | 71.9048 | 21.6453 | 16.9612 | 20.2541 | 90.42 | 89.89 | 94.50 | 94.00 | -0.0524 | -0.1602 | 6.3710   | 0.0795   |
| 123.00                                  | 0.0 | 0.0154  | 70.9041 | 21.6458 | 16.9615 | 20.2544 | 90.42 | 89.89 | 94.50 | 94.00 | -0.0518 | -0.1604 | 6.4550   | 0.0840   |



| T      | PHC | PHI    | TLEGI   | TTURN1  | TC21    | TT21    | MTG   | HEG   | HTA   | HEA   | FTSUE   | EEST    | PHD1    | PHD2    |
|--------|-----|--------|---------|---------|---------|---------|-------|-------|-------|-------|---------|---------|---------|---------|
| 124.00 | 0.0 | 0.0114 | 69.9036 | 21.6461 | 16.9617 | 20.2546 | 90.42 | 99.89 | 94.50 | 94.00 | -0.0511 | -0.1606 | 6.5431  | 0.0881  |
| 125.00 | 0.0 | 0.0084 | 68.9032 | 21.6464 | 16.9619 | 20.2548 | 50.42 | 89.89 | 94.50 | 94.00 | -0.0505 | -0.1607 | 6.6349  | 0.0919  |
| 126.00 | 0.0 | 0.0062 | 67.6369 | 21.3346 | 16.8272 | 20.1198 | 90.42 | 89.43 | 94.50 | 93.48 | -0.0498 | -0.2014 | 6.7304  | 0.0955  |
| 127.00 | 0.0 | 0.0046 | 66.6367 | 21.3347 | 16.8273 | 20.1199 | 90.42 | 89.43 | 94.50 | 93.49 | -0.0492 | -0.2023 | 10.3196 | 3.5891  |
| 128.00 | 0.0 | 0.0034 | 65.6365 | 21.3348 | 16.8274 | 20.1200 | 90.42 | 89.43 | 94.50 | 93.49 | -0.0486 | -0.2031 | 10.4771 | 0.1575  |
| 129.00 | 0.0 | 0.0025 | 64.6364 | 21.3349 | 16.8275 | 20.1200 | 50.42 | 89.43 | 94.50 | 92.49 | -0.0479 | -0.2040 | 10.6399 | 0.1628  |
| 130.00 | 0.0 | 0.0018 | 63.6363 | 21.3349 | 16.8275 | 20.1200 | 50.42 | 89.43 | 94.50 | 93.49 | -0.0473 | -0.2049 | 10.8061 | 0.1682  |
| 131.00 | 0.0 | 0.0014 | 62.6363 | 21.3350 | 16.8275 | 20.1201 | 50.42 | 89.43 | 94.51 | 93.49 | -0.0466 | -0.2057 | 10.9820 | 0.1739  |
| 132.00 | 0.0 | 0.0010 | 62.8422 | 21.2942 | 16.7298 | 20.0222 | 50.42 | 89.06 | 94.51 | 93.11 | -0.0460 | -0.2455 | 11.1617 | 0.1797  |
| 133.00 | 0.0 | 0.0007 | 61.8422 | 21.2942 | 16.7299 | 20.0222 | 50.42 | 89.06 | 94.51 | 93.11 | -0.0453 | -0.2469 | 14.4836 | 3.3220  |
| 134.00 | 0.0 | 0.0005 | 60.8422 | 21.2942 | 16.7299 | 20.0222 | 50.42 | 89.06 | 94.51 | 93.11 | -0.0447 | -0.2484 | 14.7260 | 0.2424  |
| 135.00 | 0.0 | 0.0034 | 59.8422 | 21.2942 | 16.7299 | 20.0222 | 50.42 | 89.06 | 94.51 | 93.11 | -0.0440 | -0.2498 | 14.9767 | 0.2507  |
| 136.00 | 0.0 | 0.0003 | 58.8421 | 21.2942 | 16.7299 | 20.0222 | 50.42 | 89.06 | 94.51 | 93.11 | -0.0434 | -0.2512 | 15.2361 | 0.2594  |
| 137.00 | 0.0 | 0.0002 | 57.8421 | 21.2942 | 16.7299 | 20.0222 | 90.42 | 89.06 | 94.51 | 93.11 | -0.0427 | -0.2526 | 15.5046 | 0.2685  |
| 138.00 | 0.0 | 0.0002 | 53.4136 | 21.3131 | 16.9656 | 20.2585 | 90.42 | 89.98 | 94.51 | 94.02 | -0.0421 | -0.1495 | 15.7828 | 0.2782  |
| 139.00 | 0.0 | 0.0001 | 52.4136 | 21.3131 | 16.9656 | 20.2585 | 90.42 | 89.98 | 94.51 | 94.02 | -0.0415 | -0.1495 | 7.4597  | -8.2831 |
| 140.00 | 0.0 | 0.0001 | 51.4136 | 21.3131 | 16.9656 | 20.2585 | 90.42 | 89.98 | 94.51 | 94.02 | -0.0408 | -0.1495 | 7.6454  | 0.1457  |
| 141.00 | 0.0 | 0.0001 | 50.4136 | 21.3131 | 16.9656 | 20.2585 | 90.42 | 89.98 | 94.51 | 94.02 | -0.0402 | -0.1496 | 7.7969  | 0.1515  |
| 142.00 | 0.0 | 0.0000 | 49.4136 | 21.3131 | 16.9656 | 20.2585 | 90.42 | 89.98 | 94.51 | 94.02 | -0.0395 | -0.1496 | 7.9546  | 0.1576  |
| 143.00 | 0.0 | 0.0000 | 48.4136 | 21.3131 | 16.9656 | 20.2585 | 90.42 | 89.98 | 94.51 | 94.02 | -0.0389 | -0.1496 | 8.1187  | 0.1641  |
| 144.00 | 0.0 | 0.0000 | 46.7969 | 21.3868 | 17.0442 | 20.3373 | 90.42 | 90.27 | 94.51 | 94.32 | -0.0382 | -0.1153 | 8.2897  | 0.1710  |
| 145.00 | 0.0 | 0.0000 | 45.7969 | 21.3868 | 17.0442 | 20.3373 | 50.42 | 90.27 | 94.51 | 94.32 | -0.0376 | -0.1149 | 5.4002  | -2.8695 |
| 146.00 | 0.0 | 0.0000 | 44.7969 | 21.3868 | 17.0442 | 20.3373 | 50.42 | 90.27 | 94.51 | 94.32 | -0.0369 | -0.1145 | 5.5157  | 0.1195  |
| 147.00 | 0.0 | 0.0000 | 43.7969 | 21.3868 | 17.0442 | 20.3373 | 50.42 | 90.27 | 94.51 | 94.32 | -0.0363 | -0.1141 | 5.6446  | 0.1249  |
| 148.00 | 0.0 | 0.0000 | 42.7969 | 21.3868 | 17.0442 | 20.3373 | 90.42 | 90.27 | 94.51 | 94.32 | -0.0357 | -0.1137 | 5.7753  | 0.1307  |
| 149.00 | 0.0 | 0.0000 | 41.7969 | 21.3868 | 17.0442 | 20.3373 | 50.42 | 90.27 | 94.51 | 94.32 | -0.0350 | -0.1133 | 5.9122  | 0.1369  |
| 150.00 | 0.0 | 0.0000 | 42.0859 | 21.3384 | 16.9314 | 20.2242 | 50.42 | 89.84 | 94.51 | 93.89 | -0.0344 | -0.1679 | 6.0557  | 0.1435  |
| 151.00 | 0.0 | 0.0000 | 41.0859 | 21.3384 | 16.9314 | 20.2242 | 50.42 | 89.84 | 94.51 | 93.89 | -0.0337 | -0.1682 | 11.3585 | 5.3028  |
| 152.00 | 0.0 | 0.0000 | 40.0859 | 21.3384 | 16.9314 | 20.2242 | 50.42 | 89.84 | 94.51 | 93.89 | -0.0331 | -0.1684 | 11.6426 | 0.2841  |
| 153.00 | 0.0 | 0.0000 | 39.0859 | 21.3384 | 16.9314 | 20.2242 | 50.42 | 89.84 | 94.51 | 93.89 | -0.0324 | -0.1687 | 11.9413 | 0.2987  |
| 154.00 | 0.0 | 0.0000 | 38.0859 | 21.3384 | 16.9314 | 20.2242 | 50.42 | 89.84 | 94.51 | 93.89 | -0.0318 | -0.1689 | 12.2557 | 0.3144  |
| 155.00 | 0.0 | 0.0000 | 37.0859 | 21.3384 | 16.9314 | 20.2242 | 90.42 | 89.84 | 94.51 | 93.89 | -0.0311 | -0.1692 | 12.5872 | 0.3314  |
| 156.00 | 0.0 | 0.0000 | 36.4294 | 21.2590 | 16.8668 | 20.1615 | 90.42 | 89.61 | 94.51 | 93.65 | -0.0305 | -0.1984 | 12.9370 | 0.3498  |
| 157.00 | 0.0 | 0.0000 | 35.4294 | 21.2590 | 16.8668 | 20.1615 | 90.42 | 89.61 | 94.51 | 93.65 | -0.0298 | -0.1990 | 16.3521 | 3.4161  |
| 158.00 | 0.0 | 0.0000 | 34.4294 | 21.2590 | 16.8668 | 20.1615 | 90.42 | 89.61 | 94.51 | 93.65 | -0.0292 | -0.1996 | 16.8328 | 0.4798  |



| T                      | PHC      | PHI      | PLEGI   | TTURN1  | T021    | T121    | HTG   | HEG   | HTA   | HEA   | EFUE    | EFST    | PHO1    | PHO2   |
|------------------------|----------|----------|---------|---------|---------|---------|-------|-------|-------|-------|---------|---------|---------|--------|
| 159.00                 | 0.0      | 0.0000   | 33.4294 | 21.2590 | 16.8688 | 20.1615 | 90.42 | 89.61 | 94.51 | 93.65 | -0.0286 | -0.2002 | 17.3416 | 0.5087 |
| 160.00                 | 0.0      | 0.0000   | 32.4294 | 21.2590 | 16.8689 | 20.1615 | 90.42 | 89.61 | 94.51 | 93.65 | -0.0279 | -0.2008 | 17.8819 | 0.5404 |
| 161.00                 | 0.0      | 0.0000   | 31.4294 | 21.2590 | 16.8688 | 20.1615 | 90.42 | 89.61 | 94.51 | 93.65 | -0.0273 | -0.2014 | 18.4570 | 0.5751 |
| 162.00                 | 0.0      | 0.0000   | 28.0981 | 21.4655 | 17.1354 | 20.4286 | 90.42 | 90.61 | 94.51 | 94.67 | -0.0266 | -0.0635 | 18.4570 | 0.5751 |
| 163.00                 | 0.0      | 0.0000   | 27.0981 | 21.4655 | 17.1354 | 20.4286 | 90.42 | 90.61 | 94.51 | 94.67 | -0.0260 | -0.0625 | 18.4570 | 0.5751 |
| 164.00                 | 0.0      | 0.0000   | 26.0981 | 21.4655 | 17.1354 | 20.4286 | 90.42 | 90.61 | 94.51 | 94.67 | -0.0253 | -0.0616 | 18.4570 | 0.5751 |
| 165.00                 | 0.0      | 0.0000   | 25.0981 | 21.4655 | 17.1354 | 20.4286 | 90.42 | 90.61 | 94.51 | 94.67 | -0.0247 | -0.0606 | 18.4570 | 0.5751 |
| 166.00                 | 0.0      | 0.0000   | 24.0981 | 21.4655 | 17.1354 | 20.4286 | 90.42 | 90.61 | 94.51 | 94.67 | -0.0240 | -0.0597 | 18.4570 | 0.5751 |
| 167.00                 | 0.0      | 0.0000   | 23.0981 | 21.4655 | 17.1354 | 20.4286 | 90.42 | 90.61 | 94.51 | 94.67 | -0.0234 | -0.0587 | 18.4570 | 0.5751 |
| 168.00                 | 0.0      | 0.0000   | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 90.42 | 91.19 | 94.51 | 95.28 | -0.0227 | 0.0265  | 18.4570 | 0.5751 |
| STARTING TURN = 169.00 |          |          |         |         |         |         |       |       |       |       |         |         |         |        |
| TINTRN = 0.0           |          |          |         |         |         |         |       |       |       |       |         |         |         |        |
| 169.00                 | -30.0000 | -7.8427  | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 90.17 | 90.95 | 94.24 | 95.02 | -0.0222 | 0.0282  | 18.4570 | 0.5751 |
| 170.00                 | -30.0000 | -13.6351 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 89.52 | 90.30 | 93.54 | 94.33 | -0.0244 | 0.0292  | 18.4570 | 0.5751 |
| 171.00                 | -30.0000 | -17.9133 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 88.57 | 89.36 | 92.52 | 93.32 | -0.0239 | 0.0290  | 18.4570 | 0.5751 |
| 172.00                 | -30.0000 | -21.0730 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 87.39 | 88.20 | 91.26 | 92.07 | -0.0269 | 0.0271  | 18.4570 | 0.5751 |
| 173.00                 | -30.0000 | -23.4068 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 86.06 | 86.88 | 89.62 | 90.66 | -0.0320 | 0.0233  | 18.4570 | 0.5751 |
| 174.00                 | -30.0000 | -25.1304 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 84.60 | 85.44 | 88.26 | 89.11 | -0.0392 | 0.0173  | 18.4570 | 0.5751 |
| 175.00                 | -30.0000 | -26.4034 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 83.06 | 83.92 | 86.60 | 87.48 | -0.0487 | 0.0090  | 18.4570 | 0.5751 |
| 176.00                 | -30.0000 | -27.3436 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 81.46 | 82.34 | 84.61 | 85.77 | -0.0606 | -0.0017 | 18.4570 | 0.5751 |
| 177.00                 | -30.0000 | -28.0381 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 79.81 | 80.70 | 83.09 | 84.01 | -0.0750 | -0.0149 | 18.4570 | 0.5751 |
| 178.00                 | -30.0000 | -28.5510 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 78.13 | 79.04 | 81.26 | 82.21 | -0.0921 | -0.0308 | 18.4570 | 0.5751 |
| 179.00                 | -30.0000 | -28.9299 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 76.42 | 77.36 | 79.41 | 80.38 | -0.1117 | -0.0492 | 18.4570 | 0.5751 |
| 180.00                 | -30.0000 | -29.2090 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 74.70 | 75.65 | 77.54 | 78.54 | -0.1339 | -0.0703 | 18.4570 | 0.5751 |
| 181.00                 | -30.0000 | -29.4162 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 72.97 | 73.94 | 75.66 | 76.67 | -0.1568 | -0.0940 | 18.4570 | 0.5751 |
| 182.00                 | -30.0000 | -29.5688 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 71.23 | 72.21 | 73.76 | 74.80 | -0.1863 | -0.1203 | 18.4570 | 0.5751 |
| 183.00                 | -30.0000 | -29.6815 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 69.48 | 70.48 | 71.85 | 72.92 | -0.2165 | -0.1493 | 18.4570 | 0.5751 |
| 184.00                 | -30.0000 | -29.7648 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 67.72 | 68.75 | 69.94 | 71.03 | -0.2492 | -0.1809 | 18.4570 | 0.5751 |
| 185.00                 | -30.0000 | -29.8263 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 65.97 | 67.02 | 68.02 | 69.14 | -0.2846 | -0.2152 | 18.4570 | 0.5751 |
| 186.00                 | -30.0000 | -29.8717 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 64.21 | 65.28 | 66.10 | 67.24 | -0.3225 | -0.2519 | 18.4570 | 0.5751 |
| 187.00                 | -30.0000 | -29.9052 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 62.46 | 63.54 | 64.18 | 65.34 | -0.3629 | -0.2913 | 18.4570 | 0.5751 |
| 188.00                 | -30.0000 | -29.9300 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 60.70 | 61.81 | 62.25 | 63.44 | -0.3738 | -0.3052 | 18.4570 | 0.5751 |
| 189.00                 | -30.0000 | -29.9483 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 58.94 | 60.07 | 60.33 | 61.54 | -0.3290 | -0.2563 | 18.4570 | 0.5751 |
| 190.00                 | -30.0000 | -29.9618 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 57.19 | 58.33 | 58.40 | 59.64 | -0.2865 | -0.2137 | 18.4570 | 0.5751 |
| 191.00                 | -30.0000 | -29.9718 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 55.43 | 56.60 | 56.47 | 57.74 | -0.2465 | -0.1716 | 18.4570 | 0.5751 |
| 192.00                 | -30.0000 | -29.9792 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 53.68 | 54.86 | 54.54 | 55.83 | -0.2085 | -0.1319 | 18.4570 | 0.5751 |



| T                                     | PHC      | PHI      | TLEGI   | TTURN1  | Y021    | TT21    | HTG   | HEG   | HTA   | HEA   | ETPUE   | EEST    | PH01    | PH02   |
|---------------------------------------|----------|----------|---------|---------|---------|---------|-------|-------|-------|-------|---------|---------|---------|--------|
| 193.00                                | -30.0000 | -29.9846 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 51.92 | 53.13 | 52.61 | 53.93 | -0.1739 | -0.0947 | 18.4570 | 0.5751 |
| 194.00                                | -30.0000 | -29.9886 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 50.17 | 51.39 | 50.68 | 52.02 | -0.1414 | -0.0600 | 18.4570 | 0.5751 |
| 195.00                                | -30.0000 | -29.9916 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 48.41 | 49.66 | 48.75 | 50.12 | -0.1115 | -0.0279 | 18.4570 | 0.5751 |
| 196.00                                | -30.0000 | -29.9938 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 46.66 | 47.92 | 46.82 | 48.21 | -0.0842 | 0.0016  | 18.4570 | 0.5751 |
| 197.00                                | -30.0000 | -29.9954 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 44.90 | 46.19 | 44.89 | 46.31 | -0.0596 | 0.0285  | 18.4570 | 0.5751 |
| 198.00                                | -30.0000 | -29.9966 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 43.15 | 44.46 | 42.96 | 44.40 | -0.0377 | 0.0527  | 18.4570 | 0.5751 |
| 199.00                                | -30.0000 | -29.9975 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 41.39 | 42.72 | 41.03 | 42.50 | -0.0184 | 0.0742  | 18.4570 | 0.5751 |
| 200.00                                | -30.0000 | -29.9982 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 39.64 | 40.99 | 39.10 | 40.59 | -0.0019 | 0.0930  | 18.4570 | 0.5751 |
| 201.00                                | -30.0000 | -29.9986 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 37.89 | 39.25 | 37.17 | 38.63 | 0.0119  | 0.1091  | 18.4570 | 0.5751 |
| 202.00                                | -30.0000 | -29.9990 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 36.12 | 37.52 | 35.24 | 36.78 | 0.0229  | 0.1225  | 18.4570 | 0.5751 |
| 203.00                                | -30.0000 | -29.9993 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 34.37 | 35.78 | 33.31 | 34.88 | 0.0311  | 0.1330  | 18.4570 | 0.5751 |
| TURN ENDING T = 204.00 TINTRN = 35.00 |          |          |         |         |         |         |       |       |       |       |         |         |         |        |

# LEG NUMBER 3

LEG START POINT (X,Y) = 50.3553 44.0156  
 LEG END POINT (X,Y) = 53.3553 52.6758  
 LEG LENGTH (NM) = 10.00  
 LEG AZIMUTH (DEG) = 30.00  
 DESIRED GROUND SPEED (FT/SEC) = 548.13  
 DESIRED AIR HEADING (DEG) = 28.52  
 AVG RANGE OF LEG FROM RADAR (NM) = 71.63  
 AVG AZIMUTH OF LEG FROM RADAR (DEG) = 47.35  
 TLES = 110.852

| T                                       | PHC | PHI      | TLEGI   | TTURN1  | Y021    | TT21    | HTG   | HEG   | HTA   | HEA   | ETPUE  | EEST   | PH01    | PH02     |
|---|-----|----------|---------|---------|---------|---------|-------|-------|-------|-------|--------|--------|---------|----------|
| 204.00                                  | 0.0 | -22.1568 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 32.85 | 34.28 | 31.64 | 33.23 | 0.0368 | 0.1410 | 18.4570 | 0.5751   |
| 205.00                                  | 0.0 | -16.3645 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 31.73 | 33.18 | 30.41 | 32.02 | 0.0403 | 0.1469 | 18.4570 | 0.5751   |
| 206.00                                  | 0.0 | -12.0864 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 30.90 | 32.36 | 29.51 | 31.12 | 0.0424 | 0.1513 | 18.4570 | 0.5751   |
| 207.00                                  | 0.0 | -8.9267  | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 30.29 | 31.76 | 28.84 | 30.46 | 0.0433 | 0.1546 | 18.4570 | 0.5751   |
| 208.00                                  | 0.0 | -6.5931  | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 29.84 | 31.31 | 28.34 | 29.97 | 0.0434 | 0.1570 | 18.4570 | 0.5751   |
| 209.00                                  | 0.0 | -4.8695  | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 29.50 | 30.98 | 27.97 | 29.61 | 0.0426 | 0.1583 | 18.4570 | 0.5751   |
| 210.00                                  | 0.0 | -3.5965  | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 29.26 | 30.74 | 27.70 | 29.34 | 0.0419 | 0.1601 | 18.4570 | 0.5751   |
| TURN COMPLETE T = 211.00 TINTRN = 42.00 |     |          |         |         |         |         |       |       |       |       |        |        |         |          |
| 211.00                                  | 0.0 | -2.6563  | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 29.08 | 30.56 | 27.50 | 29.14 | 0.0405 | 0.1612 | 18.4570 | 0.5751   |
| 212.00                                  | 0.0 | -1.9619  | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.94 | 30.42 | 27.36 | 29.00 | 0.0390 | 0.1619 | -5.9740 | -25.4310 |
| 213.00                                  | 0.0 | -1.4490  | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.84 | 30.32 | 27.25 | 28.89 | 0.0372 | 0.1625 | -6.5221 | 0.4519   |
| 214.00                                  | 0.0 | -1.0702  | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.77 | 30.25 | 27.17 | 28.81 | 0.0353 | 0.1630 | -6.2055 | 0.5166   |





| T      | PHC | PH1     | TLEG1   | TURN1   | T021    | HTG   | HEG   | HTA   | HEA   | ETRUE   | EECT    | PH01    | PH02    |
|--------|-----|---------|---------|---------|---------|-------|-------|-------|-------|---------|---------|---------|---------|
| 215.00 | 0.0 | -0.7904 | 20.9781 | 21.6161 | 17.2921 | 28.71 | 30.20 | 27.11 | 28.75 | 0.0334  | 0.1433  | -5.9893 | 0.2162  |
| 216.00 | 0.0 | -0.5838 | 20.9781 | 21.6161 | 17.2921 | 28.67 | 30.17 | 27.06 | 28.71 | 0.0313  | 0.1675  | -5.8476 | 0.1417  |
| 217.00 | 0.0 | -0.4312 | 20.9781 | 21.6161 | 17.2921 | 28.64 | 30.14 | 27.03 | 28.68 | 0.0292  | 0.1677  | -5.8958 | -0.0482 |
| 218.00 | 0.0 | -0.3185 | 20.9781 | 21.6161 | 17.2921 | 28.62 | 30.12 | 27.01 | 28.66 | 0.0270  | 0.1674  | -5.8510 | 0.0448  |
| 219.00 | 0.0 | -0.2352 | 20.9781 | 21.6161 | 17.2921 | 28.61 | 30.10 | 26.99 | 28.64 | 0.0249  | 0.1681  | -5.8375 | 0.0135  |
| 220.00 | 0.0 | -0.1737 | 20.9781 | 21.6161 | 17.2921 | 28.60 | 30.09 | 26.98 | 28.63 | 0.0227  | 0.1683  | -5.8477 | -0.0101 |
| 221.00 | 0.0 | -0.1283 | 20.9781 | 21.6161 | 17.2921 | 28.59 | 30.08 | 26.97 | 28.62 | 0.0204  | 0.1684  | -5.9757 | -0.0281 |
| 222.00 | 0.0 | -0.0948 | 20.9781 | 21.6161 | 17.2921 | 28.58 | 29.62 | 26.96 | 28.11 | 0.0182  | 0.0906  | -5.9176 | -0.0419 |
| 223.00 | 0.0 | -0.0700 | 20.9781 | 21.6161 | 17.2921 | 28.57 | 29.61 | 26.95 | 28.11 | 0.0160  | 0.0900  | -1.5235 | 4.3342  |
| 224.00 | 0.0 | -0.0517 | 20.9781 | 21.6161 | 17.2921 | 28.57 | 29.61 | 26.95 | 28.10 | 0.0137  | 0.0894  | -1.5250 | -0.0015 |
| 225.00 | 0.0 | -0.0382 | 20.9781 | 21.6161 | 17.2921 | 28.57 | 29.61 | 26.95 | 28.10 | 0.0115  | 0.0888  | -1.5318 | -0.0068 |
| 226.00 | 0.0 | -0.0282 | 20.9781 | 21.6161 | 17.2921 | 28.57 | 29.60 | 26.95 | 28.10 | 0.0092  | 0.0882  | -1.5426 | -0.0109 |
| 227.00 | 0.0 | -0.0208 | 20.9781 | 21.6161 | 17.2921 | 28.57 | 29.60 | 26.94 | 28.10 | 0.0070  | 0.0875  | -1.5567 | -0.0141 |
| 228.00 | 0.0 | -0.0154 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.20 | 26.94 | 27.66 | 0.0047  | 0.0148  | -1.5733 | -0.0166 |
| 229.00 | 0.0 | -0.0114 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.20 | 26.94 | 27.66 | 0.0025  | 0.0135  | 2.6610  | 4.2344  |
| 230.00 | 0.0 | -0.0084 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.20 | 26.94 | 27.66 | 0.0002  | 0.0123  | 2.7037  | 0.0427  |
| 231.00 | 0.0 | -0.0062 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.20 | 26.94 | 27.66 | -0.0021 | 0.0110  | 2.7468  | 0.0431  |
| 232.00 | 0.0 | -0.0046 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.20 | 26.94 | 27.65 | -0.0043 | 0.0097  | 2.7905  | 0.0438  |
| 233.00 | 0.0 | -0.0034 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.20 | 26.94 | 27.65 | -0.0066 | 0.0084  | 2.8352  | 0.0447  |
| 234.00 | 0.0 | -0.0025 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.09 | 26.94 | 27.54 | -0.0088 | -0.0143 | 2.8809  | 0.0457  |
| 235.00 | 0.0 | -0.0018 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.09 | 26.94 | 27.54 | -0.0111 | -0.0158 | 4.2371  | 1.3561  |
| 236.00 | 0.0 | -0.0014 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.09 | 26.94 | 27.54 | -0.0134 | -0.0173 | 4.3071  | 0.0701  |
| 237.00 | 0.0 | -0.0010 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.09 | 26.94 | 27.54 | -0.0156 | -0.0187 | 4.3794  | 0.0723  |
| 238.00 | 0.0 | -0.0007 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.09 | 26.94 | 27.54 | -0.0179 | -0.0202 | 4.4541  | 0.0746  |
| 239.00 | 0.0 | -0.0005 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.09 | 26.94 | 27.54 | -0.0202 | -0.0216 | 4.5312  | 0.0771  |
| 240.00 | 0.0 | -0.0004 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 28.85 | 26.94 | 27.28 | -0.0224 | -0.0201 | 4.6110  | 0.0798  |
| 241.00 | 0.0 | -0.0003 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 28.85 | 26.94 | 27.28 | -0.0247 | -0.0219 | 7.7633  | 3.1523  |
| 242.00 | 0.0 | -0.0002 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 28.85 | 26.94 | 27.28 | -0.0270 | -0.0237 | 7.9061  | 0.1427  |
| 243.00 | 0.0 | -0.0002 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 28.85 | 26.94 | 27.28 | -0.0292 | -0.0256 | 8.0541  | 0.1481  |
| 244.00 | 0.0 | -0.0001 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 28.85 | 26.94 | 27.28 | -0.0315 | -0.0274 | 8.2078  | 0.1537  |
| 245.00 | 0.0 | -0.0001 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 28.85 | 26.94 | 27.28 | -0.0337 | -0.0293 | 8.3675  | 0.1597  |
| 246.00 | 0.0 | -0.0001 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.26 | 26.94 | 27.73 | -0.0360 | 0.0026  | 8.5335  | 0.1660  |
| 247.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.26 | 26.94 | 27.73 | -0.0383 | 0.0014  | 2.8279  | -5.7030 |
| 248.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.26 | 26.94 | 27.73 | -0.0405 | 0.0002  | 2.8856  | 0.0377  |
| 249.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 28.56 | 29.26 | 26.94 | 27.73 | -0.0428 | -0.0010 | 2.9453  | 3.0631  |



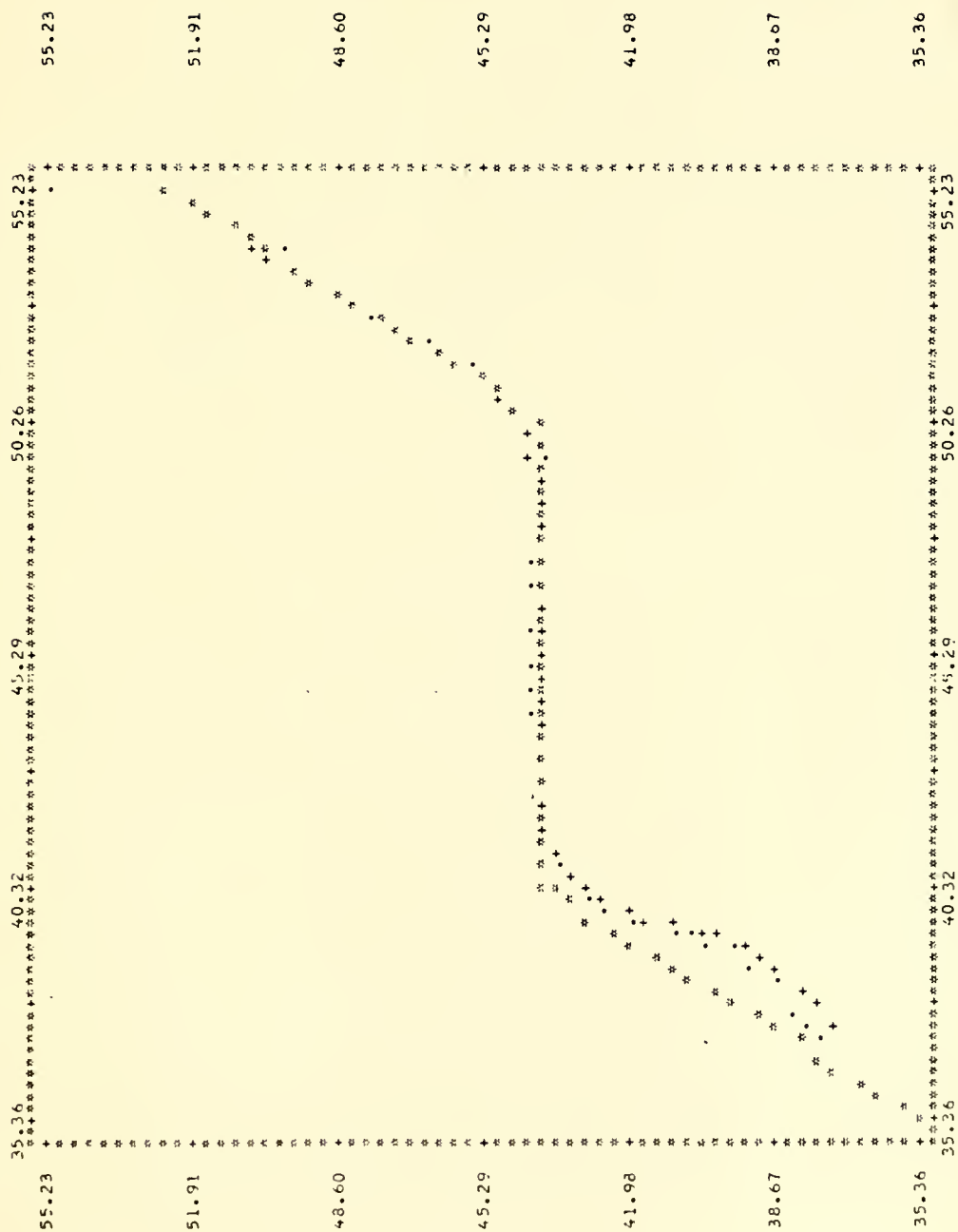
| Y      | PHC | PHI     | YLEG1   | YUON1   | YQ21    | YT21    | HTG   | HEG   | HTA   | HEA   | ETRUE   | EFST    | PHD1    | PHQ2    |
|--------|-----|---------|---------|---------|---------|---------|-------|-------|-------|-------|---------|---------|---------|---------|
| 250.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.26 | 26.94 | 27.73 | -0.0451 | -0.0021 | 3.3085  | 0.0627  |
| 251.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.26 | 26.94 | 27.73 | -0.0473 | -0.0033 | 3.0739  | 0.0654  |
| 252.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.13 | 26.94 | 27.58 | -0.0496 | -0.0281 | 3.1422  | 0.0685  |
| 253.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.13 | 26.94 | 27.58 | -0.0518 | -0.0295 | 5.3606  | 1.9184  |
| 254.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.13 | 26.94 | 27.58 | -0.0541 | -0.0309 | 5.1768  | 0.1162  |
| 255.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.13 | 26.94 | 27.56 | -0.0564 | -0.0322 | 5.2985  | 0.1217  |
| 256.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.13 | 26.94 | 27.58 | -0.0586 | -0.0336 | 5.4260  | 0.1275  |
| 257.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.13 | 26.94 | 27.58 | -0.0609 | -0.0350 | 5.5598  | 0.1338  |
| 258.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.37 | 26.94 | 27.84 | -0.0632 | 0.0136  | 5.7004  | 0.1406  |
| 259.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.37 | 26.94 | 27.84 | -0.0654 | 0.0126  | 1.6404  | -4.0600 |
| 260.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.37 | 26.94 | 27.84 | -0.0677 | 0.0116  | 1.6840  | 0.0436  |
| 261.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.37 | 26.94 | 27.84 | -0.0700 | 0.0106  | 1.7300  | 0.0459  |
| 262.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.37 | 26.94 | 27.84 | -0.0722 | 0.0096  | 1.7785  | 0.0485  |
| 263.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.37 | 26.94 | 27.84 | -0.0745 | 0.0086  | 1.9298  | 0.0513  |
| 264.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.39 | 26.94 | 27.86 | -0.0767 | 0.0131  | 1.8842  | 0.0544  |
| 265.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.39 | 26.94 | 27.86 | -0.0790 | 0.0121  | 1.9328  | -0.4514 |
| 266.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.39 | 26.94 | 27.86 | -0.0813 | 0.0112  | 1.4778  | 0.0451  |
| 267.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.39 | 26.94 | 27.86 | -0.0835 | 0.0102  | 1.5258  | 0.0480  |
| 268.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.39 | 26.94 | 27.86 | -0.0858 | 0.0092  | 1.3771  | 0.0512  |
| 269.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.39 | 26.94 | 27.86 | -0.0881 | 0.0083  | 1.6318  | 0.0548  |
| 270.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.56 | 26.94 | 28.04 | -0.0903 | 0.0462  | 1.6906  | 0.0587  |
| 271.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.56 | 26.94 | 28.04 | -0.0926 | 0.0455  | -2.5292 | -4.2198 |
| 272.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.56 | 26.94 | 28.04 | -0.0948 | 0.0447  | -2.6261 | -0.0969 |
| 273.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.55 | 26.94 | 28.04 | -0.0971 | 0.0440  | -2.7307 | -0.1046 |
| 274.00 | 0.0 | -0.0000 | 20.9781 | 21.6161 | 17.2921 | 20.5857 | 28.56 | 29.56 | 26.94 | 28.04 | -0.0994 | 0.0433  | -2.8440 | -0.1133 |

MS ETRUE = 0.480284

MS EEST = 0.366266



LENTZ AN/TPQ-27  
 DESIRED, TRUE, AND ESTIMATED POSITION











```

DATA G1,G2,TLVL,TLVL1,THA,TTHD,TP,ENSTP/75.,75.,2.,3.,0.,
1 13.5,0.,12./
DATA CTV,XE,XEQ,XEEXP,N,DXE,HDE,HDEOLD,HDEDOT,PHDAVG/9*0.00/
DATA PHD1,PHD2,PHD/3*0.00/
DATA ZIP/0.00/

C-----PRIMARY ARRAY DEFINITIONS
C X1: STATE ESTIMATION VECTOR IN RADAR COORDINATES
C X2: TRUE COORDINATES OF AIRCRAFT IN RADAR FRAME
C X3: TRUE COORDINATES OF AIRCRAFT IN TARGET FRAME
C X4: USED FOR TEMPORARY STORAGE ONLY
C X5: ESTIMATED COORDINATES OF THE TARGET IN THE "PRIMED" FRAME
C X6: ESTIMATED COORDINATES OF TARGET IN THE "DOUBLE PRIMED" SYSTEM
C X7: ESTIMATED TARGET-AIRCRAFT VECTOR IN RADAR FRAME

C EV1: TRUE TARGET COORDINATES IN THE RADAR FRAME
C WH: TRUE WIND VECTOR IN THE TARGET FRAME
C WH: ESTIMATED WIND VECTOR IN THE TARGET FRAME
C WR: ESTIMATED WIND VECTOR IN THE RADAR FRAME

C-----NON-ZERO COMMON INITIALIZATIONS
C ITH=-1
C TG=1000.0
C N=16
C IEX=1
C ISTF=0
C NAC=4
C ERGR=1.0-06
C XMXX=3000.00
C NWLD=-1
C IU=635897

C-----READ DATA FOR PROBLEM STARTING WITH POSITION AND RADAR VALUES
C READ(5,2) WT,WH
C READ(5,2) BIS,SIG(4),SIG(5),SIG(6)
C READ(5,2) SIG(1),SIG(2),SIG(3)
C READ(5,2) SIGW
C READ(5,2) X3
C READ(5,2) XD3
C READ(5,2) PHB,TB,DT,DTCON,PHI,TWLD,MWLD

C-----READ GIVE MODE DATA
C READ(5,2) T3,THNM,THDM,THD,ATT,ATH
C READ(5,102) ANH,TUP,HTOL,ATOL,S,IB1,IACC

C-----READ TITLES FOR PLOTTED OUTPUT
C READ(5,101) ATITLE,BITITLE,CTITLE,DTITLE,ETITLE,FTITLE,
LENT0490
LENT0500
LENT0510
LENT0520
LENT0530
LENT0540
LENT0550
LENT0560
LENT0570
LENT0580
LENT0590
LENT0600
LENT0610
LENT0620
LENT0630
LENT0640
LENT0650
LENT0660
LENT0670
LENT0680
LENT0690
LENT0700
LENT0710
LENT0720
LENT0730
LENT0740
LENT0750
LENT0760
LENT0770
LENT0780
LENT0790
LENT0800
LENT0810
LENT0820
LENT0830
LENT0840
LENT0850
LENT0860
LENT0870
LENT0880
LENT0890
LENT0900
LENT0910
LENT0920
LENT0930
LENT0940
LENT0950
LENT0960

```



```

1GTITLE,HTITLE,OTITLE,PTITLE,QTITLE,RTITLE,STITLE,TITLE,UTITLE,
2VTITLE,WTITLE,XTITLE,YTITLE,ZTITLE
C-----READ BOMBING DATA TABLE CONSTANTS AND FIND CORRECT TABLE
READ(5,102) WBLX,WBLY,BFF,D,W,NTB
READ(5,9)NTABS,(NTAB(I),NENT(I),I=1,NTABS)
DO 100 I=1,NTABS
  NNT=NENT(I)
100 READ(5,1)(XKD(J,I),GKD(J,I),J=1,NNT)
  IF(NTB.EQ.NTBP) GO TO 114
  NTBP=NTB
  DO 111 I=1,NNTABS
    IF(NTB.EQ.NTAB(I)) GO TO 112
111 CONTINUE
  WRITE(6,90)NTB
  GO TO 99
112 NNT=NENT(I)
  DO 113 J=1,NNT
    EKDTAB(J)=GKD(J,I)
113 VKDTAB(J)=XKD(J,I)
114 IPLC=NNT/2
  IDTCN=DTCON/DT+0.5
C-----TH IS THE ANGLE BETWEEN THE TARGET AND THE RADAR
TH=THNN/THDM
STH=DSIN(TH/DEG)
CTH=DCOS(TH/DEG)
C-----SET UP MATRIX FOR COORDINATE TRANSFORMATION
EM1(1,1)=1.DC
EM1(2,2)=CTH
EM1(2,3)=STH
EM1(3,2)=-STH
EM1(3,3)=CTH
C
EV1(1)=0.DC
EV1(2)=RE*STH
EV1(3)=-RE+RE*CTH
C
DO 11 I=1,3
  DO 11 J=1,3
    EM2(I,J)=EM1(J,I)
    EM3(I,J)=0.DC
11 IF(I.EQ.J) EM3(I,J)=1.DC
C-----PHI IS RADAR LATITUDE
SPH=DSIN(PHI/DEG)

```



```

C-----CPH=DCOS(PHI/DEG)
C-----TRANSFORM ESTIMATED WIND VALUES FROM TARGET TO
C-----RADAR COORDINATE SYSTEM.
C-----CALL MATMLT(EM1,WH,WR)
C-----PRINT OUT INITIAL VALUES AND CONSTANTS FOR THE PROBLEM
1WRITE(6,5) WT,WH,MWLD,TWLD,SIG(1),SIG(2),SIG(3),BIS,
  SIG(4),SIG(5),SIG(6),SIGW,DT,X3,XD3
1WRITE(6,60) TB,PHB
1WRITE(6,61) DTCCN,G1,G2
1WRITE(6,62) WBLY,BFF,D,W,NTB
1WRITE(6,63) THD,ATT,ATH,ANH,TUP,HTOL,ATOL,THNM,
  THDM,IBL,IACC
C-----DIVE EQUATION CONSTANTS
C-----IBL=0 WHEN IN LEVEL BOMBING MODE
1IF(THD.GT.0.D0) IBL=1
1D2W=D*D/(144.D0*W)*BFF
C-----CD4=THD/DEG
C-----CD1=DEXP(ATH*CD4/ANH)
C-----CD2={CD1-1.D0}/ATH
C-----CTHD=DCOS(CD4)
C-----STHD=DSIN(CD4)
C-----TTHD=STHD/CTHD
C-----CD4=(ATH+ATH)/(ANH*ANH+4.D0*ATH*ATH)
C-----CD3=CD4*(CD1*CD1*(CTHD+.5D0*ANH/ATH*STHD)-1.D0)
C-----CD4=CD4*(CD1*CD1*(STHD-.5D0*ANH/ATH*CTHD)+.5D0*ANH/ATH)
C-----ATTL=ATOL/(DEG*CTHD*CTHD)
C-----*****
C-----BEGIN MAJOR LOOP
12 ITH=ITH+1
C-----CALL ARCRFT
C-----TRANSFORM FROM TARGET TO RADAR COORDINATE SYSTEM
C-----CALL MATMAD(EM1,EV1,X3,X2)
C-----CALL MATMLT(EM1,XD3,XD2)
C-----ITH=0 ON FIRST TIME THROUGH LOOP
C-----ITH=N ON NTH TIME THROUGH LOOP
C-----ITH=-1 ON LAST TIME THROUGH LOOP
C-----IF(ITH.GE.0) GO TO 14
C-----SET UP INDICES AND VECTORS FOR LAST TIME THROUGH LOOP

```



LENT11930  
 LENT11940  
 LENT11950  
 LENT11960  
 LENT11970  
 LENT11980  
 LENT11990  
 LENT12000  
 LENT12010  
 LENT12020  
 LENT12030  
 LENT12040  
 LENT12050  
 LENT12060  
 LENT12070  
 LENT12080  
 LENT12090  
 LENT12100  
 LENT12110  
 LENT12120  
 LENT12130  
 LENT12140  
 LENT12150  
 LENT12160  
 LENT12170  
 LENT12180  
 LENT12190  
 LENT12200  
 LENT12210  
 LENT12220  
 LENT12230  
 LENT12240  
 LENT12250  
 LENT12260  
 LENT12270  
 LENT12280  
 LENT12290  
 LENT12300  
 LENT12310  
 LENT12320  
 LENT12330  
 LENT12340  
 LENT12350  
 LENT12360  
 LENT12370  
 LENT12380  
 LENT12390  
 LENT12400

```

125 DO 13 I=1,3
    WH(I)=WT(I)
    CALL MATMLT(EM1,WH,WR)
    X1(I)=X2(I)
13  XDI(I)=XD2(I)
    JTH=8
    KTH=32
    ITH=-1
    GO TO 15
C-----GENERATE A TOTAL OF MWLD "WILD" POINTS BEGINNING AT TIME TWLD
C  MWLD SET EQUAL TO MWLD AND DECREMENTED UNTIL NEGATIVE
C  AT THAT TIME WILD POINTS STOP
14  IF(T.NE.TWLD) GO TO 141
    MWLD=MWLD-1
141 MWLD=MWLD-1
C  CALL RADAR9
C-----COMPUTE RADAR ESTIMATION ERROR RESIDUALS
    DUMSUM=0.00
    IF(ITH.EQ.0) WRITE(6,8)
    NSAMPL=NSAMPL+1
    DO 142 I=1,3
        FILRES(I)=X1(I)-X2(I)
        DUMSUM=DUMSUM+FILRES(I)**2
142  SUMSOR(I)=SUMSOR(I)+FILRES(I)**2
        FILRES(I)=DSORT(DUMSUM)
        SUMSOR(4)=SUMSOR(4)+DUMSUM
    IF(ITH.EQ.0) GO TO 18
C-----X7 CONTAINS ESTIMATE OF TARGET-AIRCRAFT COORDINATES
C  IN THE RADAR FRAME.
15  DO 16 I=1,3
16  X7(I)=EVI(I)-X1(I)
C-----X5 CONTAINS COORDINATES OF THE TARGET IN THE AIRCRAFT
C  (PRIMED) REFERENCE FRAME.
    CALL MATMLT(EM2,X7,X5)
    CALL MATMLT(EM2,XDI,XD5)
C  CA=DSORT(XD5(1)*XD5(1)+XD5(2)*XD5(2))
    SA=XD5(1)/CA
    CA=XD5(2)/CA
    EM3(1,1)=CA
    EM3(1,2)=-SA
    EM3(2,1)=SA
    EM3(2,2)=CA
  
```





```

C-----X6 CONTAINS COORDINATES OF THE TARGET IN THE AIRCRAFT FRAME,
C ROTATED SUCH THAT THE XD6(2) VECTOR POINTS AT THE TARGET.
C NOTE: XD5 AND XD6 ARE ACTUALLY NEGATIVE DERIVATIVES OF XD5/XD6
C CALL MATMLT(EM3,X5,X6)
C CALL MATMLT(EM3,XD5,XD6)
C
C AA=DEG*DARCS(CA)
C EM3(1,2)=-EM3(1,2)
C EM3(2,1)=-EM3(2,1)
C
C X4(1)=0.D0
C X4(2)=XD6(2)
C X4(3)=XD6(3)
C
C-----PUT DATA BACK INTO UNROTATED A/C COORDINATES
C CALL MATMLT(EM3,X4,XD5)
C
C HATS=HAT
C IF(IBM1.EQ.0.CP.IBM1.EQ.2) HAT=-X6(3)
C
C-----BYPASS DIVE EQUATIONS WHEN IBM1=0
C IF(IBM1.NE.1) GO TO 165
C I2=XD6(2)*CD2
C DY2=XD6(2)*XD6(2)
C DZ2=CD4*DY2
C DY2=CD3*DY2
C V2=XD6(2)+ATH*T2
C V3=V2+ATH*T3
C DY3=.5D0*T3*(V2+V3)
C DZ3=DY3*SCTHD
C DY3=DY3*SCTHD
C VV=-V3*SCTHD
C VV=-V3*SCTHD
C HAT=-X6(3)-DZ2-DZ3
C X4(1)=VH*SA-WH(1)
C X4(2)=VH*CA-WH(2)
C X4(3)=VV
C GO TO 170
C-----SUBTRACT EST WIND VALUES AT ALT OF TARGET IN A/C COORDINATES
C 165 DO 17 I=1,3
C 17 X4(I)=XD5(I)-WH(I)
C 170 VE2=X4(1)*X4(1)+X4(2)*X4(2)
C
C-----VEH IS HORIZONTAL AIRSPEED
C VE IS TOTAL AIRSPEED
C DOWNWARD VELOCITY ANGLE(THETA) IS SET TO ZERO IN LEVEL BOMB MODE

```



```

C      HA IS TOTAL HEIGHT OF TARGET ABOVE SEA LEVEL
      VEH=DSQRT(VE2)
      SG=X4(1)/VEH
      CG=X4(2)/VEH
      SAG=SA*CG-CA*SG
      CAG=CA*CG+SA*SG
      IF(1B1.NE.2.OR.XD6(3).GE.--.100*VEH)      GO TO 171
      1B1=3
      TP=T
      HAT=HATS
      171 VE2=VE2+X4(3)*X4(3)
      VE=DSQRT(VE2)
      THE=0.00
      IF(ITH.LT.0.OR.1B1.GT.1)      THE=DATAN2(X4(3),VEH)*DEG
      IF(1B1.EQ.0.AND.ITH.GE.0)      X4(3)=0.00
      HA=HAT+HT
      VDR(1,2)=HA
      VDR(1,3)=VEH
      VDR(1,4)=X4(3)
C-----BRANCH AROUND TIME OF FALL(TF) AND BALLISTIC RANGE(RA)
C      EQUATIONS WHEN TOTAL ELAPSED TIME IS LESS THAN 2 SECONDS
      IF(ITH.LT.0)      GO TO 173
      IF(ITH.LE.49)      GO TO 18
C-----TF AND RA ARE COMPUTED ON EACH LOOP, THROUGH THE USE OF PARTIAL
C      DERIVATIVES WHICH ARE CALCULATED EVERY 4 SECONDS, STARTING AT T=2
      173 TF=TF+((HA-DSV)*SENCO(1)+(VEH-DXSV)*SENCO(2)+(X4(3)-DZSV)*SENCO(3)
      1)
      RA=RA+((HA-DSV)*SENCO(4)+(VEH-DXSV)*SENCO(5)+(X4(3)-DZSV)*SENCO(6)
      1)
      18 JTH=JTH+1      JTH=1
      IF(JTH.EQ.9)      KTH=KTH+1
C-----BRANCH AROUND INTEGRATOR UNLESS 4 SECONDS HAVE ELAPSED SINCE LAST
      IF(KTH.LT.33)      GO TO 205
      KTH=1
C-----STORE INITIAL CONDITIONS FOR NEXT 4 SECONDS EXTRAPOLATION
      DXSV=ZSV
      DXSV=XDSV
      DZSV=ZDSV
      RARA=FSRA
      TPTF=TSTF
C-----STORE PARTIAL VALUES FOR NEXT 4 SECONDS EXTRAPOLATION
      DO 183 I=1,6

```







JENT 3850  
 JENT 3860  
 JENT 3870  
 JENT 3880  
 JENT 3890  
 JENT 3900  
 JENT 3910  
 JENT 3920  
 JENT 3930  
 JENT 3940  
 JENT 3950  
 JENT 3960  
 JENT 3970  
 JENT 3980  
 JENT 3990  
 JENT 4000  
 JENT 4010  
 JENT 4020  
 JENT 4030  
 JENT 4040  
 JENT 4050  
 JENT 4060  
 JENT 4070  
 JENT 4080  
 JENT 4090  
 JENT 4100  
 JENT 4110  
 JENT 4120  
 JENT 4130  
 JENT 4140  
 JENT 4150  
 JENT 4160  
 JENT 4170  
 JENT 4180  
 JENT 4190  
 JENT 4200  
 JENT 4210  
 JENT 4220  
 JENT 4230  
 JENT 4240  
 JENT 4250  
 JENT 4260  
 JENT 4270  
 JENT 4280  
 JENT 4290  
 JENT 4300  
 JENT 4310  
 JENT 4320

```

IF(TF.LT.0.000001)TF=0.000001
YG=WB*Y*TF+RA*CAG
DXG=WE*TF*(HAT*CPH*CA+RA*SPH)
DYG=WE*TF*(HAT*CPH*SA
DZG=WE*TF*(RA*CPH*SA
XGC=XG+DXG
YGC=YG+DYG
ZGC=DZG
IF(IB1.GT.0)      GO TO 2051

C-----COMPUTE TIME TO GO TO RELEASE BOMB(TG) AND LATERAL ERROR(XE)
TG=(X6(2)-YGC)/XD6(2)
XEC=XE
XE=XG(1)-XGC
IF(ITH.EQ.48) XELIM=.05*XE
IF(XE.LE.XELIM) IIFLG=1
IF(IIFLG.EQ.1) XEEXPN=XE
GO TO 2059

C-----FOLLOWING BLOCK OF EQUATIONS BYPASSED UNLESS IN DIVE MODE
2051 IF(IB1.GT.1)      GO TO 2052
    XE=XG(1)-XGC
    TP=(X6(2)-YGC-DY2-DY3)/XD6(2)
    TG=TP+T2+T3
    IF(TP.GT.0.00)      GO TO 2059
    IB1=2
    TP=1
    TRF=TF
    R4F=RA
    HPF=HAT
    HO=-X6(3)
    GO TO 2059
2052 IF(IB1.GT.2)      GO TO 2053
    TG=(X6(2)-YGC)/XD6(2)
    GO TO 2054
2053 TG=(X6(3)+HAT)/XD6(3)
2054 YPPA=TC*XD6(2)
    ZPPA=TC*XD6(3)
    YPPI=YPPA+YGC
    XPPM=X6(1)-XGC
    YPPM=X6(2)-YPO1
    DTG=TC+DTG
    XE=XPPM-DTG*XD6(3)*OMP*(-SENCO(4)*CAG+WBX*SENCO(1))
    IF(IB1.GT.2)      GO TO 2055
    HAT=-X6(3)+XD6(3)*TG
    GO TO 2056
  
```





```

2055 HAT=HAT+XD6(3)*DTG
2056 IF(I81.EQ.4) GO TO 2059
      IF((HAT-HPF).GT.HTOL.AND.(TTHD+XD6(3)/XD6(2)).GT.ATTL)
      I81=4
      TP=T
      THC=DEG*DATAN(-XD6(3)/XD6(2))
C-----X5 AND XD6 AT THIS POINT ARE ERRORS IN ESTIMATED A/C
C POSITION AND VELOCITY IN ROTATED A/C SYSTEM
2059 DO 206 I=1,3
      X5(I)=-X5(I)
      X6(I)=X3(I)-X5(I)
      XD6(I)=XD3(I)-XD5(I)
C-----RBT IS HORIZONTAL DISTANCE BETWEEN A/C AND TARGET
C HOEDOT IS THE ANGLE BETWEEN BOMB IMPACT AND THE TARGET IN DEGREES
C HOEDOT IS THE ANGLE BETWEEN ERROR RATE
C CTV IS CROSS TRACK VELOCITY
      PBT=DSOPT(X5(1)*X5(1)+X5(2)*X5(2))
      HDEGLD=HDE
      HDE=ARCSIN(XE/RBT)*DEG
      HOEDOT=(HDE-HDEGLD)/DT
      IF(DABS(T-6.)*LE.0.0001) HOEDOT=0.00
C-----IF T IS LESS THAN 20 SECS AND TG IS LESS THAN 2 SECS,
C SET A DUMMY TIME TO GO(TQ) EQUAL TO 3 SECS
      TQ=TG
      IF(T.GT.20.0) GO TO 207
      IF(TQ.LE.2.) TQ=3.
      GO TO 209
207 IF(ITH.LT.0)
C-----IF TG IS LESS THAN ZERO, BRANCH FOR LAST TIME THROUGH LOOP
      IF(TG.LE.0.00) GO TO 125
      IF(I81.GT.0.AND.I81.LT.4) TG=1000.00
      CTV=-XE*VEH/RBT
      DXE=(XE-XEC)/DT
      IF(DABS(T-6.)*LE.0.0001) DXE=0.00
C-----GENERATE CONTROL COMMAND BANK ANGLE ERROR RATE HOEDOT
C PHD1 IS COMPONENT BASED ON ANGLE ERROR RATE HDE
C PHD2 IS COMPONENT BASED ON ANGLE ERROR RATE
C PHD IS REQUESTED COMMAND ANGLE IN DEGREES
C GENERATE NEW COMMAND EVERY DTCON SECONDS
      IF(MOD(ITH,DTCON).NE.0) GO TO 2082
      PHD1=G1*HDE
      PHD2=G2*HOEDOT
      PHD=PHD1+PHD2

```

```

LENT 4330
LENT 4340
LENT 4350
LENT 4360
LENT 4370
LENT 4380
LENT 4390
LENT 4400
LENT 4410
LENT 4420
LENT 4430
LENT 4440
LENT 4450
LENT 4460
LENT 4470
LENT 4480
LENT 4490
LENT 4500
LENT 4510
LENT 4520
LENT 4530
LENT 4540
LENT 4550
LENT 4560
LENT 4570
LENT 4580
LENT 4590
LENT 4600
LENT 4610
LENT 4620
LENT 4630
LENT 4640
LENT 4650
LENT 4660
LENT 4670
LENT 4680
LENT 4690
LENT 4700
LENT 4710
LENT 4720
LENT 4730
LENT 4740
LENT 4750
LENT 4760
LENT 4770
LENT 4780
LENT 4790
LENT 4800

```

GOTO2059



```

C-----ILVL IS INITIALIZED TO ZERO AND SET TO 1 ONLY AFTER TIME TG
C      IS FOUND LESS THAN TLVL, WHICH IS THE TIME AT THE END ON MISSION
C      FOR WHICH NO COMMANDS ARE TO BE SENT
2082  IF(ILVL.EQ.1)      GO TO 2087
      IF(IQ.LE.TLVL)   GO TO 20855
      IF(IG.LE.TLVL)   GO TO 2086
      PHDAVG=PHDAVG+PHI
      JAVG=JAVG+1
      GO TO 2086
20855  ILVL=1
      PHD=PHDAVG/FLOAT(JAVG)
C-----COMPUTE BANK COMMAND, PHC TO NEAREST 15/128 OF A DEGREE
C      PHC IS LIMITED TO PLUS OR MINUS 30 DEGREES
2086  PHC=(PHD)*128.00/15.00+.500
      IF(PHC.LT.0.00) PHC=PHC-1.00
      PHC=PHC
      PHC=NHC
      PHC=PHC*15.00/128.00
      IF(PHC.GT.29.3828125) PHC=29.3828125
      IF(PHC.LT.-30.00) PHC=-30.00
C-----IF COMPUTED TIME TO GO IS LESS THAN THE SAMPLING INTERVAL
C      SET TG=TO
2087  IF(TG.LT.DT)      ITH=-2
      IF(TO.LT.DT)      TG=TO
C-----GO TO 209 TO PRINT OUTPUT FOR THIS TIME THROUGH LOOP
306  IF(NWLD.GT.-2)      GO TO 209
      IMCD=IMCD+1
      IF(TG.LE.1.0) IMCD=8
      IF(IMCD.NE.8) GO TO 12
      IMCD=0
      IF(ITH.LT.48) GO TO 209
C-----STORE VALUES FOR PLOTTING EVERY SECOND
      ITAB1=ITAB1+1
      XXA(ITAB1)=FILPES(1)
      XXB(ITAB1)=FILPES(2)
      XXC(ITAB1)=FILPES(3)
      XXD(ITAB1)=FILPES(4)
      XXE(ITAB1)=X6(1)
      XXF(ITAB1)=X6(2)
      YYA(ITAB1)=XEE
      YYC(ITAB1)=XEEEXPN
      YYD(ITAB1)=PHD

```

```

LENT4810
LENT4820
LENT4830
LENT4840
LENT4850
LENT4860
LENT4870
LENT4880
LENT4890
LENT4900
LENT4910
LENT4920
LENT4930
LENT4940
LENT4950
LENT4960
LENT4970
LENT4980
LENT4990
LENT5000
LENT5010
LENT5020
LENT5030
LENT5040
LENT5050
LENT5060
LENT5070
LENT5080
LENT5090
LENT5100
LENT5110
LENT5120
LENT5130
LENT5140
LENT5150
LENT5160
LENT5170
LENT5180
LENT5190
LENT5200
LENT5210
LENT5220
LENT5230
LENT5240
LENT5250
LENT5260
LENT5270
LENT5280

```



```

C-----PRINT SUMMARY OF VALUES EACH SECOND
209 PRINT 4, X1,XD1,XDD1(1),XDD1(2),
      1 X2,XD2,TF,RA,
      2 X3,XD3,XGC,YGC,
      3 X5,XD5:AA,HAI,
      4 X6,XD6:YNP,ZIP,HDE,HDEDOT,TG,VEH,THN,
      5 PHD1,PHD2,PHD,PS,PSI,ZIP,ZIP,ZIF,
      6 PH,PHI,PHC,PC,PSI,ZIP,GNY,GNZ,T
      7 XE,DXE,CTV,ZIP,GMX,GNZ,ON A PAGE, AND THE WRITE
C-----STATEMENT YIELDS A NEW PAGE
      IF(ITH.EQ.-1) GO TO 22
      LNC=LNC+1
      IF(LNC.LT.7) GO TO 21
      LNC=0
      WRITE(6,8)
C-----LIMIT OF 2000 ITERATIONS PER PROBLEM
      21 IF(ITH.LE.2000) GO TO 12
C-----CALCULATE AND PRINT FINAL ERROR SUMMARY. RESIDUAL VALUES
      22 AND BIAS ESTIMATE AT PROBLEM TERMINATION
      X1(1)=XGC
      X1(2)=YGC
      X1(3)=0.DO
      X3(3)=0.DO
      CALL MATMAD(EM3,X3,X1,X2)
      X2(3)=DSQR(X2(1)*X2(1)+X2(2)*X2(2))
      DO 10 I=1,4
      SUMSQ(I)=DSQR(SUMSQ(I)/NSAMPL)
1010 PRINT 7,X2,SUNSQR
C-----EXECUTE PLOTS
      WRITE(6,991) ATITLE
      CALL PLOTP(XXA,XXB,ITAB1,0)

```



```

WRITE(6,991) BTITLE
CALL PLOTP(XA,XXC,ITAB1,0)
WRITE(6,991) CTITLE
CALL PLOTP(XA,XXD,ITAB1,0)
WRITE(6,991) DTITLE
CALL PLOTP(XA,XXE,ITAB1,0)
WRITE(6,991) ETITLE
CALL PLOTP(XA,XXF,ITAB1,0)
WRITE(6,991) FTITLE
CALL PLOTP(XA,XXG,ITAB1,0)
WRITE(6,991) GTITLE
CALL PLOTP(XA,XXH,ITAB1,0)
WRITE(6,991) HTITLE
CALL PLOTP(XA,XXI,ITAB1,0)
WRITE(6,991) ITITLE
CALL PLOTP(XA,XXJ,ITAB1,0)
WRITE(6,991) JTITLE
CALL PLOTP(XA,XXK,ITAB1,0)
WRITE(6,991) KTITLE
CALL PLOTP(XA,XXL,ITAB1,0)
WRITE(6,991) LTITLE
CALL PLOTP(XA,XXM,ITAB1,0)
WRITE(6,991) MTITLE
CALL PLOTP(XA,XXN,ITAB1,0)
WRITE(6,991) NTITLE
CALL PLOTP(XA,XXO,ITAB1,0)
WRITE(6,991) OTITLE
CALL PLOTP(XA,XXP,ITAB1,1)
WRITE(6,991) PTITLE
CALL PLOTP(XA,XXQ,ITAB1,2)
WRITE(6,991) QTITLE
CALL PLOTP(XA,XXR,ITAB1,3)
WRITE(6,991) RTITLE
CALL PLOTP(XA,XXS,ITAB1,1)
WRITE(6,991) STITLE
CALL PLOTP(XA,XXT,ITAB1,2)
WRITE(6,991) TTITLE
CALL PLOTP(XA,XXU,ITAB1,3)
WRITE(6,991) UTITLE
CALL PLOTP(XA,XXV,ITAB1,0)
WRITE(6,991) VTITLE
CALL PLOTP(XA,XXW,ITAB1,0)
WRITE(6,991) WTITLE
WRITE(6,991) XTITLE
WRITE(6,991) YTITLE
WRITE(6,991) ZTITLE
PRINT,992
STOP

```

99S

CON  
STOP

C-----INPUT FORMAT STATEMENTS  
C 1 FORMAT(12F6.0)

C 2 FORMAT(6F10.3)

C 3 FORMAT(6F10.3,13)

C 101 FORMAT(6A8)

```

LENT5770
LENT5780
LENT5790
LENT5800
LENT5810
LENT5820
LENT5830
LENT5840
LENT5850
LENT5860
LENT5870
LENT5880
LENT5890
LENT5900
LENT5910
LENT5920
LENT5930
LENT5940
LENT5950
LENT5960
LENT5970
LENT5980
LENT5990
LENT6000
LENT6010
LENT6020
LENT6030
LENT6040
LENT6050
LENT6060
LENT6070
LENT6080
LENT6090
LENT6100
LENT6110
LENT6120
LENT6130
LENT6140
LENT6150
LENT6160
LENT6170
LENT6180
LENT6190
LENT6200
LENT6210
LENT6220
LENT6230
LENT6240

```





```

C 102 FORMAT(5F10.3,2I3)
C-----OUTPUT FORMAT STATEMENTS
C
C 4 FORMAT(/2X, 8D16.5/(2X,8D16.5))
C
C 5 FORMAT(1H1,48X,'AN/TPQ-27 SIMULATION',//,37X,'PRECISION',
1'GUIDANCE MCDE WITH KALMAN FILTERING',//,5X,'INITIAL CONDITIONS',
2'//,6X,'TRUE WIND AT TARGET =',10X,1P3D16.5,/,8X,
3'ESTIMATED WIND AT TARGET =',5X,1P3D16.5,/,8X,
4'RADAR DATA',//,10X,
5'NUMBER OF NOISY POINTS(NWLD) =',15,/,10X,
6'START TIME OF WILD POINTS =',5X,OPF7.3,/,10X,
7'MEASUREMENT SIGMAS(R(FT.),AZ(MRAD),EL(MRAD)) =',1P3D16.5,/,10X,
8'INITIAL VELOCITY BIASES{ MEASUREMENT VALUES (SIGN) =',9X,1P3D16.5,/,
9'10X,'INITIAL FORCING ASSUMPTION VALUES (SIGN) =',5X,1P3D16.5,/,
10'10X,'RANDOM SAMPLING INTERVAL =',26X,OPF6.4,/,8X,
11'10X,'RANDOM SAMPLING OF A/C IN TARGET SYSTEM =',1P3D16.5,/,8X,
12'INITIAL POSITION OF A/C IN TARGET SYSTEM =',1P3D16.5,///)
13'INITIAL VELOCITY OF A/C IN TARGET SYSTEM =',1P3D16.5,///)
C
C 60 FORMAT(5X,'AIRCRAFT PARAMETERS :',//,9X,'TB =',F8.5,6X,'PHB =',
1F8.5,///)
C
C 61 FORMAT(5X,'CONTROL PARAMETERS:',//,9X,'DTCON =',
1F8.5,/,9X,'G1 =',F8.4,/,9X,'G2 =',F8.4,///)
C
C 62 FORMAT(5X,'BALLISTIC TABLE PARAMETERS:',//,9X,
1'BALLISTIC WIND VALUES (WBLX,WZLY) =',2F10.6,/,9X,
2'BFF =',F10.6,/,9X,'D =',2X,F10.5,/,9X,
3'W =',2X,F10.6,/,9X,'NTB =',15,///)
C
C 63 FORMAT(5X,'DIVE BOMBING MODE PARAMETERS:',//,9X,
1'THD =',F8.2,6X,'ATT =',F8.2,/,9X,
2'ATH =',F8.2,6X,'ANH =',F8.2,/,9X,
3'TUP =',F8.2,5X,'HTOL =',F8.2,/,3X,
4'ATGL =',F8.2,5X,'THNM =',F8.2,/,8X,
5'THDM =',F8.2,6X,'IB1 =',15,/,8X,
6'IACC =',15,///)
C
C 64 FORMAT(1H1,//,59X,'OUTPUT FORMAT',//,
111X,'X1',14X,'Y1',14X,'Z1',13X,'XD1',13X,'ZD1',12X,
2'XDD1',12X,'YDD1',14X,
311X,'X2',14X,'Y2',14X,'Z2',13X,'XD2',13X,'ZD2',12X,
4'XDD2',12X,'YDD2',14X,
511X,'X3',14X,'Y3',14X,'Z3',13X,'XD3',13X,'ZD3',13X,
6'XDD3',13X,'YDD3',14X,

```

```

LENT6250
LENT6260
LENT6270
LENT6280
LENT6290
LENT6300
LENT6310
LENT6320
LENT6330
LENT6340
LENT6350
LENT6360
LENT6370
LENT6380
LENT6390
LENT6400
LENT6410
LENT6420
LENT6430
LENT6440
LENT6450
LENT6460
LENT6470
LENT6480
LENT6490
LENT6500
LENT6510
LENT6520
LENT6530
LENT6540
LENT6550
LENT6560
LENT6570
LENT6580
LENT6590
LENT6600
LENT6610
LENT6620
LENT6630
LENT6640
LENT6650
LENT6660
LENT6670
LENT6680
LENT6690
LENT6700
LENT6710
LENT6720

```



```

711X,'X5','14X','Y5','14X','Z5','13X','XD5','13X','YD5','13X','ZD5','14X,
811A,'13X','HAT',/,
911X,'X5','14X','Y6','14X','Z6','13X','XD6','13X','YD6','13X','ZD6','10X,
C33X,'YNP',/,
19X,'PHD1','12X','PHD2','13X','PHD','13X','HDE','10X','HDEDOT','14X','TG',
213X,'VEH','13X','THN',/,
311X,'PH','13X','PHI','13X','PHC','14X','PS','13X','PS1',/,
411X,'XE','13X','DXE','13X','CTV','10X',/,
5'G(1,1)',10X,'G(4,2)',10X,'G(7,3)',15X,'T',/,
C
9 FORMAT(26I3)
C
7 FORMAT(/ /25X,4HX1=1PD13.5,6X,4HY1=D13.5,6X,4HRI =D13.5,
1//,20X,'AVG X RESIDUAL = ',OPF10.4,5X,'AVG Y RESIDUAL = ',
2F10.4,5X,'AVG Z RESIDUAL = ',F10.4,/,49X,
3'AVG RADIAL RESIDUAL = ',F10.4, ///)
C
90 FORMAT(/ /49X,I6,27H IS AN ILLEGAL TABLE NUMBER)
C
991 FORMAT(1H1,10X,648,/,11X,6A8,///)
C
992 FORMAT(1H1)
C
END
C
SUBROUTINE ARCPT
C
IMPLICIT REAL*8 (A-H,O-Z)
C
COMMON/AIRCOM/X3(3),XD3(3),WT(3),PHB,TB,DT,PHC,
1 TG,ITH,IBL,PH,PSD,PS,THC,ANH,ATT,TUP,THN,T
C
DATA DEG,G/57.295779513082321,32.174049/
C
-----FIRST TIME THROUGH, ITH=0
IF(ITH)5,1,4
C
-----SUBTRACT WIND VELOCITY
1 SM1=XD3(1)-WT(1)
SM2=XD3(2)-WT(2)
C

```



```

C-----VT IS AIRSPEED OF A/C
C PHB IS AUTOPILOT BANK ANGLE BIAS
C TR IS A/C RESPONSE LOOP TIME CONSTANT
C PS IS A/C RESPONSE LOOP TIME CONSTANT
C PSD IS INITIAL TURN ANGLE
C VTD IS INITIAL TURN RATE
C VTD=DSQRT(SM1*SM1+SM2*SM2)
C PH=PHB
C CA1=G/VT
C CA2=DEXP(-DT/TR)
C CA3=CA1
C CA4=DT*(12.00*DEG)
C CA5=TB*(1.00-CA2)
C DT3=.500*DT
C PSD=CA1*PH
C PS=DATA2(SM1,SM2)
C CPS=DCOS(PS)
C PS=PS*DEG
C-----EQUATIONS AND CONSTANTS FOR DIVE MODE FOLLOW
C A1=ATT*DT3
C VTC=VT
C VTH=VT
C TH=0.00
C THD=TH
C THN=TH
C THDN=TH
C SHN=TH
C CTH=1.00
C CTHN=CTH
C DTP=1.00/TUP
C CA6=DEXP(-DT/TUP)
C AND=ANH*DEG
C AN8=AND*DT
C RETURN
C-----ENTER MAIN CALCULATION STREAM
C-----PHC IS NOW THE COMMAND BANK ANGLE AT T(N-1)
C PHN IS THE NEW BANK ANGLE
C PSDN IS THE NEW TURNING RATE
C PSN IS NEW HEADING ANGLE FOR VELOCITY WITH RESPECT TO WIND
C T=T+DT
C PSN=PHB+PHC
C PHN=PSN+(PH-PSN)*CA2
C PSDN=CA1*PHN

```



```

PSN=PS+CA3*(PSN*DT+CA5*(PH-PSN))
CPSN=PSN/DEG
SPSN=DSIN(CPSN)
CPSN=DCOS(CPSN)
C-----BYPASS FOLLOWING BLOCK OF EQUATIONS UNLESS IN DIVE MODE
C IF(IB1.LE.1) GO TO 43
VTQ=VT
VTH=VT+AT1
VT=VTH+AT1
CA1=G/VTH
CA3=G/VTH
THDN=AMD/VT
THN=(THC-TH)*DTP
IF(DABS(THN).GT.THDN) GO TO 41
THDN=THN*CA6
THN=THC-TUP*THDN
GO TO 42
41 THN=AN8/VTH+TH
42 CTHN=THN/DEG
CTHN=DSIN(CTHN)
CTHN=DCOS(CTHN)
C-----UPDATE VELOCITY VECTOR FOR NEW TURN ANGLE
43 XD3(1)=WT(1)+VT*SPSN*CTHN
XD3(2)=WT(2)+VT*CPSN*CTHN
XD3(3)=-VT*STHN
C-----UPDATE POSITION VECTOR FOR NEW TURN ANGLE
SM1=DT3*(SPS*CTH+SPSN*CTHN)-CA4*(CPSN*CTHN*PSDN-SPSN*STHN*THDN-CPS
1 *CTH*(PSN+SPS*STH*THD)
1 SM2=DT3*(CPS*CTH+CPSN*CTHN)-CA4*(-SPSN*CTHN*PSDN-CPSN*STHN*THDN+
1 SPS*CTH*PSD-CPS*STH*THD)
SM3=DT3*(STH+STHN)-CA4*(CTHN*THDN-CTH*THD)
C X3(1)=DT*WT(1)+VTH*SM1+X3(1)
X3(2)=DT*WT(2)+VTH*SM2+X3(2)
X3(3)=-VTH*SM3+X3(3)
C-----RESET VALUES FOR NEXT TIME IN SUBROUTINE
PH=PHN
PS=PSN
PSD=PSDN
SPS=SPSN
CPS=CPSN
TH=THN
THD=THDN

```

LENT 7690  
 LENT 7700  
 LENT 7710  
 LENT 7720  
 LENT 7730  
 LENT 7740  
 LENT 7750  
 LENT 7760  
 LENT 7770  
 LENT 7780  
 LENT 7790  
 LENT 7800  
 LENT 7810  
 LENT 7820  
 LENT 7830  
 LENT 7840  
 LENT 7850  
 LENT 7860  
 LENT 7870  
 LENT 7880  
 LENT 7890  
 LENT 7900  
 LENT 7910  
 LENT 7920  
 LENT 7930  
 LENT 7940  
 LENT 7950  
 LENT 7960  
 LENT 7970  
 LENT 7980  
 LENT 7990  
 LENT 8000  
 LENT 8010  
 LENT 8020  
 LENT 8030  
 LENT 8040  
 LENT 8050  
 LENT 8060  
 LENT 8070  
 LENT 8080  
 LENT 8090  
 LENT 8100  
 LENT 8110  
 LENT 8120  
 LENT 8130  
 LENT 8140  
 LENT 8150  
 LENT 8160





```

STH=STHN
CTH=CTHN
RETURN

```

```

C-----ENTER THIS SECTION ONLY ON LAST TIME THROUGH MAIN LOOP
C
C
5
C-----RECOMPUTE CONSTANTS FOR LAST DELTAT

```

```

DT=TG
DT3=.5D0*DT
AN8=AND*DT
CA6=DEXP(-DT/TUP)
CA2=DEXP(-DT/TB)
CA5=TB*(1.D0-CA2)
CA4=DT*DT/(12.D0*DEG)
AT1=AT*DT2
GU TO 4
END

```

# SUBROUTINE RADAR9

```

C-----THIS SUBROUTINE SIMULATES A RADAR PROCESSOR. IT CONVERTS FROM
CARTESIAN TO SPHERICAL, ADDS NOISE, AND THEN CONVERTS BACK TO
CARTESIAN COORDINATES. DATA IS FILTERED USING A
THIRD ORDER KALMAN FILTER WITH DETERMINISTIC FORCING FROM THE
AIRCRAFT CONTROLLER INCLUDED.

```

```

IMPLICIT REAL*8 (A-H,O-Z)
REAL*4 PAN(3)

```

```

COMMON/AIRCOROM/X3(3),XD3(3),WT(3),PHB,TB,DT,PHC,
TG,ITH,IBI,PH,PSD,PS,THC,ANH,ATT,TUP,THN,T

```

```

1
COMMON/RADCOM/SIG(6),BIS(3),X2(3),XD2(3),X1(3),XD1(3),
SIGW(3),WR(3),PS1,PH1,XDD1(3),GNX,GNV,
GNZ,IU,NWLD

```

```

2
DIMENSION Q(9,9),GAMMA(9,9),ADUM(9,9),BDUM(9,9),W(9,9),
1PP(9,9),PE(9,9),H(9,9),HT(9,9),R(9,9),PHI(9,9),SIG1(3),
2PHITEN(9,9),G(9,9),XIDENT(9,9),X1P(3),XD1P(3),XD1P(3),
3XDATA(3),DELX(3)

```

```

EQUIVALENCE (XDATA(1),PR),(XDATA(2),A),(XDATA(3),E)

```



```

C      DATA DEG:GG/57.295779513082321,32.174049/
C      DATA PSDN,PSD1,PHN,PSN,SN1,SN2,SPSN,CPSN,VT1/9*0.DO/
C      DATA AMGMIN,ANGMAX/0.0000001,1.5707963/
C      IF(ITH.NE.0) GO TO 50
C-----INITIALIZE BANK ANGLE AND CONSTANTS FOR DETERMINISTIC
C      CONTROL MOTION CALCULATIONS
C      CA42=DEXP(-DT/TB)
C      CA4=DT*DT/(12.DO*DEG)
C      CA5=TB*(1.DO-CA42)
C      DT3=DT/2.DO
C-----GENERATE Q ARRAY
C      DO 1 I=1,9
C      DO 1 J=1,9
C      PE(I,J)=0.DO
C      BDUM(I,J)=0.DO
C      PP(I,J)=0.DO
C      GG(I,J)=0.DO
C      GAMMA(I,J)=0.DO
C      W(I,J)=0.DO
C      Q(I,J)=0.DO
C      DT2=DT*DT/2.DO
C      DT4=DT*DT*3/6.DO
C      W(1,1)=SIGW(1)**2
C      W(2,2)=SIGW(2)**2
C      W(3,3)=SIGW(3)**2
C      GAMMA(1,1)=DT4
C      GAMMA(2,1)=DT2
C      GAMMA(3,1)=DT2
C      GAMMA(4,2)=DT4
C      GAMMA(5,2)=DT2
C      GAMMA(6,2)=DT4
C      GAMMA(7,3)=DT2
C      GAMMA(8,3)=DT2
C      GAMMA(9,3)=DT2
C      CALL TRANS(GAMMA,9,3,ADUM)
C      CALL PROD(GAMMA,W,9,3,BDUM)
C      CALL PROD(PDUM,ADUM,9,3,9,Q)
C-----INITIALIZE COVARIANCE OF PREDICTION ARRAY (PP)
C      DO 2 I=1,9
C      DO 2 J=1,9

```

```

LENT 8650
LENT 8660
LENT 8670
LENT 8680
LENT 8690
LENT 8700
LENT 8710
LENT 8720
LENT 8730
LENT 8740
LENT 8750
LENT 8760
LENT 8770
LENT 8780
LENT 8790
LENT 8800
LENT 8810
LENT 8820
LENT 8830
LENT 8840
LENT 8850
LENT 8860
LENT 8870
LENT 8880
LENT 8890
LENT 8900
LENT 8910
LENT 8920
LENT 8930
LENT 8940
LENT 8950
LENT 8960
LENT 8970
LENT 8980
LENT 8990
LENT 9000
LENT 9010
LENT 9020
LENT 9030
LENT 9040
LENT 9050
LENT 9060
LENT 9070
LENT 9080
LENT 9090
LENT 9100
LENT 9110
LENT 9120

```



```

PP(I,J)=0.D0
2 IF(I.EQ.J) PP(I,J)=1.D06
C-----COMPUTE MEASUREMENT MATRIX AND VARIANCE
DO 3 I=1,9
DO 3 J=1,9
H(I,J)=0.D0
H(I,1)=1.D0
H(2,4)=1.D0
H(5,7)=1.D0
CALL TRANS(H,3,9,HT)
C
SIG1(1)=SIG(1)
SIG1(2)=SIG(2)*1.D-03
SIG1(3)=SIG(3)*1.D-03
VART=SIG1(1)**2
VART=SIG1(2)**2
VART=SIG1(3)**2
C-----COMPUTE STATE TRANSITION ARRAY (PHI)
DO 4 I=1,9
DO 4 J=1,9
PHI(I,J)=0.D0
IF(I.EQ.J) PHI(I,J)=1.D0
PHI(1,2)=DT
PHI(1,3)=DT
PHI(2,3)=DT
PHI(4,5)=DT
PHI(4,6)=DT
PHI(5,6)=DT
PHI(7,8)=DT
PHI(7,9)=DT
PHI(8,9)=DT
CALL TRANS(PHI,9,9,PHITRN)
C-----CREATE IDENTITY ARRAY
DO 8 I=1,9
DO 8 J=1,9
XIDENT(I,J)=0.D0
IF(I.EQ.J) XIDENT(I,J)=1.D0
C
310 PRINT 310, ((H(I,J),J=1,9),I=1,9)
FORMAT(//,10X,'H ARRAY',//,9(//,9F14.5))
311 PRINT 311, ((GAMMA(I,J),J=1,9),I=1,9)
FORMAT(//,10X,'GAMMA ARRAY',//,9(//,9F14.5))
312 PRINT 312, ((Q(I,J),J=1,9),I=1,9)
FORMAT(//,10X,'Q ARRAY',//,9(//,9F14.5))
313 PRINT 313, ((PP(I,J),J=1,9),I=1,9)

```

```

LENT9130
LENT9140
LENT9150
LENT9160
LENT9170
LENT9180
LENT9190
LENT9200
LENT9210
LENT9220
LENT9230
LENT9240
LENT9250
LENT9260
LENT9270
LENT9280
LENT9290
LENT9300
LENT9310
LENT9320
LENT9330
LENT9340
LENT9350
LENT9360
LENT9370
LENT9380
LENT9390
LENT9400
LENT9410
LENT9420
LENT9430
LENT9440
LENT9450
LENT9460
LENT9470
LENT9480
LENT9490
LENT9500
LENT9510
LENT9520
LENT9530
LENT9540
LENT9550
LENT9560
LENT9570
LENT9580
LENT9590
LENT9600

```



```

313  FORMAT(//,IOX,PP ARRAY,/,9(/,9F14.5))
      PRINT 316,((PHI(I,J),J=1,9),I=1,9)
316  FORMAT(//,IOX,PHI ARRAY,/,9(/,9F14.4))
C*****
C-----BEGIN NORMAL FILTER COMPUTATIONS
C-----COMPUTE TRUE P,AZ,EL,ADD NOISE, AND COMPUTE NOISY MEASUREMENTS
C      IN CARTESIAN COORDINATES
50  IF(NWLD,GE.O.AND.ITH.NE.O) GO TO 61
      RS=X2(1)*X2(1)+X2(2)*X2(2)
      A=DATAN2(X2(1),X2(2))
      E=DATAN2(X2(3),DSQRT(RR))
      RR=DSQRT(RR+X2(3)*X2(3))
      RM2=PR**2
C      CALL NCRNAL(IU,RAN,3)
      DO 6 I=1,3
6      XDATA(I)=XDATA(I)+BIS(I)+SIG1(I)*RAN(I)
C      IF(DABS(A).LT.ANGMIN) A=ANGMIN
      IF(DABS(E).LT.ANGMIN) E=ANGMIN
      SIGNE=A/DABS(A)
      SIGNE=E/DABS(E)
      DELA=DABS(A-ANGMAX)
      DELE=DABS(E-ANGMAX)
      IF(DELA.LT.ANGMIN) A=SIGNE*ANGMAX
      IF(DELE.LT.ANGMIN) E=SIGNE*ANGMAX
C      CA=DCOS(A)
      SA=DSIN(A)
      CE=DCOS(E)
      SE=DSIN(E)
      CA2=CA**2
      SA2=SA**2
      CE2=CE**2
      SE2=SE**2
      XDATA(3)=RR*SE*CA
      XDATA(2)=RR*CE*SA
      XDATA(1)=RR*CE*SA
C      IF(ITH.NE.O) GO TO 63
      DO 62 I=1,3
      XI(I)=XDATA(I)
      XI(I)=XI(I)
      XDIP(I)=SIG(I+3)
      XDIP(I)=0.D0
      DELX(I)=0.D0
62

```





```

IF(NWLD.GE.0) GO TO 61
C----- COMPUTE COVARIANCE OF MEASUREMENT ERROR ARRAY (R)
63 R(1,1)=RM2*(VART*SE2*SA2+VARP*CE2*CA2+VART*VARP*SE2*CA2)
+VARP*CE2*SA2
1 R(2,2)=RM2*(VART*SE2*CA2+VARP*CE2*CA2+VART*VARP*SE2*SA2)
+VARP*CE2*CA2
1 R(3,3)=RM2*VART*CE2+VARP*SE2
R(1,2)=RM2*VART*(1.DO-VARP)*(SE2*SA*CA)
+ (VARP-RM2*VARP)*(CE2*SA*CA)
1 R(2,1)=R(1,2)
R(1,3)=(VARP-RM2*VART)*SE*CE*SA
R(3,1)=R(1,3)
R(2,3)=(VARP-RM2*VART)*SE*CE*CA
R(3,2)=R(2,3)
C 121 IF(ITH.EQ.0) PRINT 317,((R(I,J),J=1,9),I=1,9)
317 FORMAT(///,10X,'R ARRAY',/,9(/,9F14.5),//)
C----- COMPUTE GAIN MATRIX
DO 81 I=1,9
DO 81 J=1,9
BDUM(I,J)=0.DO
ADUM(I,J)=0.DO
CALL PROC(H;PP,3,9,9,ADUM)
CALL PROC(ADUM,HT,3,9,3,BDUM)
DO 83 I=1,9
DO 83 J=1,9
ADUM(I,J)=0.DO
CALL ADDSUB(BDUM,R,3,3,ADUM,1)
DO 82 I=1,9
DO 82 J=1,9
BDUM(I,J)=0.DO
CALL INVERT(3,ADUM,BDUM,KER,9)
CALL KER(EQ.2) PRINT 308
308 FORMAT(10X,'INVERSION SINGULARITY ENCOUNTERED')
DO 84 I=1,9
DO 84 J=1,9
ADUM(I,J)=0.DO
CALL PROC(PP,HT,9,9,3,ADUM)
CALL PROC(ADUM,BDUM,9,3,3,G)
GNX=G(1,1)
GNY=G(4,2)
GNZ=G(7,3)
C----- COMPUTE COVARIANCE OF ESTIMATION ARRAY (PE)
DO 85 I=1,9
DO 85 J=1,9

```



```

      ADUM(I,J)=0.00
      BDUM(I,J)=0.00
      CALL PRCD(G,H,9,3,9,ADUM)
      CALL ADDSUB(XIDEN,ADUM,9,9,BDUM,-1)
      CALL PRCD(BDUM,PP,9,9,9,PE)
C-----COMPUTE COVARIANCE OF PREDICTION ARRAY (PP)
      DO 86 I=1,9
      DO 86 J=1,9
      ADUM(I,J)=0.00
      BDUM(I,J)=0.00
      CALL PRCD(PHI,PE,9,9,9,ADUM)
      CALL PRCD(ADUM,PHI,TRN,9,9,9,BDUM)
      CALL ADDSUB(BDUM,Q,9,9,PP,I)
      IF(ITH.LE.1) GO TO 66
      61
C-----COMPUTE NEW HEADING ANGLE AND HEADING ANGLE RATE, BASED ON
C UNBIASED COMMANDS AS SENT FROM THE CONTROLLER.
C PHN IS THE NEW ROLL ANGLE
C PSN IS THE NEW TURNING ANGLE
C PHN=PHC+(PHI-PHC)*CAA2
C CA1=GG/VT1
C PSDN=CA1*PHN
C DELPS1=CA1*(PHC*DT+CA5*(PHI-PHC))
C PSIDEX=DELPS1/DT
C PSN=PSI+DELPS1
C
C CPSN=PSN/DEG
C SPSN=DSIN(CPSN)
C CPSN=DCOS(CPSN)
C
C-----COMPUTE STATE PREDICTION VECTOR
      66
      XDIP(1)=VT1*SPSN+DT*XDD1(1)
      XDIP(2)=VT1*CPSN+DT*XDD1(2)
      XDIP(3)=XDIP(2)+DT*XDD1(3)
C
      DELX(1)=DT3*(XDIP(1)+SN1)-CA4*(XDIP(2)*PSDN-SN2*PSD1)
      DELX(2)=DT3*(XDIP(2)+SN2)-CA4*(-XDIP(1)*PSDN+SN1*PSD1)
      DELX(3)=XDIP(3)+DT+XDIP(3)*DT2
C
      DO 110 I=1,3
      XDDIP(I)=XDD1(I)
      XDIP(I)=XDIP(I)+WR(I)
      XI(I)=XI(I)+DT*WR(I)+DELX(I)
      110
C
      IF(NWLD.LT.0) GO TO 67
      DO 64 I=1,3

```

```

JENT0580
JENT0590
JENT0600
JENT0610
JENT0620
JENT0630
JENT0640
JENT0650
JENT0660
JENT0670
JENT0680
JENT0690
JENT0700
JENT0710
JENT0720
JENT0730
JENT0740
JENT0750
JENT0760
JENT0770
JENT0780
JENT0790
JENT0800
JENT0810
JENT0820
JENT0830
JENT0840
JENT0850
JENT0860
JENT0870
JENT0880
JENT0890
JENT0900
JENT0910
JENT0920
JENT0930
JENT0940
JENT0950
JENT0960
JENT0970
JENT0980
JENT0990
JENT1000
JENT1010
JENT1020
JENT1030
JENT1040
JENT1050

```



```

1060 X1(I)=XIP(I)
1070 XDI(I)=XDIP(I)
1080 XDDI(I)=XDDIP(I)
1090 GO TO 65
1100
1110 C-----COMPUTE STATE ESTIMATION VECTOR
1120 E1=XDATA(1)-XIP(1)
1130 E2=XDATA(2)-XIP(2)
1140 E3=XDATA(3)-XIP(3)
1150
1160 X1(1)=XIP(1)+G(1,1)*E1+G(1,2)*E2+G(1,3)*E3
1170 XDI(1)=XDIP(1)+G(2,1)*E1+G(2,2)*E2+G(2,3)*E3
1180 XDDI(1)=XDDIP(1)+G(3,1)*E1+G(3,2)*E2+G(3,3)*E3
1190
1200 X1(2)=XIP(2)+G(4,1)*E1+G(4,2)*E2+G(4,3)*E3
1210 XDI(2)=XDIP(2)+G(5,1)*E1+G(5,2)*E2+G(5,3)*E3
1220 XDDI(2)=XDDIP(2)+G(6,1)*E1+G(6,2)*E2+G(6,3)*E3
1230
1240 X1(3)=XIP(3)+G(7,1)*E1+G(7,2)*E2+G(7,3)*E3
1250 XDDI(3)=XDDIP(3)+G(8,1)*E1+G(8,2)*E2+G(8,3)*E3
1260
1270 IF(ITH.GT.1) GO TO 65
1280 DC 98 I=1,3
1290 XDDI(I)=0.00
1300
1310 C-----COMPUTE VALUES FOR ENTERING DETERMINISTIC CONTROL
1320 CALCULATIONS ON NEXT ITERATION
1330 IF(ITH.EQ.0) RETURN
1340 PHI=PHIN
1350 PSDI=PSDN
1360 SN1=XDI(1)-WR(1)
1370 SN2=XDI(2)-WR(2)
1380 VTI=DSQRRT(SN1*SN1+SN2*SN2)
1390 PSI=DATAAN2(SN1,SN2)
1400 CPS=DCOS(PSI)
1410 SPS=DSIN(PSI)
1420 PSI=PSI*DEG
1430
1440 RETURN
1450 END
1460
1470 CCCCCCCCCC
1480
1490 SUBROUTINE MATCAL
1500
1510
1520
1530

```



```

REAL*8 A,AA,B,C,D,DD,S,X,Y
DIMENSION AA(1),X(1),LL(9),MM(9),Y(9,9),S(1),D(1),
1A(9,9),B(9,9),C(9,9)
ENTRY INVERT(N,AA,X,KER,K)
THIS SUBROUTINE INVERTS THE MATRIX A AND LEAVES THE
RESULTS IN THE MATRIX X. N AND K ARE THE ORDER OF THE MATRIX.
IF KER EQUALS 2 THEN A SINGULARITY HAS BEEN DETECTED.
DO 1 I=1,N
DO 1 J=1,N
IND=(I-1)*K+J
Y(I,J)=AA(IND)
KER=1
N2=2*N
CALL ARRAY(2,N,N,9,9,Y,Y)
CALL DMINV(Y,N,DD,LL,MM)
CALL ARRAY(1,N,N,9,9,Y,Y)
IF(DD.EQ.0) KER=2
DO 2 I=1,N
DO 2 J=1,N
IND=(I-1)*K+J
X(IND)=Y(I,J)
RETURN
1
2
ENTRY ADDSUB(A,B,N,M,C,ISIGN)
THIS SUBROUTINE ADDS (ISIGN=1) OR SUBTRACTS (ISIGN=-1)
THE NXM MATRICES A AND B (A+B OR A-B),
STORING THE RESULT IN C.
DO 125 I=1,N
DO 125 J=1,M
C(I,J)=A(I,J)+FLOAT(ISIGN)*B(I,J)
RETURN
125
ENTRY PRCD(A,B,N,M,L,C)
THIS SUBROUTINE COMPUTES THE MATRIX PRODUCT AB
AND STORES THE RESULT IN C. A IS NXM, B IS MXL, AND C IS NXL.
DO 3 I=1,N
DO 3 J=1,L
C(I,J)=0.D0
3

```









```

SUBROUTINE DER
IMPLICIT REAL*8(A-H,C-Z)
COMMON/DERCOM/EKDTAB(112),VKDTAB(112),D2W,HT,IPLC,NNT
COMMON/DIFCOM/HMX,HMN,H,ERROR,X,XMX,VDR(16,16),N,NAC,IFL,IFX,ISTF
DATA G/32.174049/
VDP(12,1)=VDR(1,3)
VDP(12,2)=VDR(1,4)
GG=6*(1.00-VDR(1,2))*(9.5897768D-08-VDR(1,2))*6.872006D-15))
P=1.00-6.875347D-06*VDR(1,2)*(1.00-4.7948887D-08*VDR(1,2))
PP=(-6.875347D-06*(1.00-9.5897774D-08*VDR(1,2)))/P
PL=-D2W*.076475137*(P**4.25561222)
P2=DSQRT(P)
VS=1116.4437*P2
V21=VDP(1,3)*VDR(1,3)
V22=VDR(1,4)*VDR(1,4)
V=DSQRT(V2)
VM=V/VS
TTP=EKDTAB(1)
=0.00
IF (VM.LE.VKDTAB(1)) GO TO 4
=EKDTAB(NNT)
IF (VM.GE.VKDTAB(NNT)) GO TO 4
IF (VM.NNT/2) GO TO 4
IF (VM.GT.VKDTAB(IPLC-1)) GO TO 2
IPLC=IPLC-1
GO TO 1
IF (VM.LE.VKDTAB(IPLC)) GO TO 3
IPLC=IPLC+1
GO TO 2
D1=(VKDTAB(IPLC-1)-VKDTAB(IPLC)))*(VKDTAB(IPLC-1)-VKDTAB(IPLC+1))
D2=(VKDTAB(IPLC)-VKDTAB(IPLC+1))*(VKDTAB(IPLC-1)-VKDTAB(IPLC+1))
D3=(VKDTAB(IPLC+1)-VKDTAB(IPLC-1))*(VKDTAB(IPLC+1)-VKDTAB(IPLC-1))
E1=(VM-VKDTAB(IPLC))*(VM-VKDTAB(IPLC+1))
E2=(VM-VKDTAB(IPLC-1))*(VM-VKDTAB(IPLC+1))
E3=(VM-VKDTAB(IPLC-1)+E2/D2*EKDTAB(IPLC)+E3/D3*EKDTAB(IPLC+1)
=EI/D1*EKDTAB(IPLC)-VKDTAB(IPLC+1)
E1=VM+VM-VKDTAB(IPLC)-VKDTAB(IPLC+1)
E2=VM+VM-VKDTAB(IPLC-1)-VKDTAB(IPLC+1)
E3=VM+VM-VKDTAB(IPLC-1)-VKDTAB(IPLC)
TP=EI/D1*EKDTAB(IPLC-1)+E2/D2*EKDTAB(IPLC)+E3/D3*EKDTAB(IPLC+1)
TP=TP/VS
VDR(12,3)=PL*V*VDR(1,3)*T
VDR(12,4)=PL*V*VDP(1,4)*T-GG
VDR(12,5)=VDR(1,11)
VDR(12,6)=VDR(1,12)
VDR(12,7)=VDP(1,13)

```



```

VDR(12,8)=VDR(1,14)
VDR(12,9)=VDR(1,15)
VDR(12,10)=VDR(1,16)
A44=4.2561222*T-.5D0*V*TP
A32=PL*V*VDR(1,3)*PP*A44
A33=PL*((V21+V2)/V*TP+V21*TP)
A34=PL*VDR(1,3)*VDR(1,4)*(T/V+TP)
VDR(12,11)=A32*VDR(1,8)+A33*VDR(1,11)+A34*VDR(1,14)
VDR(12,12)=A32*VDR(1,9)+A33*VDR(1,12)+A34*VDR(1,15)
VDR(12,13)=A32*VDR(1,10)+A33*VDR(1,13)+A34*VDR(1,16)
A42=PL*V*VDR(1,4)*PP*A44+G*(9.5897768D-08-VDR(1,2))*1.3944012D-14)
A43=A34
A44=PL*((V2+V22)/V*TP+V22*TP)
VDR(12,14)=A42*VDR(1,8)+A43*VDR(1,11)+A44*VDR(1,14)
VDR(12,15)=A42*VDR(1,9)+A43*VDR(1,12)+A44*VDR(1,15)
VDR(12,16)=A42*VDR(1,10)+A43*VDR(1,13)+A44*VDR(1,16)
RETURN
END

```

CCCCCCCC

```

SUBROUTINE OUT
IMPLICIT REAL*8 (A-H,O-Z)
COMMON/ DIFCOM/HMX,HM,N,ERROR,X,XX,VDR(16,16),N,NAC,IFL,IFX,ISTF
COMMON/ DERCOM/EKDTAB(112),VKDTAB(112),D2W,HT,IPLC,NNT
IF(X.EQ.0.00) JFL=1
IF(JFL.GT.0) GO TO 29
G5=HT-VDR(1,2)
G6=HT-VDR(2,2)
G7=VDR(2,2)-VDR(1,2)
G0=G5/G7
G2=G0*G0
G0=(G7-G5-G6)/G7*G2
G2=G2*G6
G3=G3*G3*G5
XX=X-G0*H+G2/VDR(13,2)+G3/VDR(12,2)
G5=XX-X
G6=G5+H
G0=G0*G0
G0=(H+G6+G6)/H*G2

```

27



```

G2=G2*G6
G3=G6/H
G3=G3*G3*G5
G1=1.00-G0
DC 2 I=1,10
2 VDP(1,1)=G0*VDR(2,1)+G1*VDR(1,1)+G2*VDR(13,1)+G3*VDR(12,1)
X=XX
IFL=-1
VDR(4,1)=-VDR(1,8)/VDR(1,4)
VDR(4,2)=-VDR(1,9)/VDR(1,4)
VDR(4,3)=-VDR(1,10)/VDR(1,4)
G3=VDR(1,3)
VDR(4,4)=VDP(1,5)+G3*VDR(4,1)
VDR(4,5)=VDP(1,6)+G3*VDR(4,2)
VDR(4,6)=VDR(1,7)+G3*VDR(4,3)
GO TO 3
29 IF(VDR(1,2).LE.HT) GO TO 27
YP=VDR(1,2)+H*(VDR(12,2)-16.08700*H)-HT
IF(YP.GT.0.00) GO TO 3
YP=VDR(1,2)-HT
H=-((YP+YP)/(VDR(12,2)-DSQRT(VDR(12,2)*VDR(12,2)-2.00*YP*VDR(12,4)))
1 JFL=0 IFL=-1
3 IF(X.GE.XMX) IFL=-1
RETURN
CCCCCCCCC
SUBROUTINE STIFF(SUBA,SUBB)
IMPLICIT REAL*8 (A-H,C-Z)
COMMON/DIFFCM/HMX,HMN,H,ERROR,X,XX,VDR(16,16),N,NAC,IFL,IFX,ISTF
IF(NAC.LE.0) NAC=N
IFL=-2
1 CALL SUBA
CALL SUBB
IF(IFL+1)2,22,3
2 IFT=0
IFP=ERROR
EPL=.00500*ERROR
DO 200 I=1,N
200 VDR(11,I)=DABS(VDR(1,I))
IFL=0

```

LENT3460  
 LENT3470  
 LENT3480  
 LENT3490  
 LENT3500  
 LENT3510  
 LENT3520  
 LENT3530  
 LENT3540  
 LENT3550  
 LENT3560  
 LENT3570  
 LENT3580  
 LENT3590  
 LENT3600  
 LENT3610  
 LENT3620  
 LENT3630  
 LENT3640  
 LENT3650  
 LENT3660  
 LENT3670  
 LENT3680  
 LENT3690  
 LENT3700  
 LENT3710  
 LENT3720  
 LENT3730  
 LENT3740  
 LENT3750  
 LENT3760  
 LENT3770  
 LENT3780  
 LENT3790  
 LENT3800  
 LENT3810  
 LENT3820  
 LENT3830  
 LENT3840  
 LENT3850  
 LENT3860  
 LENT3870  
 LENT3880  
 LENT3890  
 LENT3900  
 LENT3910  
 LENT3920  
 LENT3930





```

3 H2=H+H IF(FIP*GI.EPL.OR.IFX.GT.0.OR.DABS(H2).GT.HMX) GO TO 4
  JST=I*ST/2
  KST=I*ST-JST
  IF(KST.GT.0) GO TO 4
  I*ST=JST
  H=H2
4 I=I
  X=X
  H2=.5D0*H
  DO 5 I=1,N
    VDP(2,I)=VDR(1,I)
    VDP(10,I)=VDR(1,I)
    VDR(13,I)=VDR(12,I)
    VDR(16,I)=VDR(12,I)
5 X=X+H2
  DO 7 I=1,N
    VDP(1,I)=VDP(10,I)+H2*VDR(16,I)
7 CALL SUBA
  DO 8 I=1,N
    VDR(3,I)=VDR(1,I)
    VDR(14,I)=VDR(12,I)
    VDP(1,I)=VDP(10,I)+H2*VDR(12,I)
8 CALL SUBA
  DO 10 I=1,N
    VDR(4,I)=VDR(1,I)
    VDR(15,I)=VDR(12,I)
    IF(I*ST.EQ.0) GO TO 9
    P=VDP(4,I)-VDR(3,I)
    IF(P.EQ.0.D0) GO TO 9
    P=-VDR(15,I)-VDR(14,I)/P
    PH=P*H
    IF(PH.LT.5D0) GO TO 9
    VDR(5,I)=P
    P=DEXP(-PH)
    VDR(6,I)=(1.D0-P)/PH
    VDR(7,I)=(1.D0-VDR(6,I))/PH
    VDR(8,I)=(.5D0-VDR(7,I))/PH
    VDR(1,I)=VDR(10,I)+H*(VDR(15,I)+VDR(13,I))*VDR(7,I)*PH
    VDR(1,I)-VDR(7,I)+VDR(14,I)+VDR(7,I)*PH
    GO TO 10
9 VDR(5,I)=0.D0
  VDR(1,I)=VDP(10,I)+H*VDR(15,I)
10 CONTINUE
  X=X+H2
  CALL SUBA
  DO 12 I=1,N
    P=VDR(5,I)

```

```

LENT 3940
LENT 3950
LENT 3960
LENT 3970
LENT 3980
LENT 3990
LENT 4000
LENT 4010
LENT 4020
LENT 4030
LENT 4040
LENT 4050
LENT 4060
LENT 4070
LENT 4080
LENT 4090
LENT 4100
LENT 4110
LENT 4120
LENT 4130
LENT 4140
LENT 4150
LENT 4160
LENT 4170
LENT 4180
LENT 4190
LENT 4200
LENT 4210
LENT 4220
LENT 4230
LENT 4240
LENT 4250
LENT 4260
LENT 4270
LENT 4280
LENT 4290
LENT 4300
LENT 4310
LENT 4320
LENT 4330
LENT 4340
LENT 4350
LENT 4360
LENT 4370
LENT 4380
LENT 4390
LENT 4400
LENT 4410

```



```

IF (ISTF.EQ.Q.OR.P.EQ.O.DO)      GO TO 11
PH=VDR(6,I)*VDR(16,I)
F1P=VDR(16,I)+P*VDR(10,I)
F2P=VDR(14,I)+P*VDR( 3,I)
F3P=VDR(15,I)+P*VDR( 4,I)
F4P=VDR(12,I)+P*VDR( 1,I)
VDR(1,I)=VDR(10,I)+H*(PH+VDR(7,I)*(-F1P-F1P-F2P+F3P-F4P)
1P)+4.DO*(F1P-F2P-F3P+F4P)*VDR(8,I)
GO TO 12
11 VDR(1,I)=VDR(10,I)+H/6.DO*(VDR(16,I)+VDR(14,I)+VDR(15,I)
1+VDR(15,I)+VDR(12,I))
12 CONTINUE
13 IF (IT-2)13,15,17
14 GO TO 14 I=1,N
15 X=XS
16 IT=2
17 H=H2
18 H2=5DQ*H
19 CALL SUBA
20 I=1,N
21 VDR(10,I)=VDR( 1,I)
22 VDR(16,I)=VDR(12,I)
23 IT=3
24 GO TO 6
25 F1P=O.DO
26 I=1,N
27 DP=(VDR(1,I)-VDR(9,I))/15.DO
28 IF (I.GT.NAC) GO TO 18
29 F3P=DABS(F3P)
30 F4P=DABS(VDR(1,I))
31 P=VDR(1,I)
32 IF (F4P.GT.P) P=F4P
33 IF (P.NE.O.DO) F3P=F3P/P
34 IF (F3P.GT.EGR) GO TO 19
35 IF (F3P.GT.F1P) F1P=F3P
36 VDR(1,I)=VDR(1,I)+F2P
37 IST=IST+1
38 H=H+H
39 GO TO 180 I=1,N
40 F3P=DABS(VDR(1,I))
41 IF (F3P.GT.VDR(11,I)) VDR(11,I)=F3P
42 GO TO 1
43 H=H2
44 IF (DABS(H2).GT.HMN) GO TO 20
45 IFL=-1

```

```

LENT4420
LENT4430
LENT4440
LENT4450
LENT4460
LENT4470
LENT4480
LENT4490
LENT4500
LENT4510
LENT4520
LENT4530
LENT4540
LENT4550
LENT4560
LENT4570
LENT4580
LENT4590
LENT4600
LENT4610
LENT4620
LENT4630
LENT4640
LENT4650
LENT4660
LENT4670
LENT4680
LENT4690
LENT4700
LENT4710
LENT4720
LENT4730
LENT4740
LENT4750
LENT4760
LENT4770
LENT4780
LENT4790
LENT4800
LENT4810
LENT4820
LENT4830
LENT4840
LENT4850
LENT4860
LENT4870
LENT4880
LENT4890

```



JENT4900  
 JENT4910  
 JENT4920  
 JENT4930  
 JENT4940  
 JENT4950  
 JENT4960  
 JENT4970  
 JENT4980  
 JENT4990  
 JENT5000  
 JENT5010  
 JENT5020  
 JENT5030  
 JENT5040  
 JENT5050  
 JENT5060  
 JENT5070  
 JENT5080  
 JENT5090  
 JENT5100  
 JENT5110  
 JENT5120  
 JENT5130  
 JENT5140  
 JENT5150  
 JENT5160  
 JENT5170  
 JENT5180  
 JENT5190  
 JENT5200  
 JENT5210  
 JENT5220  
 JENT5230  
 JENT5240  
 JENT5250  
 JENT5260  
 JENT5270  
 JENT5280  
 JENT5290  
 JENT5300  
 JENT5310  
 JENT5320  
 JENT5330  
 JENT5340  
 JENT5350  
 JENT5360  
 JENT5370

```

      GO TO 1
20  X=XS
    H2=.5D0*H
    I1=2
    DO 21 I=1,N
      VDR( 9,I)=VDR( 10,I)
      VDR(10,I)=VDR( 2,I)
21  VDR(16,I)=VDR(13,I)
    I1=I1+I1
    GO TO 0
22  RETURN
    END

      SUBROUTINE MATNAD(A,Z,X,Y)
      REAL*8 A(3,3),X(3),Y(3),Z(3)
      IGO=1
      DO 1 I=1,3
        MATMLT(A,X,Y)
        IGO=0
1    Y(I)=0.D0
        IF(IGO.NE.0) Y(I)=Z(I)
        DO 2 J=1,3
          Y(I)=Y(I)+A(I,J)*X(J)
2    RETURN
      END

      BLOCK DATA
      SET ENTIRE COMMON BLOCK TO ZERO
      IMPLICIT REAL*8(Z)
      COMMON/AIRCCM/Z1(25)
      COMMON/RADCCM/Z2(37)
      COMMON/DERCCM/Z3(228)
  
```



```
COMMON/DIFFCCM/Z4(267)
DATA Z1/25*0.00/
DATA Z2/37*0.00/
DATA Z3/228*0.00/
DATA Z4/267*0.00/
END
```

```
CCCCCCCC
```

```
//G0.SYSIN DD *
```

```
15.0 0.1 0.1 0.125 0.125
-50000. 20000. 10000.
500. 2.0 0.125 0.125
0.0 5. 6. 0.
10. 1. 1. 1.
X RESIDUAL VS. T
Y RESIDUAL VS. T
Z RESIDUAL VS. T
RADIAL RESIDUAL VS. T
X6(1) VS. T
X6(2) VS. T
X6(2) VS. X6(1)
LATERAL ERROR (XE) VS. T
LATERAL ERROR (EXPANDED SCALE) VS. T
LATERAL ERROR RATE (DXE) VS. T
PHD, PHD1, AND PHD2 VS. T
ROLL ANGLE(COMMAND, ACTUAL, GEST) VS. T
```

```
LENT 5380
LENT 5390
LENT 5400
LENT 5410
LENT 5420
LENT 5430
LENT 5440
LENT 5450
LENT 5460
LENT 5470
LENT 5480
LENT 5490
LENT 5500
LENT 5510
LENT 5520
LENT 5530
LENT 5540
LENT 5550
LENT 5560
LENT 5570
LENT 5580
LENT 5590
LENT 5600
LENT 5610
LENT 5620
LENT 5630
LENT 5640
LENT 5650
LENT 5660
LENT 5670
LENT 5680
LENT 5690
LENT 5700
LENT 5710
LENT 5720
LENT 5730
LENT 5740
LENT 5750
LENT 5760
LENT 5770
LENT 5780
LENT 5790
LENT 5800
LENT 5810
LENT 5820
LENT 5830
LENT 5840
```









178







```

C      SIGW(1)=0.0
C      SIGW(2)=0.0
C      SIGW(3)=0.0
C-----TB IS TRUE AIRCRAFT ROLL RESPONSE TIME CONSTANT
C      TAUH IS THE ESTIMATED AIRCRAFT ROLL RESPONSE TIME CONSTANT
C      TAUH=TP
C-----READ INPUT PARAMETERS
C      READ(5,100) NLEG,RANGEI,AZI,VA,VAH,VW,VWH,THETW,THETWH
C      READ(5,110) (PLENTH(I),THETA(I),I=1,NLEG)
C      READ(5,111) HTG,DELMW
C      READ(5,112) ATITLE
C-----COMPUTE TRUE WIND (WT) AND ESTIMATED WIND (WH) COMPONENTS
C      WT(1)=VW*DSIN(THETW*DEG)
C      WT(2)=VW*DCOS(THETW*DEG)
C      WT(3)=0.0
C      WH(1)=VWH*DSIN(THETWH*DEG)
C      WH(2)=VWH*DCOS(THETWH*DEG)
C      WH(3)=0.0
C      DO 2 I=1,3
C      W(1)=WH(1)
C      HTG IS INITIAL TRUE GROUND HEADING
C      HTG IS INITIAL TRUE AIR HEADING
C      VTA IS INITIAL TRUE GROUND SPEED
C      VA IS THE TRUE AIR SPEED THROUGHOUT PROBLEM
C      UI=VW*DSIN(THETW*DEG)/VA
C      HTA=HTG-UI*360.
C      IF(HTA.GT.360.) HTA=HTA-360.
C      VTG=VW*DCOS(THETW*DEG)+VA*DCOS((HTA-HTG)*DEG)
C-----COMPUTE INITIAL TRUE A/C VELOCITY
C      XD3(1)=VTG*DSIN(HTG*DEG)
C      XD3(2)=VTG*DCOS(HTG*DEG)
C      XD3(3)=0.
C-----COMPUTE LEG PARAMETERS FOR MISSION DATA TABLE
C      XWP,YWP ARE COORDINATES OF LEG START/STOP POINTS
C      RANGE IS AVG DISTANCE TO LEG FROM RADAP; AZ IS AVG ANGLE TO LEG
C      H IS DESIRED AIR SPEED HEADING ALONG LEG
C      VGH IS DESIRED AIR GROUND SPEED ALONG LEG
C      VGX,VGY ARE COMPONENTS OF VGH
C      XWP(1)=RANGEI*DSIN(AZI*DEG)

```





```

YWP(1)=RANGEI*FEET*DCOS(AZI*DEG)
XWPNM(1)=XWP(1)/FEET
YWPNM(1)=YWP(1)/FEET
YVAX=XWPNM(1)
XMIN=XWPNM(1)
YMAX=YWPNM(1)
YMIN=YWPNM(1)

C-----COMPUTE INITIAL TRUE A/C POSITION
DO 9 KK=1,3
  DEL(KK)=DELNM(KK)*FEET
  X2(1)=XWP(1)+DEL(1)
  X2(2)=YWP(1)+DEL(2)
  X3(3)=DEL(3)
DO 10 KK=1,3
  X3NM(KK)=X2(KK)/FEET

C-----PRINT OUT SIMULATION INITIAL CONDITIONS AND PARAMETERS
PRINT 1000,VW,THETW,WT(1),WT(2),VWH,THETWH,WH(1),WH(2),
1 SIG(1),SIG(2),SIG(3),8IS,SIG(4),SIG(5),SIG(6),
2 SIGW,DTRAD,DELNM,VTC,HTG,XD3(1),XD3(2),VA,HTA,TB
1 PRINT 1001,NLEG,RANGEI,AZI,XWPNM(1),YWPNM(1),DTCON,PHILIM,
1 G1,G2,HERMIN

C-----COMPUTE MISSION DATA TABLE
DO 120 I=1,NLEG
  XWP(I+1)=XWP(I)+PLENTH(I)*FEET*DSIN(DEG*THETA(I))
  YWP(I+1)=YWP(I)+PLENTH(I)*FEET*DCOS(DEG*THETA(I))
  YWPNM(I+1)=XWP(I+1)/FEET
  YWPNM(I+1)=YWP(I+1)/FEET
  RANGC(I)=0.5*DSQRT((XWP(I)-XWP(I+1))**2+(YWP(I)-YWP(I+1))**2)/FEET
  A4(I)=RAD*DSIN((THETWH-THETA(I))*DEG)/VAH
  U1=VWH*DSIN((THETWH-THETA(I))-RAD*DARSIN(U1))
  H(I)=THETA(I)-RAD*360.
  IF(H(I).LT.0.) H(I)=H(I)+360.
  IF(H(I).GE.360.) H(I)=H(I)-360.
  VGH(I)=VAH*DCOS(DEG*(H(I)-THETWH-THETA(I)))
  VGH(I)+VWH*DCOS(DEG*(THETWH-THETA(I)))
1 TLEG(I)=(PLENTH(I)*FEET)/VGH(I)
VGX(I)=VGH(I)*SIN(THETA(I)*DEG)
VGY(I)=VGH(I)*COS(THETA(I)*DEG)

C-----SET UP X2 VECTOR WHICH WILL PLOT AS DESIRED TRACK
DO 123 I=1,NLEG
  ITABA=I+TABA+1
  X2NM(I)=XWPNM(I)
  X2NM(I+1)=YWPNM(I)

```



```

XXC(I,TABA)=X2NM(1)
YYC(I,TABA)=X2NM(2)
D=2*PI/TLEG(I)/DTRAD
DO 121 J=1, ID*2
  I,TABA=I,TABA+1
  X2NM(1)=X2NM(2)+(DTRAD*VGX(I))/FEET
  X2NM(2)=X2NM(1)+X2NM(2)*XMAX
  IF(X2NM(1).GT.XMIN) XMIN=X2NM(1)
  IF(X2NM(2).GT.XMIN) XMIN=X2NM(2)
  IF(X2NM(1).GT.YMIN) YMIN=X2NM(1)
  IF(X2NM(2).GT.YMIN) YMAX=X2NM(2)
  XXC(I,TABA)=X2NM(1)
  YYC(I,TABA)=X2NM(2)
CONTINUE
121
123
C-----SET UP PROBLEM INITIAL CONDITIONS
I=1
CALCST=2.0*DTRAD+1.0-EPS
CALCST=CALCST+1.0
HSTART=H(1)
HNEXT=H(2)
C
  PRINT 1100,I,XWPNM(I),YWPNM(I),VGH(I),H(I),RANGE(I),AZ(I),TLEG(I),
  1 PRINT 1101
  PRINT 1200
  LNC=3
C*****
C-----BEGIN MAIN PROCESSING STREAM
C-----THE ARCPRT SUBROUTINE CALCULATES TRUE NEW POSITION AND
  191 VELOCITY OF THE AIRCRAFT IN CARTESIAN COORDINATES
  CALL ARCPRT
  DO 192 KK=1,3
  192 X3NM(KK)=X2(KK)/FEET
C-----THE RADAR SUBROUTINE CALCULATES THE ESTIMATED POSITION
  AND VELOCITY OF THE AIRCRAFT IN CARTESIAN COORDINATES
  CALL RADAR
  DO 203 KK=1,3
  203 X1NM(KK)=X1(KK)/FEET
C-----CALCULATE HEADINGS AND ERRORS FOR USE IN CONTROL CALCULATION
  HIC IS TRUE GROUND HEADING
  HEG IS THE ESTIMATED GROUND HEADING

```



```
C C      TRUE AIR SPEED HEADING  
HEA IS THE ESTIMATED AIR SPEED HEADING  
HIA=DATAN2(XD3(1),XD3(2))*RAD  
HTG=DATAN2((XD3(1)-WT(1)), (XD3(2)-WT(2)))*RAD  
IF (.LT.(DTRAD-EPS)) GO TO 205  
HEA=DATAN2((XD1(1)-WH(1)), (XD1(2)-WH(2)))*RAD  
HEG=DATAN2(XD1(1),XD1(2))*RAD  
VEG=DSDORT(XD1(1)**2+XD1(2)**2)  
GO TO 206  
HEA=0.00  
HEG=0.00  
C 205  
  
C 206  
IF (HTG.GT.360.) HTG=HTG-360.  
IF (HEG.GT.360.) HEG=HEG-360.  
IF (HTA.GT.360.) HTA=HTA-360.  
IF (HEA.GT.360.) HEA=HEA-360.  
IF (HTG.LT.0.) HTG=HTG+360.  
IF (HEG.LT.0.) HEG=HEG+360.  
IF (HTA.LT.0.) HTA=HTA+360.  
IF (HEA.LT.0.) HEA=HEA+360.  
C-----  
C C      TRUE IS THE TRUE A/C DISPLACEMENT FROM DESIRED TRACK  
DESIRED IS THE TRACK  
DEBT=TRUE-(X3(2)-YWP(1))*DCOS(THETA(I))*DEG)/FEET  
1 DEBT=TRUE-(X3(2)-YWP(1))*DCOS(THETA(I))*DEG)/FEET  
1 DEBT=(X1(1)-XWP(1))*DCOS(THETA(I))*DEG)/FEET  
1 IF (ITURN.NE.O) GO TO 2058  
1 IF (ITEND.EQ.I) GO TO 2058  
1 DEBT=TRUE-(X3(1)-XWP(I+1))*DCOS(THETA(I+1))*DEG)/FEET  
1 DEBT=TRUE-(X3(2)-YWP(I+1))*DCOS(THETA(I+1))*DEG)/FEET  
1 DEBT1=-(X1(1)-XWP(I+1))*DCOS(THETA(I+1))*DEG)/FEET  
1 IF (DABS(DEBT1).LT.DABS(EEST)) EEST=EEST1  
1 IF (DABS(EEST1).LT.DABS(EEST)) EEST=EEST1  
C-----  
C C      COMPUTE OFF TRACK ERROR RMS SUMS  
IAVG=IAVG+1  
SUMEST=SUMEST+EEST**2  
SUMETR=SUMETR+EESTR**2  
C 2053  
  
C-----  
C C      COMPUTE PLOTTING LIMITS FOR SCALING  
IF (ACCD(ITH,IDTRAD).NE.O) GO TO 2059  
IF (AB1=7481+1  
IF (X1NM(1).GT.XMAX) XMAX=X1NM(1)  
IF (X2NM(1).GT.XMAX) XMAX=X2NM(1)  
IF (X1NM(1).LT.XMIN) XMIN=X1NM(1)
```



LENT2410  
 LENT2420  
 LENT2430  
 LENT2440  
 LENT2450  
 LENT2460  
 LENT2470  
 LENT2480  
 LENT2490  
 LENT2500  
 LENT2510  
 LENT2520  
 LENT2530  
 LENT2540  
 LENT2550  
 LENT2560  
 LENT2570  
 LENT2580  
 LENT2590  
 LENT2600  
 LENT2610  
 LENT2620  
 LENT2630  
 LENT2640  
 LENT2650  
 LENT2660  
 LENT2670  
 LENT2680  
 LENT2690  
 LENT2700  
 LENT2710  
 LENT2720  
 LENT2730  
 LENT2740  
 LENT2750  
 LENT2760  
 LENT2770  
 LENT2780  
 LENT2790  
 LENT2800  
 LENT2810  
 LENT2820  
 LENT2830  
 LENT2840  
 LENT2850  
 LENT2860  
 LENT2870  
 LENT2880

```

IF(X3NM(1).LT.XMIN) XMIN=X3NM(1)
IF(X1NM(2).LT.YMIN) YMIN=X1NM(2)
IF(X3NM(2).LT.YMIN) YMIN=X3NM(2)
IF(X1NM(2).GT.YMAX) YMAX=X1NM(2)
IF(X3NM(2).GT.YMAX) YMAX=X3NM(2)
XXA(ITAB1)=X1NM(1)
YYA(ITAB1)=X1NM(2)
YYB(ITAB1)=X3NM(1)
YYC(ITAB1)=X3NM(2)

2059 IF(T.LT.CALCST) GO TO 207
IF(ITURN.EQ.O.OR.IEND.EQ.1) GO TO 207

C-----COMPUTE TURN ANGLE AND TIME
XMI=XD1(2)/XD1(1)
XMI1=((YWP(I+1)-YWP(I+2))/(XWP(I+1)-XWP(I+2))
XINT=((YWP(I+1)-X1(2)/XMI*X1(1)-XMI1*XWP(I+1)))/(XMI1-XMI)
YINT=XMI*XINT/X1(1)+X1(2)
XINTNM=XINT/FEET
YINTNM=YINT/FEET
DTG=DSQRT((XINT-X1(1))**2+(YINT-X1(2))**2)
TLEG1=DTG/VEG
DELHE=DS(BS(H(I+1)-HEA)
I(TC21=VAH*DELH*GT.180.) DELH=360.-DELH
I(TC21=VAH*DELH*DEG/(2.0*GT.TAN)
IF(TC21>TAUH*GT.0.6) GO TO 2060
T121=TAUH*DSQRT(2.0*TC21/TAUH)
GO TO 2061

C-----COMPUTE TURN HALF PERIOD BY SOLVING EQUATION
USING THE NEWTON-RAPHSON METHOD
T121=TAUH*(1.0+TC21/TAUH)
U=T121/TAUH
DO 2062 J=1,10
F=U+DEXP(-U)-1.0-TC21/TAUH
F9=1.0-DEXP(-U)
UCUD=U
U=UCUD-F/FP
IF(DABS(TAUH*(U-UCUD)).LE.0.01) GO TO 2063
CONTINUE
T121=TAUH*U

DA1=VEG*(T121-TC21)
DC1=2.*VAH*TC21*DSIN(DEG*(THETA(I+1)-THETWH))
1 *DSIN(DEG*(THETA(I+1)-HEG))
DB1=VAH*VAH/G/TAN*(DSIN(DEG*(H(I+1)-HEA))
2 HEA))-(1.-DCOS(DEG*(H(I+1)-HEA)))
3 /DABS(DSIN(DEG*(THETA(I+1)-HEA)))
  
```





```

C      D61=DA1+D81+DC1
      TTURN1=D61/VEG
      TSTPIN=2.0*(TT21-TAUH)
      TTOTIN=2.0*TT21
      TG=TLEG1-TTURN1
C 207  IF(LNC.LE.LNCLIM) GO TO 208
      PRINT 1101
      PRINT 1200
      LNC=LNC+2
C 208  PRINT 1201,T,PHC,PH1,TLEG1,TTURN1,TO21,TT21,
      HIG,HEG,HTA,HEA,
      ETRUE,EEST,PHD1,PHD2
C-----I IS TIME TO GO BEFORE BEGINNING COMMAND TURN
C      IG IS TIME TO GO WHEN TIME TO BEGIN A TURN
C      ITH COUNTS TOTAL NUMBER OF SAMPLES ON THIS RUN
      ITH=ITH+1
      I=I+DT
      IF(I.LT.CALCS1) GO TO 191
      IF(T.GE.TSTOP) GO TO 999
C-----BRANCH TO 210 IF NOT EXECUTING OR COMPLETING A TURN
C      BRANCH TO 220 WHEN TIME TO BEGIN A TURN
C      BRANCH TO 209 WHEN COMPLETING A TURN
      IF(TTURN) 210,220,209
      IF(TG.LE.0.0.AND.IEND.NE.1) GO TO 219
      GO TO 240
C 210  IF(TG.LE.0.0.AND.IEND.NE.1) GO TO 219
C-----GENERATE COURSE GUIDANCE TO CAUSE AIRCRAFT TO FLY
C      TOWARD CURRENT LEG'S END POINT. BANK ANGLE COMMAND IS
C      QUANTIZED TO NEAREST 15/128 DEGREE. BANK PHC=0 COMMAND SENT IF
C      HEADING ERROR TO CURRENT LEG END POINT IS LESS THAN HERMIN.
      IF(TG.GT.3.0*TAUH+DT.CR.IEND.EQ.1) GO TO 212
      PHC=0.0
      GO TO 191
C 212  HEGWPT=RAD*ATAN2((XWP(I+1)-X1(1)),(YWP(I+1)-X1(2)))
      HDEOLD=HDE
      HDE=HEGWPT-HEG
      IF(HDE.GT.180.) HDE=HDE-360.
      IF(HDE.LT.-180.) HDE=HDE+360.
      HDEOLD=(HDE-HDEOLD)/DT
      PHD1=G1*HDE
      PHD2=G2*HDEDDGT

```



LENT3370  
LENT3380  
LENT3390  
LENT3400  
LENT3410  
LENT3420  
LENT3430  
LENT3440  
LENT3450  
LENT3460  
LENT3470  
LENT3480  
LENT3490  
LENT3500  
LENT3510  
LENT3520  
LENT3530  
LENT3540  
LENT3550  
LENT3560  
LENT3570  
LENT3580  
LENT3590  
LENT3600  
LENT3610  
LENT3620  
LENT3630  
LENT3640  
LENT3650  
LENT3660  
LENT3670  
LENT3680  
LENT3690  
LENT3700  
LENT3710  
LENT3720  
LENT3730  
LENT3740  
LENT3750  
LENT3760  
LENT3770  
LENT3780  
LENT3790  
LENT3800  
LENT3810  
LENT3820  
LENT3830  
LENT3840

```

PHD=PHD1+PHD2
IF(DABS(PHD).GT.PHILIM) PHD=PHILIM*PHD/DABS(PHD)
C
PHC=(PHD)*128.D0/15.D0+.500
NHC=PHC
PHC=NHC
PHC=PHC*15.D0/128.D0
C
IF(DABS(HDE).LT.HERMIN) PHC=0.0
GO TO 191
C
219 I TURN=0
C-----WLD IS SET GREATER THAN ZERO HERE TO SUPPRESS RADAR UPDATES
C DURING A COMMAND TURN
NWLDE=1
TINTRN=0.0
IF(LNC.LE.LNCLIM) GO TO 2191
PRINT 1101
LNC=0
LNC=LNC+3
PRINT 2001, T, TINTRN
IF(TINTRN.GE.TSTPTN) GO TO 239
TTC-TI=TTC
C-----COMPUTE DIRECTION OF COMMAND TURN
DELH=RNEXT-HSTART
IF(DELH.GT.180.) DELH=DELH-360.
IF(DELH.LT.-180.) DELH=DELH+360.
IF(DELH.GT.0.) PHC=PHILIM
IF(DELH.LT.0.) PHC=-PHILIM
GO TO 191
C
239 I TURN=1
IF(LNC.LE.LNCLIM) GO TO 2391
PRINT 1101
LNC=0
LNC=LNC+3
PRINT 2002, T, TINTRN
PHC=0.
C
C-----BEGIN NEW LEG
I=I+1
HSTART=H(I)
HNEXT=H(I+1)
IF(I.EQ.NLEG) IEND=1

```



```

C          IF(LNC.LE.LNCLIM-21) GO TO 2392
          PRINT 1101
          LNC=0
          LNC=LNC+21
2392      C
          PRINT 1100,I,XWPNM(I),YWPNM(I),XWPNM(I+1),YWPNM(I+1),PLENTH(I),
            1      THETA(I),VGH(I),H(I),RANGE(I),AZ(I),TLEG(I)
          PRINT 1200
C
240      IF(TINTRN.GE.TTOTT1) GO TO 280
          TINTRN=TINTRN+DT
          GO TO 191
C-----RESET TURN LOGIC FOR TURN AT END OF NEW LEG
280      ITURN=-1
          LND=-1
          IF(LNC.LE.LNCLIM) GO TO 285
          PRINT 1101
          LNC=0
          LNC=LNC+3
          PRINT 2003, I, TINTRN
          TINTRN=0.
          IF(IEND.EQ.0.1) TSTOP=T+TLEG(I)-2.0*TT21-2.0*TAUH
          GO TO 191
C999
          CONTINUE
          RMSEST=DSQRT(SUMEST/FLOAT(IAVG))
          RMSETR=DSQRT(SUMETR/FLOAT(IAVG))
          PRINT 1260, RMSETR, RMSEST
C-----EXECUTE PLOTS
          ITAB2=ITAB1+1
          ITAB3=ITAB1+2
          DXX=XMAX-XMIN
          DYY=YMAX-YMIN
          IF(DXX.GT.DYY) YMAX=YMIN+DXX
          IF(DXX.LT.DYY) XMAX=XMIN+DYY
          XXA(ITAB2)=XMAX
          XXA(ITAB3)=XMIN
          YYA(ITAB2)=YMAX
          YYA(ITAB3)=YMIN
          WRITE(6,1250) ATITLE,ITAB3,1)
          CALL PLOTP(XXA,YYA,ITAB1,2)
          CALL PLOTP(XXB,YYB,ITAB1,2)
          CALL PLOTP(XXC,YYC,ITAB1,3)
          PRINT 1101
          STOP

```

```

ENT 3850
ENT 3860
ENT 3870
ENT 3880
ENT 3890
ENT 3900
ENT 3910
ENT 3920
ENT 3930
ENT 3940
ENT 3950
ENT 3960
ENT 3970
ENT 3980
ENT 3990
ENT 4000
ENT 4010
ENT 4020
ENT 4030
ENT 4040
ENT 4050
ENT 4060
ENT 4070
ENT 4080
ENT 4090
ENT 4100
ENT 4110
ENT 4120
ENT 4130
ENT 4140
ENT 4150
ENT 4160
ENT 4170
ENT 4180
ENT 4190
ENT 4200
ENT 4210
ENT 4220
ENT 4230
ENT 4240
ENT 4250
ENT 4260
ENT 4270
ENT 4280
ENT 4290
ENT 4300
ENT 4310
ENT 4320

```



```

C-----INPUT FORMATS
100  FORMAT(11,F9.2,7F10.4)
110  FORMAT(2F10.3)
111  FORMAT(4F10.3)
112  FORMAT(6A8)
C-----OUTPUT FORMATS
C1000  FORMAT(1H1,48X,'AN/TPQ-27 SIMULATION',//,37X,'COARSE',
1'GUIDANCE MODE WITH KALMAN FILTERING',//,5X,'INITIAL CONDITIONS',
2'//,8X,'TRUE WIND =',F6.2,' FT/SEC AT ',F6.2,' DEGREES',
3'//,8X,'TRUE WIND COMPONENTS =',F6.2,'//,
48X,'ESTIMATED WIND =',F6.2,' FT/SEC AT ',F6.2,' DEGREES',//,
58X,'ESTIMATED WIND COMPONENTS =',F6.2,'//,
6'//,3X,'ADAR - SIGMAS(R,FT.),AZ(DEG),EL(DEG)) = ',1P3D16.5,/,10X
7'MEASUREMENT BIASES(
8'10X,'INITIAL VELOCITY MEASUREMENT VALUES = ',1P3D16.5,/,
9'10X,'RANDOM FORCING ASSUMPTION VALUES (SIGW) = ',3X,1P3D16.5,/,
C10X,'SAMPLING INTERVAL FOR RADAR (DTRAD) = ',OPF6.3,///,
16X,'AIRCRAFT DATA',//,
210X,'TRUE INITIAL DISPLACEMENT FROM STARTING POINT (NM) = ',
33F8.2,/,10X,'TRUE INITIAL GROUND VELOCITY = ',F8.2,
4'FT/SEC AT ',F6.2,' DEGREES',//,
510X,'TRUE INITIAL AIR VELOCITY = ',F8.2,' FT/SEC AT ',
7F6.2,' DEGREES',//,10X,'ROLL RESPONSE PARAMETER (TR) = ',F5.3,///)
C1001  FORMAT(8X,'TRACK DATA',//,10X,'NUMBER OF LEGS (NLEGS) = ',12,/,
110X,'POSITION OF FIRST LEG = ',F8.3,' NM AT ',F6.2,' DEGREES',//,
210X,'COMPONENTS OF START POINT = ',2F8.3,/,15X,
3'//,8X,'CONTROL DATA',//,10X,'CONTROL INTERVAL = ',F6.3,/,
410X,'MAXIMUM BANK ANGLE = ',F7.2,///,
510X,'G1 = ',F8.3,/,10X,'G2 = ',F8.3,///,
610X,'MIN HEADING ERROR FOR COMMAND CORRECTION = ',
7F8.3,///)
C1100  FORMAT(//,4X,'LEG NUMBER',12,/,10X,'LEG START POINT (X,Y) = ',
12F10.4,/,10X,'LEG END POINT (X,Y) = ',2X,2F10.4,/,
210X,'LEG LENGTH (NM) = ',2X,F10.2,/,10X,'LEG AZIMUTH (DEG) = ',
310X,'DESIRABLE SPEED = GROUND SPEED = ',F6.2,/,
410X,'DESIRABLE HEADING (DEG) = ',F6.2,///,
510X,'AVERAGE RANGE OF LEG FROM RADAR (NM) = ',3X,F10.2,/,
610X,'AVERAGE AZIMUTH OF LEG FROM RADAR (DEG) = ',F10.2,///,
710X,'LEG = ',F7.3,///)
C1101  FORMAT(1H1)

```









```

CA2=DEXP(-DT/TB)
CA3=CA1
CA4=DT*(12.00*DEG)
CA5=TB*(1.00-CA2)
DT3=500*DT
PSD=CA1*PH
PPS=DATAN2(SM1,SM2)
CPS=DCOS(PPS)
SPS=USIN(PPS)
P=PS*DEG
RETURN
*****
C-----ENTER MAIN CALCULATION STREAM
C-----PHC IS NOW THE COMMAND BANK ANGLE AT T(N-1)
C-----PHN IS THE NEW BANK ANGLE
C-----PPSN IS THE NEW TURNING RATE
C-----PPSN IS NEW HEADING ANGLE FOR VELOCITY WITH RESPECT TO WIND
C-----PPSN=PH+PPH
C-----PPN=PS*(PH-PPSN)*CA2
C-----PPN=CA1*PPH
C-----PPSU=PS*(CA3*(PSV*DT+CA5*(PH-PPSN)))
C-----PPSN=PPSU/DEG
C-----SPSN=DCSIN(CPPSN)
C-----CPSN=DCOS(CPPSN)
C-----UPDATE VELOCITY VECTOR FOR NEW TURN ANGLE
X3(1)=WT(1)+VT*SPSN
X3(2)=WT(2)+VT*CPSN
X3(3)=0.00
C-----UPDATE POSITION VECTOR FOR NEW TURN ANGLE
SM1=DT3*(SPS+SPSN)-CA4*(CPSN*PPSDN-PPS*PPSD)
SM2=DT3*(CPS+CPSN)-CA4*(-SPSN*PPSDN+SPS*PPSD)
SM3=0.00
X3(1)=DT*WT(1)+VT*SM1+X3(1)
X3(2)=DT*WT(2)+VT*SM2+X3(2)
X3(3)=X3(3)
C-----REPEAT VALUES FOR NEXT TIME IN SUBROUTINE
C-----PPH=PPH
PPS=PPSN
PPSU=PPSU
C-----CPS=CPSN

```







6250  
 6260  
 6270  
 6280  
 6290  
 6300  
 6310  
 6320  
 6330  
 6340  
 6350  
 6360  
 6370  
 6380  
 6390  
 6400  
 6410  
 6420  
 6430  
 6440  
 6450  
 6460  
 6470  
 6480  
 6490  
 6500  
 6510  
 6520  
 6530  
 6540  
 6550  
 6560  
 6570  
 6580  
 6590  
 6600  
 6610  
 6620  
 6630  
 6640  
 6650  
 6660  
 6670  
 6680  
 6690  
 6700  
 6710  
 6720

```

R(I,J)=0.00
GAMMA(I,J)=0.00
W(I,J)=0.00
QTRAD2=QTRAD**2/2.00
H(1,1)=SIGW(1)**2
W(2,2)=SIGW(2)**2
W(3,3)=SIGW(3)**2
GAMMA(1,1)=QTRAD
GAMMA(2,1)=QTRAD2
GAMMA(3,2)=QTRAD2
GAMMA(4,3)=QTRAD2
GAMMA(5,3)=QTRAD2
GAMMA(6,3)=QTRAD
CALL TRANS(GAMMA,6,3,ADUM)
CALL PROC(BDUM,ADUM,6,3,6,G)

C-----INITIALIZE COVARIANCE OF PREDICTION ARRAY (PP)
DO 2 I=1,6
  DO 2 J=1,6
    PP(I,J)=0.00
  IF(I.EQ.J) PP(I,J)=1.006

C-----COMPUTE MEASUREMENT MATRIX AND VARIANCE
DO 3 I=1,6
  DO 3 J=1,6
    H(I,J)=0.00
  H(1,1)=1.00
  H(2,3)=1.00
  H(3,5)=1.00
  CALL TRANS(H,3,6,HT)

  SIGI(1)=SIG(1)
  SIGI(2)=SIG(2)/DEG
  SIGI(3)=SIG(3)/DEG
  VARPP=SIGI(1)**2
  VARPP=SIGI(2)**2
  VARPP=SIGI(3)**2

C-----COMPUTE STATE TRANSITION ARRAY (PHI)
DO 4 I=1,6
  DO 4 J=1,6
    PHI(I,J)=0.00
  PHI(1,1)=1.00
  PHI(1,2)=1.00
  PHI(3,3)=1.00

```





```

PHI(3,4)=DTRAD
PHI(4,4)=1.D0
PHI(5,5)=1.D0
PHI(5,6)=DTRAD
PHI(6,6)=1.D0
CALL TRANS(PHI,6,6,PHITRN)

C-----CREATE IDENTITY ARRAY
DO 8 I=1,6
DO 8 J=1,6
XIDENT(I,J)=0.D0
IF(I.EQ.J) XIDENT(I,J)=1.D0
      8

C-----BYPASS PRINT EQUATIONS FOR THIS PROGRAM
IF(ITH.GT.10) GO TO 50
PRINT 310,((H(I,J),J=1,6),I=1,6)
PRINT 311,((I(X,I),I=1,6),J=1,6)
PRINT 311,((GAMMA(I,J),J=1,6),I=1,6)
PRINT 312,((I(X,I),I=1,6),J=1,6)
PRINT 312,((Q(I,J),J=1,6),I=1,6)
PRINT 313,((PP(I,J),J=1,6),I=1,6)
PRINT 313,((I(X,I),I=1,6),J=1,6)
PRINT 314,((PE(I,J),J=1,6),I=1,6)
PRINT 314,((I(X,I),I=1,6),J=1,6)
PRINT 316,((PHI(I,J),J=1,6),I=1,6)
PRINT 316,((I(X,I),I=1,6),J=1,6)
*****

C-----BEGIN NORMAL FILTER COMPUTATIONS
C-----COMPUTE TRUE R,AZ,EL,ADD NOISE, AND COMPUTE NOISY MEASUREMENTS
C-----IN CARTESIAN COORDINATES
50  QTCUM=DT*CU+DT
IF(QTCUM.LT.(DTRAD-EPS)) GO TO 61
IF(NHLD.GE.0.AND.ITH.NE.0) GO TO 61
R=X3(1)*X3(1)+X3(2)*X3(2)
A=DATAN2(X3(1),X3(2))
E=DATAN2(X3(3),DSORT(R))
R=DSQRT(R+X3(3)*X3(3))
RW2=RR**2

C      CALL NORMAL(IU,RAN,3)
DO 6 I=1,3
6  XDATA(I)=XDATA(I)+BIS(I)+SIG1(I)*RAN(I)

C      IF(DABS(A)-LT.ANGMIN) A=ANGMIN
      IF(DABS(E)-LT.ANGMIN) E=ANGMIN

```



```

SIGNA=A/DABS(A)
SIGNE=E/DABS(E)
DELA=DABS(A-ANGMAX)
DELE=DABS(E-ANGMAX)
IF(DELA.LT.ANGMIN) A=SIGNA*ANGMAX
IF(DELE.LT.ANGMIN) E=SIGNE*ANGMAX

CA=DCOS(A)
SA=DSIN(A)
CE=DCOS(E)
SE=DSIN(E)
CA2=CA**2
SA2=SA**2
CE2=CE**2
SE2=SE**2

XDATA(3)=RR*SE
XDATA(2)=RR*CE*CA
XDATA(1)=RR*CE*SA

IF(ITH.NE.O) GO TO 63
DO 62 I=1,3
  XIP(I)=XDATA(I)
  XI(I)=XIP(I)
  XDIP(I)=SIG(I+3)
  DELX(I)=O.DD
62 IF(NMLD.CE.O) GO TO 61

C-----COMPUTE COVARIANCE OF MEASUREMENT ERROR ARRAY (R)
63 R(1,1)=RM2*(VART*SE2*SA2+VARP*CE2*CA2+VART*VARP*SE2*CA2)
  1 R(2,2)=FM2*(VART*SE2*CA2+VARP*CE2*CA2+VART*VARP*SE2*SA2)
  1 R(3,3)=FM2*(VART*CE2*CA2+VARP*SE2
    R(1,2)=RM2*VART*(1.DD-VARP)*(SE2*SA*CA)
    + (VARP-RM2*VART)*(CE2*SA*CA)
  1 R(2,1)=F(1,2)
  R(1,3)=(VARP-RM2*VART)*SE*CE*SA
  R(3,1)=R(1,3)
  R(2,3)=(VARP-RM2*VART)*SE*CE*CA
  R(3,2)=R(2,3)

C 121 IF(ITH.EQ.-10) PRINT 317, (R(I,J),J=1,6),I=1,6
317 FORMAT(//,10X,'R ARRAY ',//,6(/,6F17.5),///)

C-----COMPUTE GAIN MATRIX (G)
DC 81 I=1,6
DC 81 J=1,6

```

```

JENT 7210
JENT 7220
JENT 7230
JENT 7240
JENT 7250
JENT 7260
JENT 7270
JENT 7280
JENT 7290
JENT 7300
JENT 7310
JENT 7320
JENT 7330
JENT 7340
JENT 7350
JENT 7360
JENT 7370
JENT 7380
JENT 7390
JENT 7400
JENT 7410
JENT 7420
JENT 7430
JENT 7440
JENT 7450
JENT 7460
JENT 7470
JENT 7480
JENT 7490
JENT 7500
JENT 7510
JENT 7520
JENT 7530
JENT 7540
JENT 7550
JENT 7560
JENT 7570
JENT 7580
JENT 7590
JENT 7600
JENT 7610
JENT 7620
JENT 7630
JENT 7640
JENT 7650
JENT 7660
JENT 7670
JENT 7680

```



```

      BDUM(I,J)=0.DO
      ADUM(I,J)=0.DO
      CALL PPROD(H:PP,3,6,6,ADUM)
      CALL PPROD(ADUM,HT,3,6,3,BDUM)
      DO 83 J=1,6
      DO 83 I=1,6
      ADUM(I,J)=0.DO
      CALL ADDSUB(BDUM,R,3,3,ADUM,1)
      DO 82 I=1,6
      DO 82 J=1,6
      BDUM(I,J)=0.DO
      CALL INVERT(3,ADUM,BDUM,KER,6)
      CALL (KER, EQ.2) PRINT 308
308  FORMAT(10X,25(1H*), 'INVERSION SINGULARITY ENCOUNTERED')
      DO 84 I=1,6
      DO 84 J=1,6
      ADUM(I,J)=0.DO
      CALL PPROD(PP,HT,6,6,3,ADUM)
      CALL PPROD(ADUM,BDUM,6,3,3,G)
      GNX=G(1,1)
      GNY=G(3,2)
      GNZ=G(5,3)
      C-----COMPUTE COVARIANCE OF ESTIMATION ARRAY (PE)
      DO 85 I=1,6
      DO 85 J=1,6
      ADUM(I,J)=0.DO
      BDUM(I,J)=0.DO
      CALL PPROD(G:H,6,3,6,ADUM)
      CALL ADDSUB(XIDENT,ADUM,6,6,2DUM,-1)
      CALL PPROD(BDUM,PP,6,6,6,PE)
      C-----COMPUTE COVARIANCE OF PREDICTION ARRAY (PP)
      DO 86 I=1,6
      DO 86 J=1,6
      ADUM(I,J)=0.DO
      BDUM(I,J)=0.DO
      CALL PPROD(PHI,PE,6,6,6,ADUM)
      CALL PPROD(ADUM,PHITRV,6,6,6,BDUM)
      CALL ADDSUB(BDUM,Q,6,6,PP,1)
      C-----BYPASS DETERMINISTIC FORCING EQUATIONS FOR FIRST
      C      SAMPLING PERIOD OF DTRAD
      C      IF (ITH.LE.INT) GO TO 65
      C-----COMPUTE NEW HEADING ANGLE AND HEADING ANGLE RATE, BASED ON
      C      UNBIASED COMMANDS AS SENT FROM THE CONTROLLER.
      C      PHN IS THE NEW POLL ANGLE

```



```

C      PSDN IS THE NEW TURNING ANGLE RATE
C      PSN IS THE NEW HEADING ANGLE
C      PHN=PHC+(PHI-PHC)*CAA2
C      CAL=GG/VTI
C      PSDN=CAL*PHN
C      DELPSI= CAL*(PHC*DT+CA5*(PHI-PHC))
C      PSIDEX=DELPSI/DT
C      PSN=PSI+DELPSI
C
C      CPSN=PSN/DEG
C      SPSN=DSIN(CPSN)
C      CPCS=DCCS(CPSN)
C
C      ----COMPUTE STATE PREDICTION VECTOR
C      66
C      XDIP(1)=VTI*SPSN
C      XDIP(2)=VTI*CPSN
C      XDIP(3)=XDI(3)
C
C      DELX(1)=DT3*(XDIP(1)+SN1)-CA4*(XDIP(2)*PSDN-SN2*PSDI)
C      DELX(2)=DT3*(XDIP(2)+SN2)-CA4*(-XDIP(1)*PSDN+SN1*PSDI)
C      DELX(3)=DT*XDI(3)
C
C      DO 110 I=1,3
C      XDIP(I)=XDIP(I)+WR(I)
C      XI(I)=XI(I)+DT*WR(I)+DELX(I)
C      110
C      IF(DTCUM.LT.DTRAD-EPS) GO TO 97
C      DTCUM=0.D0
C      IF(NWLD.LT.0) GO TO 67
C
C      DO 64 I=1,3
C      XI(I)=XI(I)
C      64
C      XDIP(I)=XDIP(I)
C      GO TO 65
C
C      ----COMPUTE STATE ESTIMATION VECTOR
C      67
C      E1=XDATA(1)-XI(1)
C      E2=XDATA(2)-XI(2)
C      E3=XDATA(3)-XI(3)
C
C      XI(1)=XI(1)+G(1,1)*E1+G(1,2)*E2+G(1,3)*E3
C      XI(1)=XDIP(1)+G(2,1)*E1+G(2,2)*E2+G(2,3)*E3
C      XI(2)=XI(2)+G(3,1)*E1+G(3,2)*E2+G(3,3)*E3
C      XI(2)=XDIP(2)+G(4,1)*E1+G(4,2)*E2+G(4,3)*E3
C      XI(3)=XI(3)+G(5,1)*E1+G(5,2)*E2+G(5,3)*E3
C      XI(3)=XDIP(3)+G(6,1)*E1+G(6,2)*E2+G(6,3)*E3
C
C      ----COMPUTE VALUES FOR ENTERING DETERMINISTIC CONTROL

```





```

C 65 CALCULATIONS ON NEXT ITERATION
      IF(I*TH.LT.INT) RETURN
      PHI=PHN
      PSDI=PSDN
      SN1=XDI(1)-WR(1)
      SN2=XDI(2)-WR(2)
      VTI=DSQRT(SN1*SN1+SN2*SN2)
      PSI=DATAI(2(SN1,SN2))
      CPS=DCOS(PSI)
      SPS=DSIN(PSI)
      PSI=PSI*DEG
      RETURN
      END

```

CCCCCCCC

```

SUBROUTINE MATCAL
  REAL*8 A,AA,B,C,D,DD,S,X,Y
  DIMENSION AA(1),X(1),LL(6),MM(6),Y(6,6),S(1),D(1),
    1A(6,6),S(6,6),C(6,6)

```

CC CCCCCC

```

ENTRY INVERT(N,AA,X,KER,K)

```

THIS SUBROUTINE INVERTS THE MATRIX A AND LEAVES THE  
RESULTS IN THE MATRIX X. N AND K AREA THE ORDER OF  
THE MATRIX.  
IF KER EQUALS 2 THEN A SINGULARITY HAS BEEN DETECTED.

```

      DO 1 I=1,N
      DO 1 J=1,N
      IND=(I-1)*K+J
      Y(I,J)=AA(IND)
      1 KER=1
      N2=2*N
      CALL APRAY(2,N,N,6,6,Y,Y)
      CALL DMINV(Y,N,DD,LL,MM)
      CALL ARAY(1,N,N,6,6,Y,Y)
      IF(DD.EQ.0) KER=2
      DO 2 I=1,N
      DO 2 J=1,N
      IND=(I-1)*K+J
      X(IND)=Y(I,J)
      2

```

I C 2

LENT 8650  
 LENT 8660  
 LENT 8670  
 LENT 8680  
 LENT 8690  
 LENT 8700  
 LENT 8710  
 LENT 8720  
 LENT 8730  
 LENT 8740  
 LENT 8750  
 LENT 8760  
 LENT 8770  
 LENT 8780  
 LENT 8790  
 LENT 8800  
 LENT 8810  
 LENT 8820  
 LENT 8830  
 LENT 8840  
 LENT 8850  
 LENT 8860  
 LENT 8870  
 LENT 8880  
 LENT 8890  
 LENT 8900  
 LENT 8910  
 LENT 8920  
 LENT 8930  
 LENT 8940  
 LENT 8950  
 LENT 8960  
 LENT 8970  
 LENT 8980  
 LENT 8990  
 LENT 9000  
 LENT 9010  
 LENT 9020  
 LENT 9030  
 LENT 9040  
 LENT 9050  
 LENT 9060  
 LENT 9070  
 LENT 9080  
 LENT 9090  
 LENT 9100  
 LENT 9110  
 LENT 9120



```

CC      ENTRY ADDSUB(A,B,N,M,C,ISIGN)
CC      THIS SUBROUTINE ADDS(ISIGN=1) OR SUBTRACTS(ISIGN=-1)
CC      THE NXM MATRICES A AND B (A+B OR A-B) ,
CC      STORING THE RESULT IN C.
125      DO 125 I=1,N
CC      DO 125 J=1,M
CC      C(I,J)=A(I,J)+FLDAT(ISIGN)*B(I,J)
CC      RETURN
CC      ENTRY PROD(A,B,N,M,L,C)
CC      THIS SUBROUTINE COMPUTES THE MATRIX PRODUCT AB
CC      AND STORES THE RESULT IN C. A IS NXM, B IS MXL, AND C IS NXL.
3      DO 3 I=1,N
CC      DO 3 J=1,L
CC      C(I,J)=0.00
CC      DO 126 I=1,N
CC      DO 126 J=1,L
CC      DO 126 K=1,M
CC      C(I,J)=C(I,J)+A(I,K)*B(K,J)
CC      RETURN
CC      ENTRY TRANS(A,N,M,C)
CC      THIS SUBROUTINE TRANSPOSES THE NXM MATRIX A
CC      AND STORES THE RESULT AS THE MXN MATRIX C.
127      DO 127 I=1,N
CC      DO 127 J=1,M
CC      C(J,I)=A(I,J)
CC      RETURN
CC      ENTRY SUBROUTINE ARRAY(MODE,I,J,N,M,S,D)
CC      DIMENSION S(1),D(1)
CC      REAL*8 S,D
CC      NI=N-I
CC      IF(MODE-1) 100,100,120
CC      IJ=I*J+1
CC      NI=M*J+1
CC      DO 110 K=1,J
CC      NI=NI-NI

```



JENT 9610  
 JENT 9620  
 JENT 9630  
 JENT 9640  
 JENT 9650  
 JENT 9660  
 JENT 9670  
 JENT 9680  
 JENT 9690  
 JENT 9700  
 JENT 9710  
 JENT 9720  
 JENT 9730  
 JENT 9740  
 JENT 9750  
 JENT 9760  
 JENT 9770  
 JENT 9780  
 JENT 9790  
 JENT 9800  
 JENT 9810  
 JENT 9820  
 JENT 9830  
 JENT 9840  
 JENT 9850  
 JENT 9860  
 JENT 9870  
 JENT 9880  
 JENT 9890  
 JENT 9900  
 JENT 9910  
 JENT 9920  
 JENT 9930  
 JENT 9940  
 JENT 9950  
 JENT 9960  
 JENT 9970  
 JENT 9980

45.0

45.0

50.0

50.0

500.

500.

500.

50.0

10.0

10.0

14.1414

14.1414

DO 110 L=1,I  
 IJ=IJ+1  
 NM=NM+1  
 D(VN)=S(IJ)  
 GO TO 140  
 IJ=0  
 NM=0  
 DO 120 K=1,J  
 DO 125 L=1,I  
 IJ=IJ+1  
 NM=NM+1  
 S(IJ)=D(NM)  
 NM=NM+1  
 RETURN  
 END

110

120

125

130

140

CCCCCCCC

BLOCK DATA REAL\*8(Z)  
 INPLCIT,RCCM/Z1(14)  
 COMMON/RADCCM/Z2(26)  
 DATA Z1/14\*0.0/  
 DATA Z2/26\*0.0/  
 END

CCCCCCCC

/GO,SYSIN DD \*  
 3 50.0 45.0  
 10.0 0.0  
 10.0 90.0  
 14.1414 225.0  
 14.1414 225.0  
 DESIRED,TRUE, AND ESTIMATED POSITION



## LIST OF REFERENCES.

1. Benedict, T. R. and Bordner, G. W., "Synthesis of an Optimal Set of Radar Track-While-Scan Smoothing Equations," IRE Transactions on Automatic Control, February 1962.
2. Mills, E. H., Applying the Kalman Filter to the Emitter Location Problem Using Airborne Angle of Arrival Information, MS Thesis, Naval Postgraduate School, Monterey, California, Marcy 1973.
3. Meditch, J. S., Stochastic Optimal Linear Estimation and Control, McGraw-Hill Book Co., Inc., 1969.
4. Demetry, J. S., Notes on the Theory and Application of Optimal Estimation, paper presented and copyrighted for use at the Naval Postgraduate School, Monterey, California, 1970.
5. Berkowitz, K., "AN/TPQ-27 Precision Guidance-Autopilot Bias Compensation," AN/TPQ-27 Program Memorandum SQM-3000-7, 5 March 1971.
6. "Design of AN/TPQ-27 Precision Guidance System," AN/TPQ-27 Program Memorandum SQM-3000-6, 24 July 1970.
7. Wylie, C. R. Jr., Advanced Engineering Mathematics, McGraw-Hill Book Co., Inc., 1966.
8. Hartnett, E. J., "Pre-Mission Flight Planning- I: Mathematical Analysis," AN/TPQ-27 Program Memorandum SQM-3000-17, 14 August 1973.
9. Shucker, S., "Coarse Guidance System Changes - I: Mathematics," AN/TPQ-27 Program Memorandum SQM-3000-18, 23 August 1973.
10. Aldrich, G. T. and Krabill, W. B., "An Application of Kalman Techniques to Aircraft and Missile Radar Tracking," Paper 72-838, AIAA Guidance and Control Conference, Stanford, California, August 1972.
11. Johnson, R. S., "SPECTRA 70 Program Specification," unnumbered AN/TPQ-27 Program Memorandum, 18 March 1970.





# INITIAL DISTRIBUTION LIST

|   | No. Copies |
|---|------------|
| 1. Defense Documentation Center<br>Cameron Station<br>Alexandria, Virginia 22314  | 2          |
| 2. Library, Code 0212<br>Naval Postgraduate School<br>Monterey, California 93940  | 2          |
| 3. Department Chairman<br>Department of Electrical Engineering<br>Naval Postgraduate School<br>Monterey, California 93940   | 1          |
| 4. Professor H. A. Titus<br>Department of Electrical Engineering<br>Naval Postgraduate School<br>Monterey, California 93940 | 20         |
| 5. Professor S. Jaurequi<br>Department of Electrical Engineering<br>Naval Postgraduate School<br>Monterey, California 93940 | 1          |
| 6. LT Robert Eugene Lentz, USN<br>SMC #1507<br>Naval Postgraduate School<br>Monterey, California 93940                      | 1          |



18 OCT 77  
23 JAN 78  
6 OCT 82

24445

275751

Thesis  
L526 Lentz  
c.1

156198

Improvement of AN/TPQ-  
27 filter and control  
techniques.

18 OCT 77  
23 JAN 78  
6 OCT 82

24445

275751

Thesis  
L526 Lentz  
c.1

156198

Improvement of AN/TPQ-  
27 filter and control  
techniques.

thesL526

Improvement of AN/TPQ-27 filter and cont



3 2768 001 03192 5

DUDLEY KNOX LIBRARY